

Towards an Improvement of the Water Balance on Steep Slopes -  
Development of a Correction Algorithm of the Runoff Curve Number  
for Slope Angles up to 100%

Para um aperfeiçoamento do balanço hídrico em encostas íngremes –  
Desenvolvimento de um Algoritmo de Correção da “Curva-Número”  
para declividades até 100%

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# Motivation

## Motivação

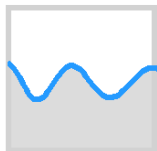
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Reliable estimations of stream flow, soil erosion or nutrients critical for model-based scenario evaluations

The crucial processes should be represented adequately for the conditions of the research region

SWAT-based study on diffuse matter inputs in the Three Gorges Region, China, with very steep slopes (average slope: 40%)

Critical question for representation of processes in SWAT:  
**How do HRUs in SWAT behave with slope?**



# Experimental Design

## A estrutura do projeto experimental

- **Experimental design:**

SWAT model with only one subbasin containing one HRU

- different vegetation types
- different soil types with uniform soil depth
- two years run (1 year warmup)
- climate data from Xiangxi catchment (China): 1116 mm/a

**Parametrization:**

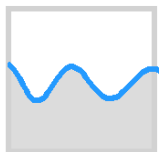
HRU area: 5 km<sup>2</sup>

Soil Depth: 1000 mm

Slope Length: *variable*

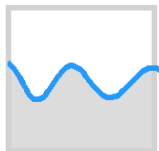
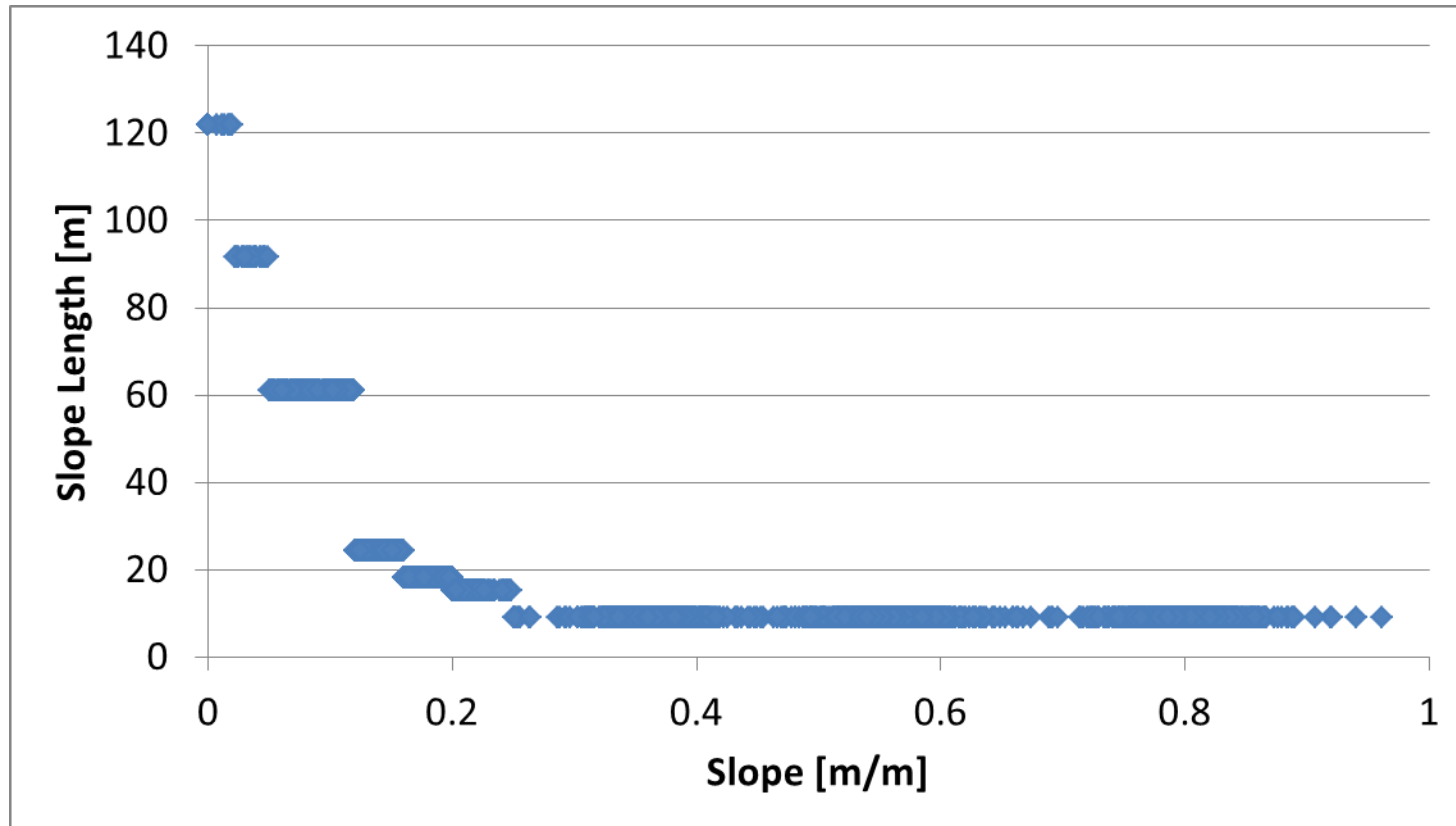
Land Use	Agricultural Land	Fallow Land	Forest	Rangeland
CN2	77	86	55	61
USLE_C	0.200	1.000	0.001	0.003
Soil	Brown	Limestone	Yellow Brown	Yellow
SOL_AWC	0.15	0.15	0.15	0.14
SOL_BD	1.00	1.20	1.43	1.40
SOL_K	26.10	26.10	26.10	8.38
Texture (S/U/C [%])	21.8/48.4/29.8	16.5/16.9/66.6	39.2/47.6/13.2	32.6/39.0/28.4
USLE_K	0.43	0.34	0.39	0.30

**- HRU slope is varied > Annual output from output.hru**



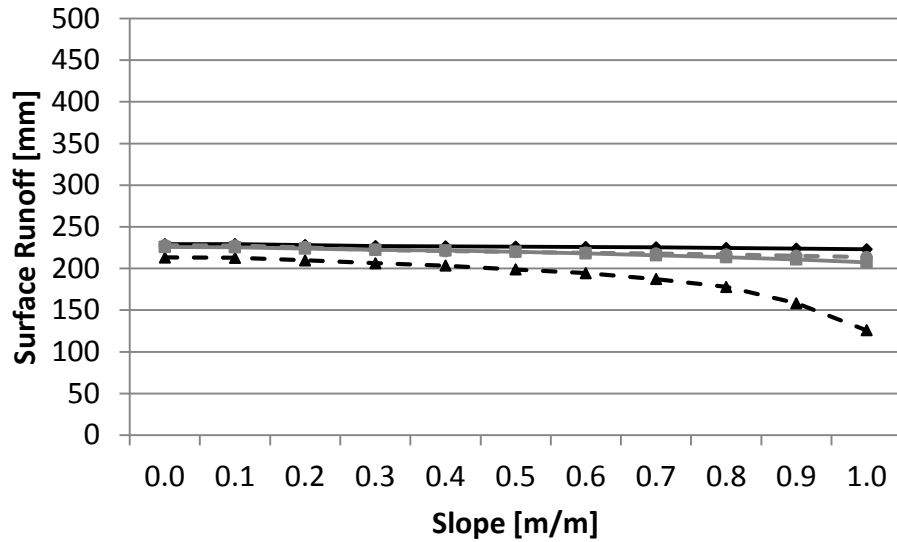
# Relation between Slope and Slope Length

## Relação entre declividade e comprimento da encosta

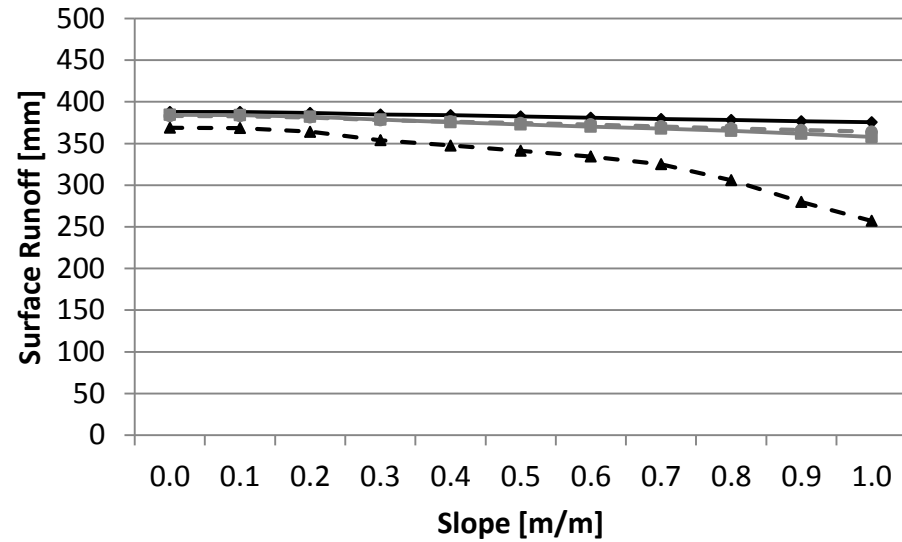


# SUR\_Q - Surface Runoff – Escoamento Superficial

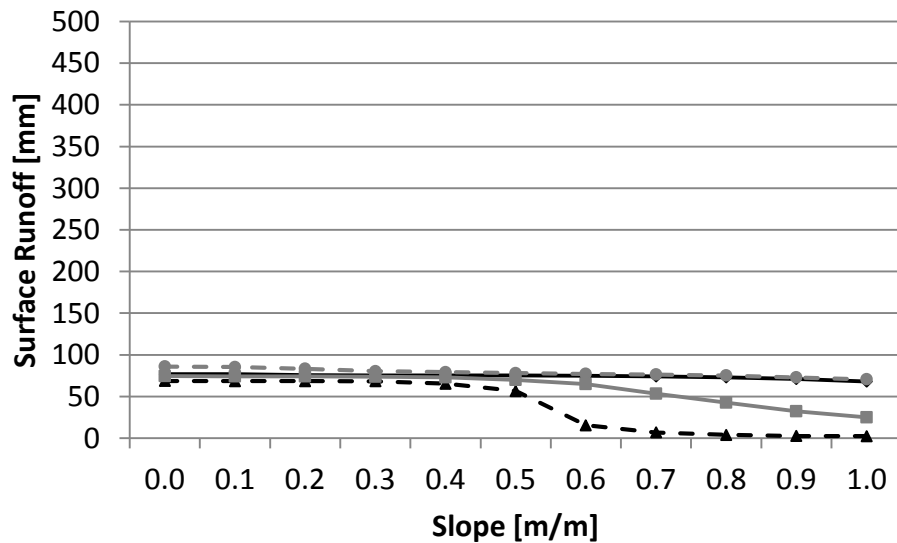
## Agricultural Land



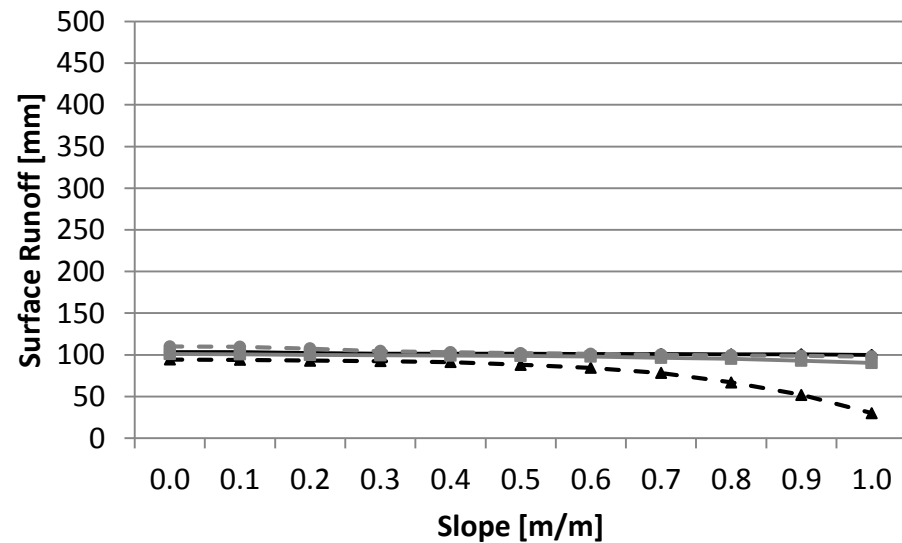
## Fallow Land



## Evergreen Forest



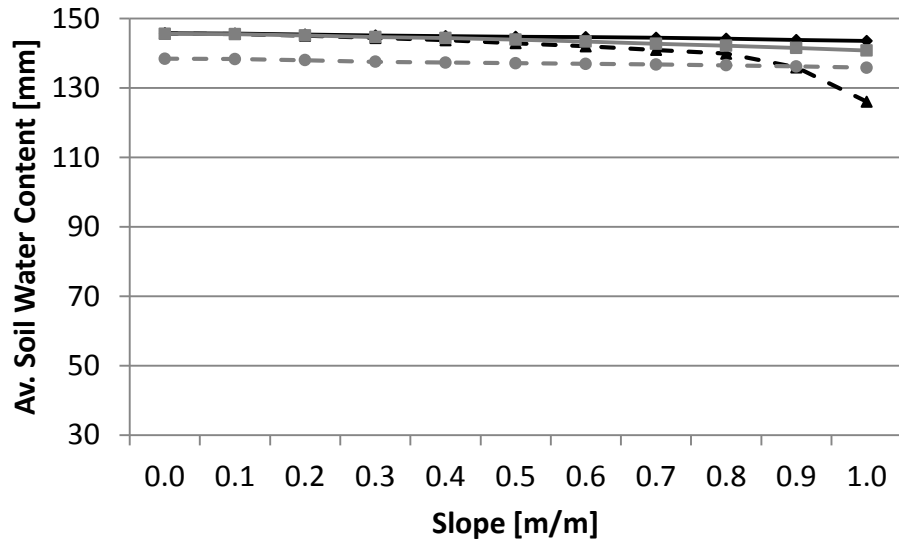
## Rangeland



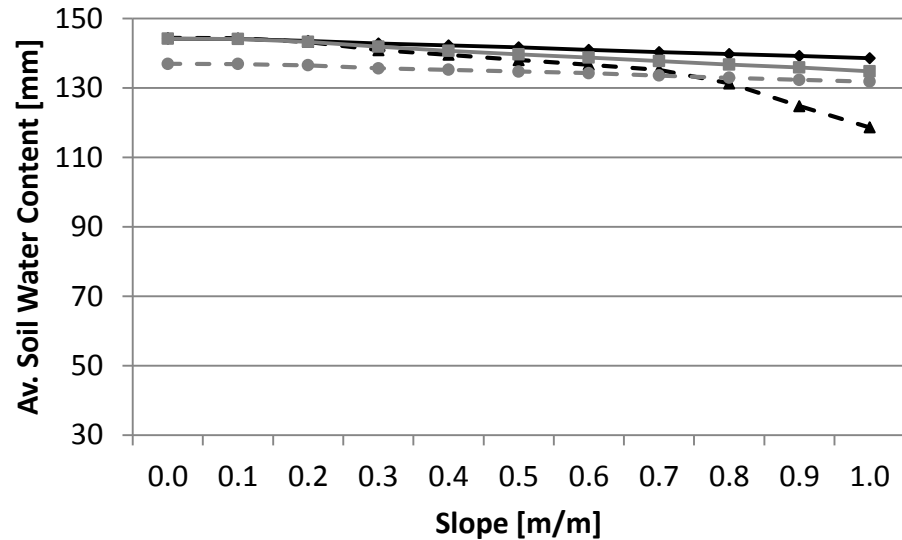
—●— Brown Soil    -▲- Limestone Soil    —■— Yellow Brown Soil    -◆- Yellow Soil

# SW - Soil Water Content - Umidade do Solo

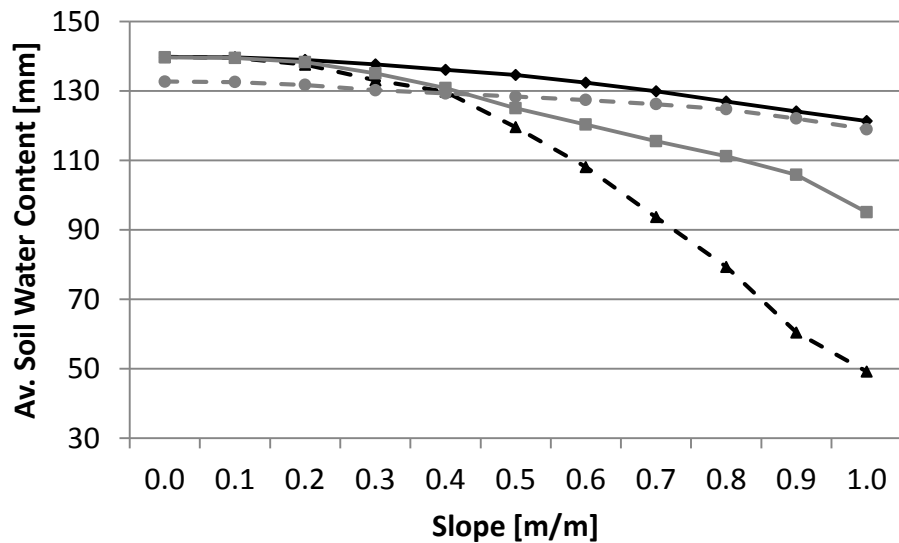
## Agricultural Land



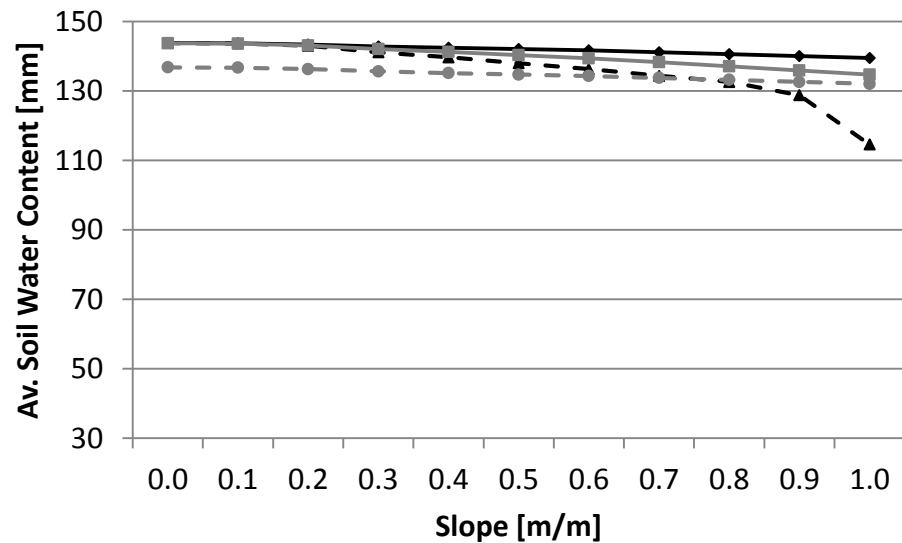
## Fallow Land



## Evergreen Forest



## Rangeland

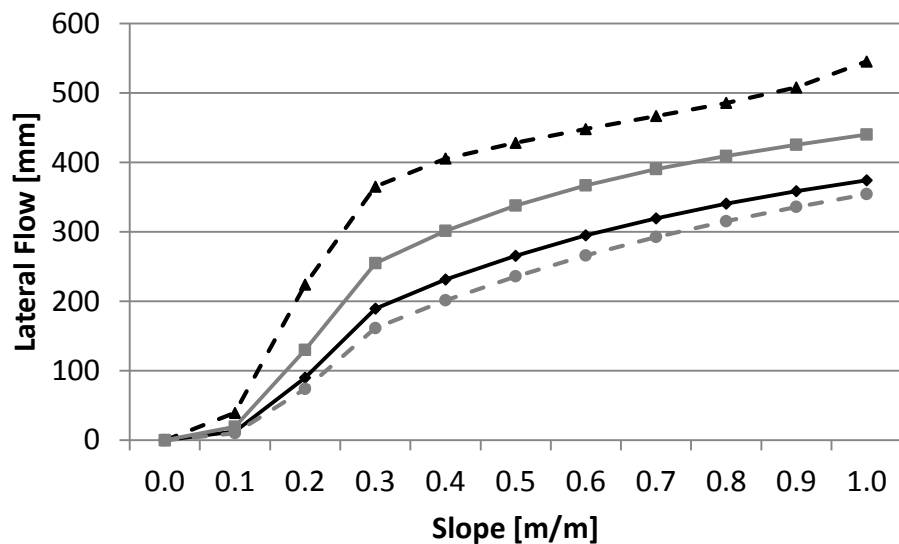


—◆— Brown Soil    -▲- Limestone Soil    —■— Yellow Brown Soil    -●- Yellow Soil

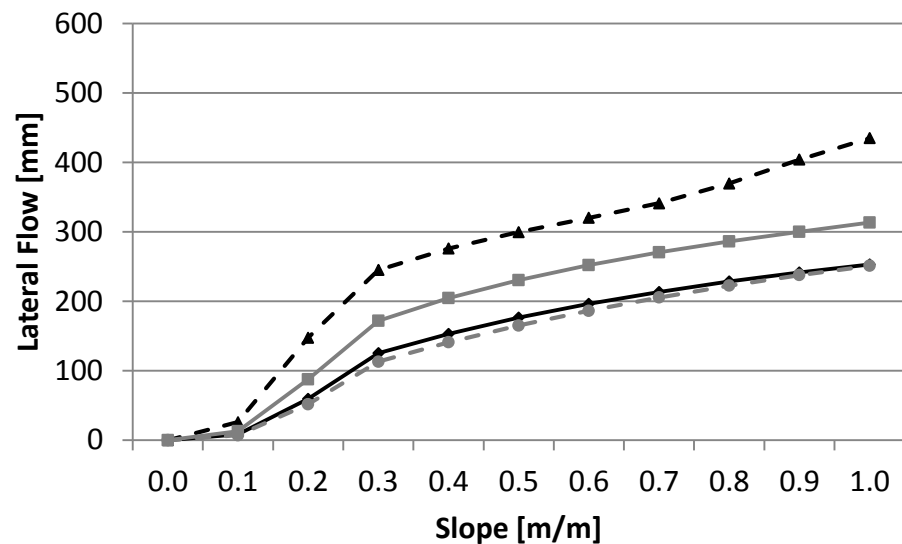


# LAT\_Q - Lateral Flow – Escoamento Lateral

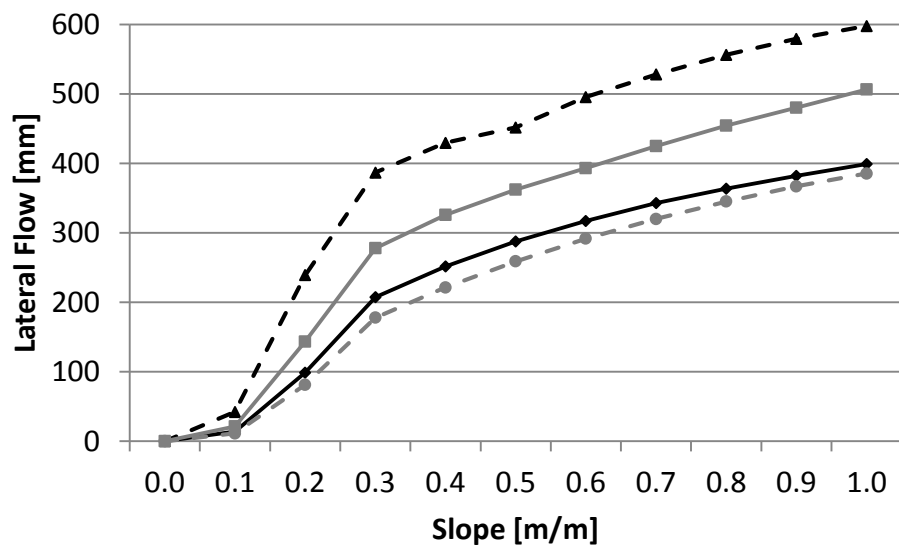
## Agricultural Land



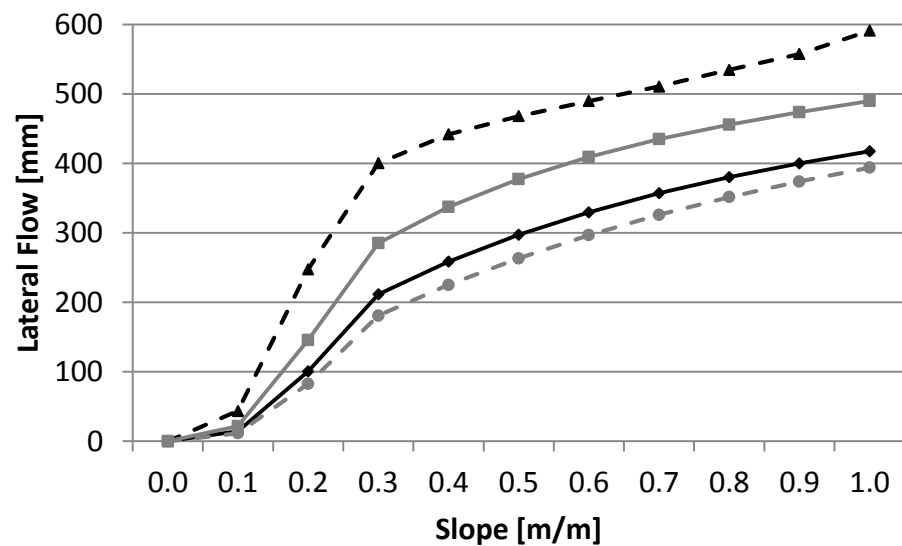
## Fallow Land



## Evergreen Forest



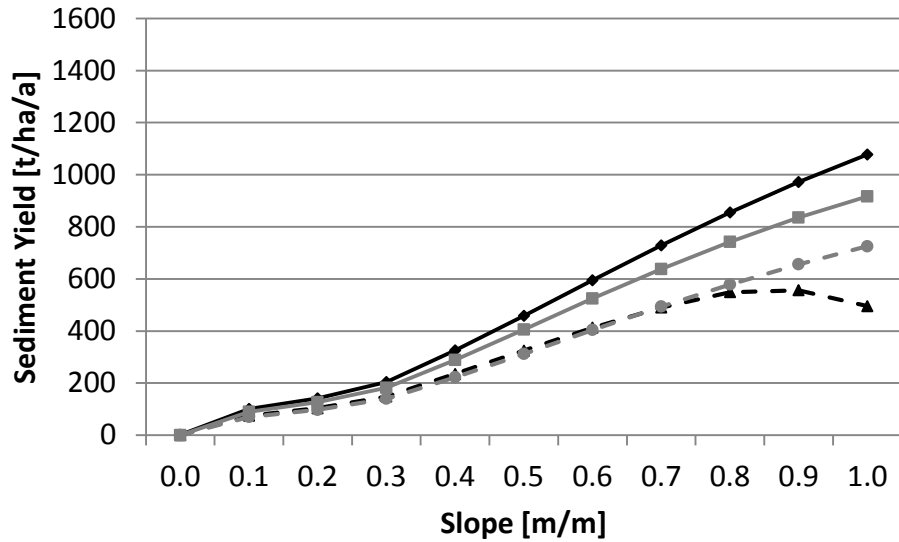
## Rangeland



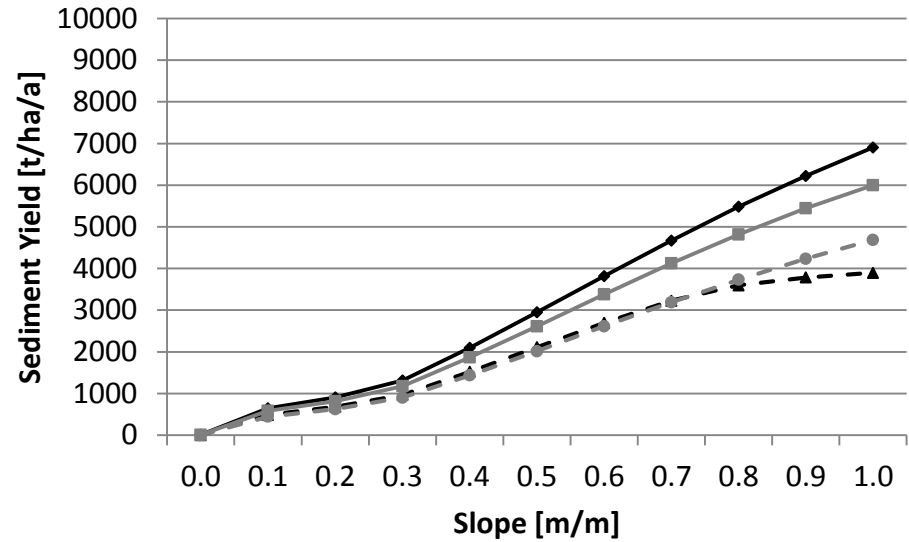
—◆— Brown Soil    -▲- Limestone Soil    —■— Yellow Brown Soil    -●- Yellow Soil

# SED\_YLD - Sediment Yield - Produção de sedimentos

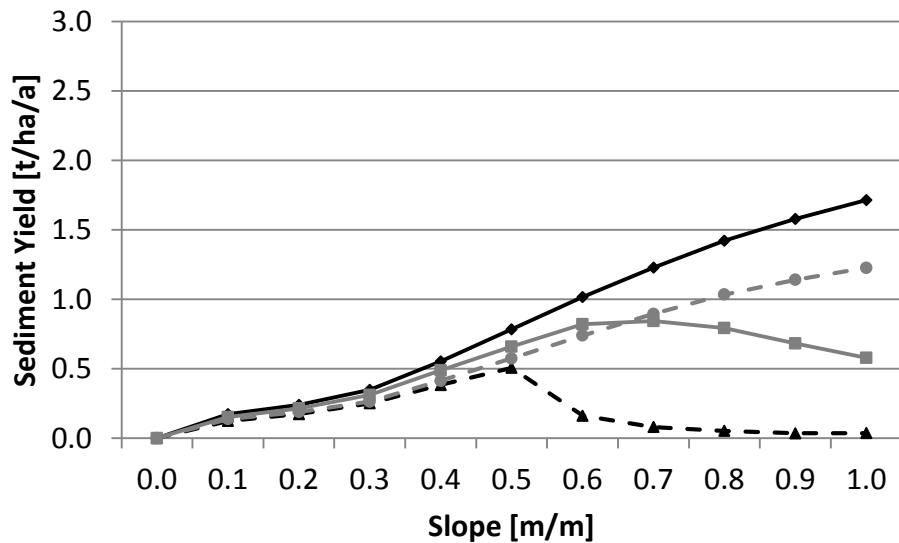
## Agricultural Land



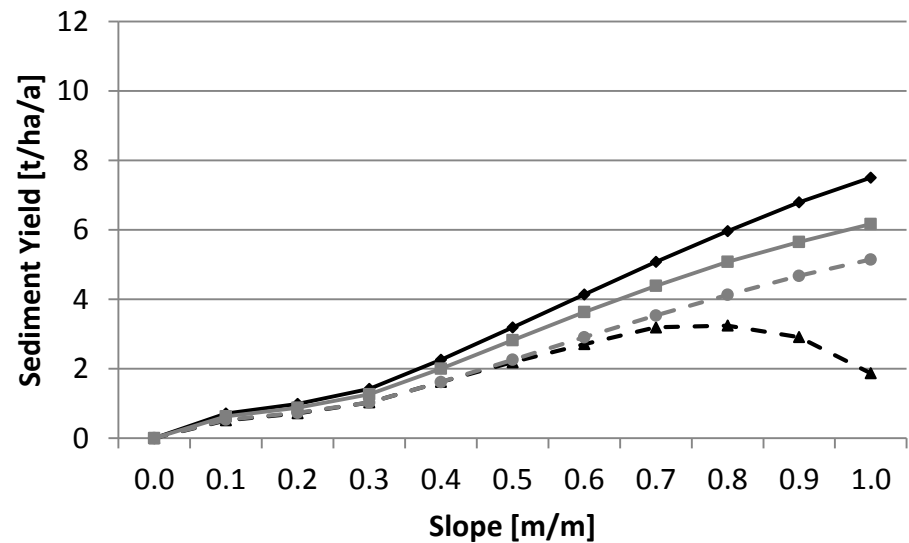
## Fallow Land



## Evergreen Forest



## Rangeland



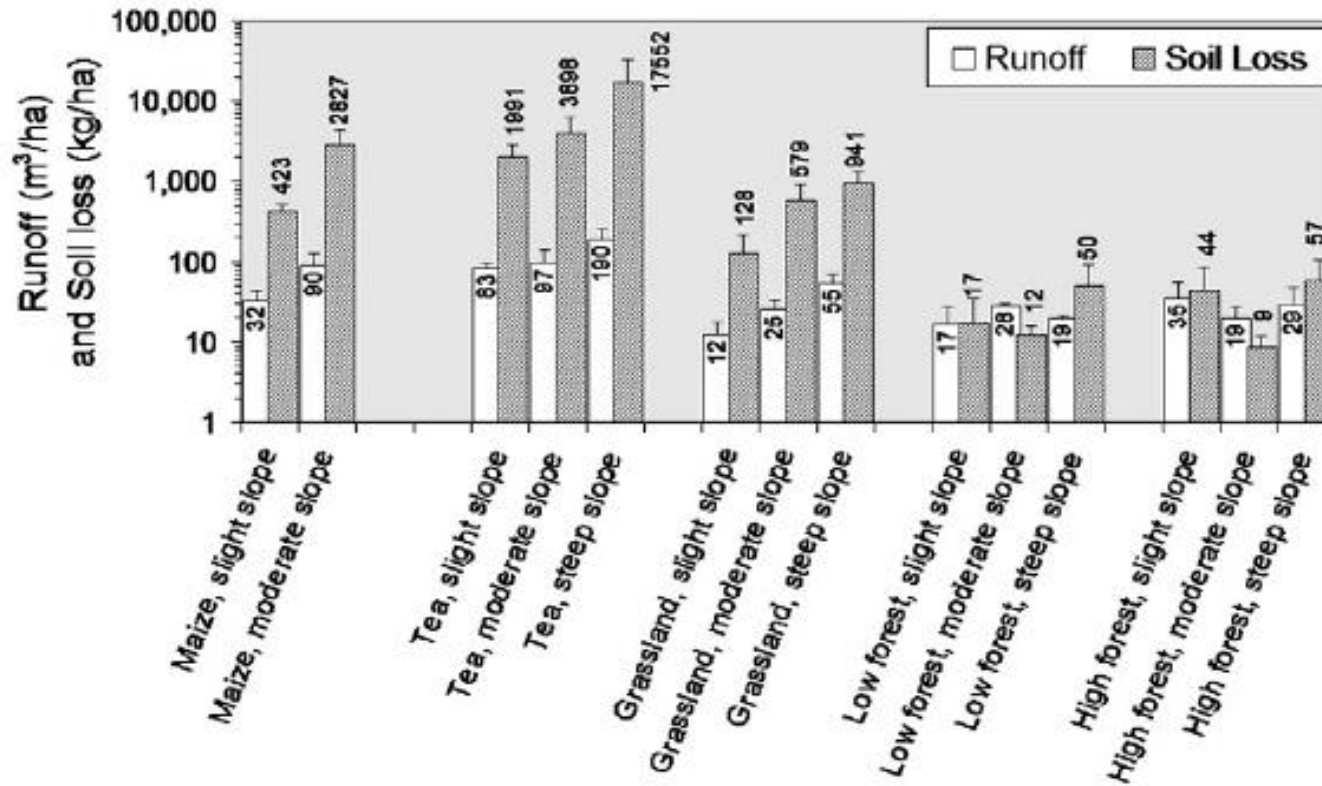
—◆— Brown Soil    -▲- Limestone Soil    —■— Yellow Brown Soil    -●- Yellow Soil



# How does surface runoff behave with slope?

Como o escoamento superficial se comporta em relação à declividade?

- Surface runoff:  
Increases with increasing slope angle  
e.g. El Kateb et al., 2013



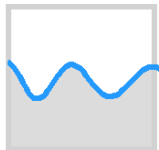
Many other studies also confirm this relation, e.g. Chaplot & Bissonais, 2003  
Haggard et al., 2002  
Barros et al., 1999

How does surface runoff behave with slope?

Como o escoamento superficial se comporta em relação à declividade?

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- According to Huang et al. (2006) surface runoff increases with slope due to:
  1. a reduction of the initial abstraction (Huang, 1995; Fox et al., 1997; Chaplot & Bissonnais, 2003)
  2. a decrease in infiltration
  3. a reduction of the recession time of overland flow (Evet & Dutt, 1985)



# Correction Algorithms for CN

## Algoritmos de correção para CN

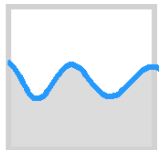
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- Williams (1995):

$$CN_{2s} = \frac{(CN_3 - CN_2)}{3} \cdot [1 - 2 \cdot \exp(-13.86 \cdot slp)] + CN_2$$

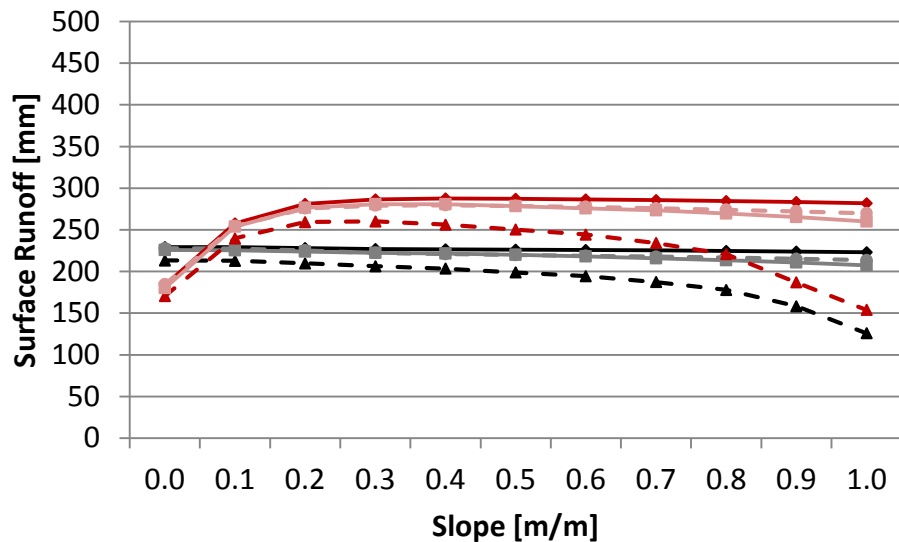
- Huang et al. (2006):

$$CN_{2s} = CN_2 \frac{322.79 + 15.63 \cdot slp}{slp + 323.52}$$

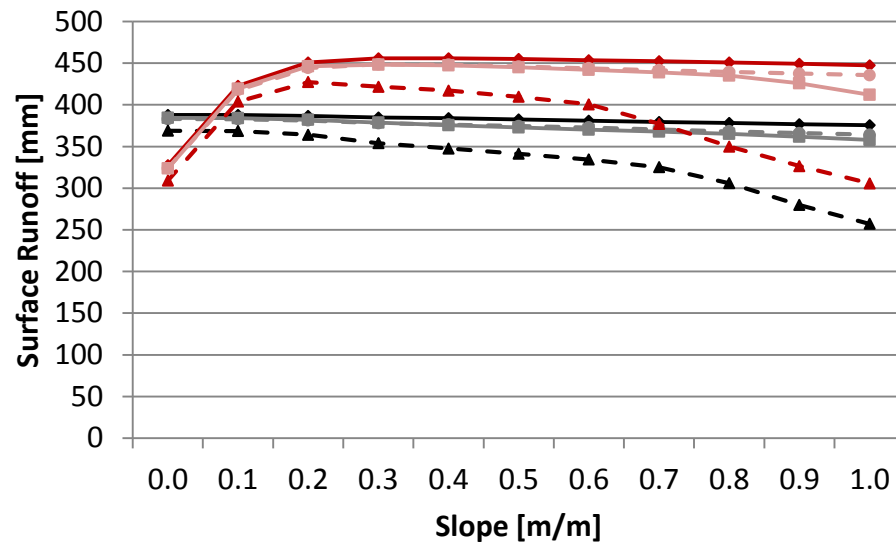


# Slope Correction – Correção de declividade – Williams, 1995

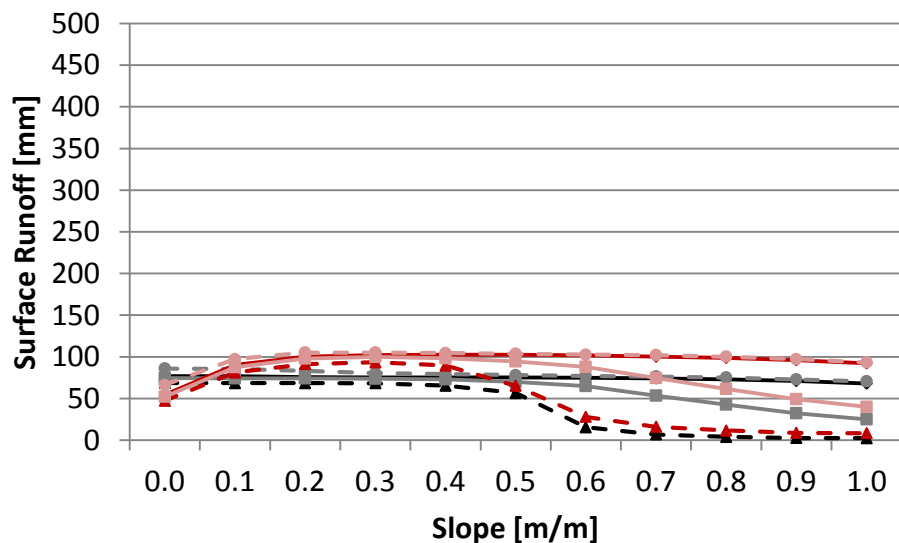
## Agricultural Land



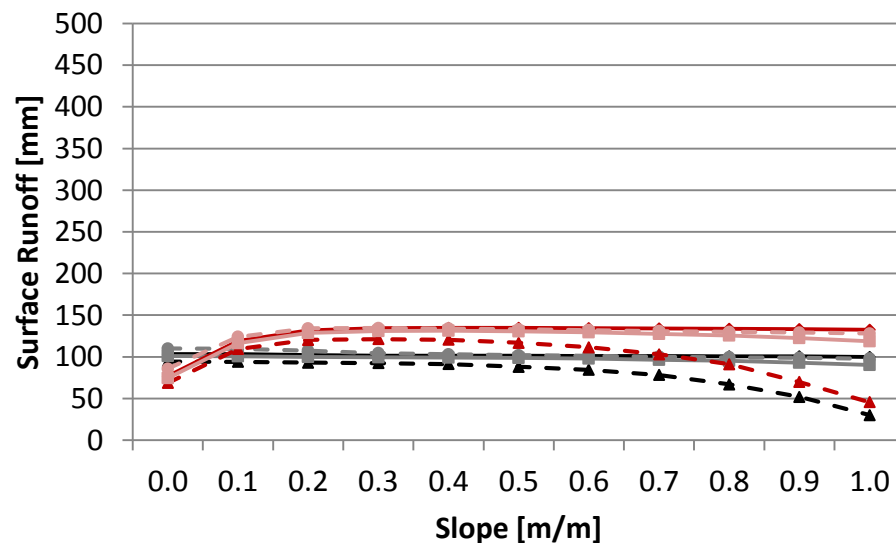
## Fallow Land



## Evergreen Forest



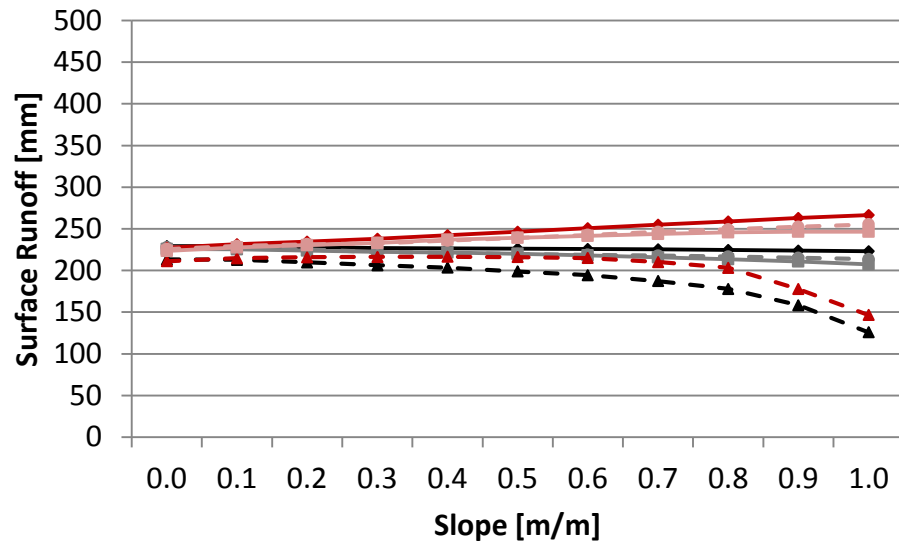
## Rangeland



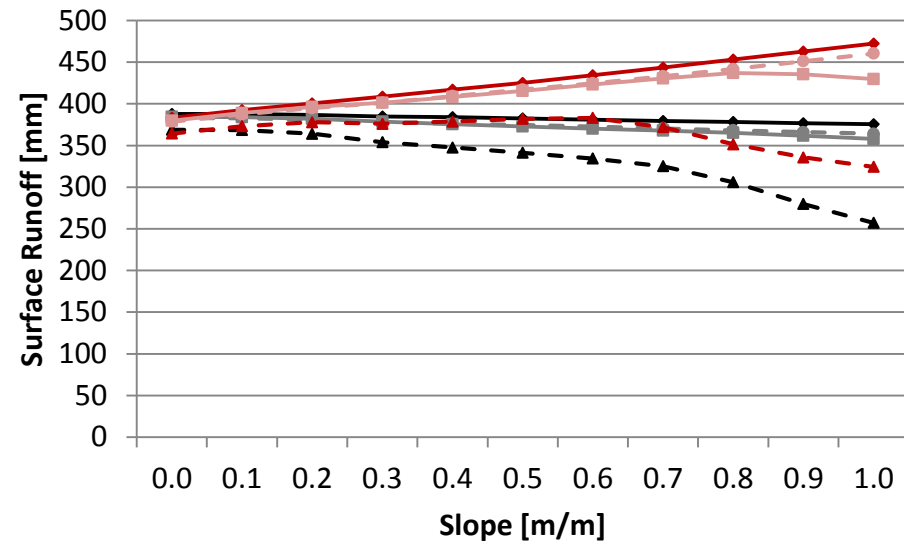
Brown Soil    
  Limestone Soil    
  Yellow Brown Soil    
  Yellow Soil

# Slope Correction – Correção de declividade – Huang et al., 2006

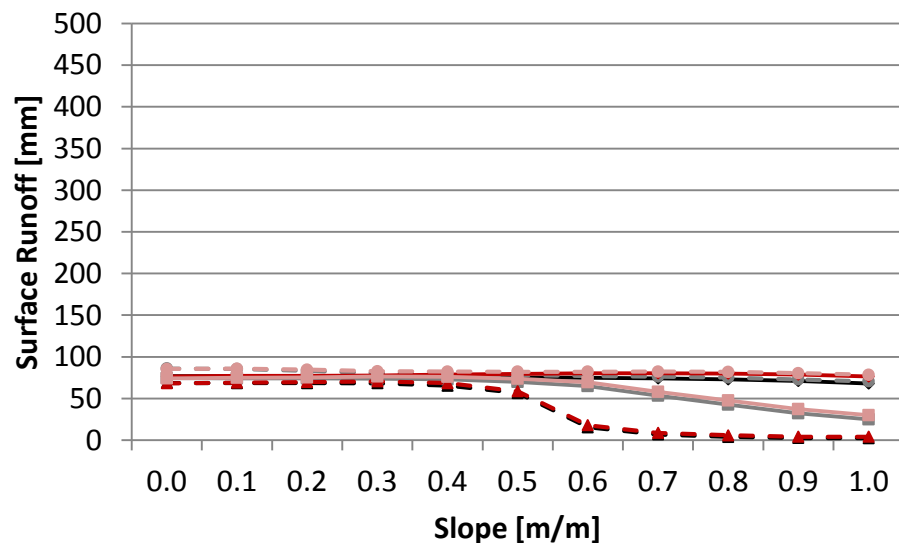
## Agricultural Land



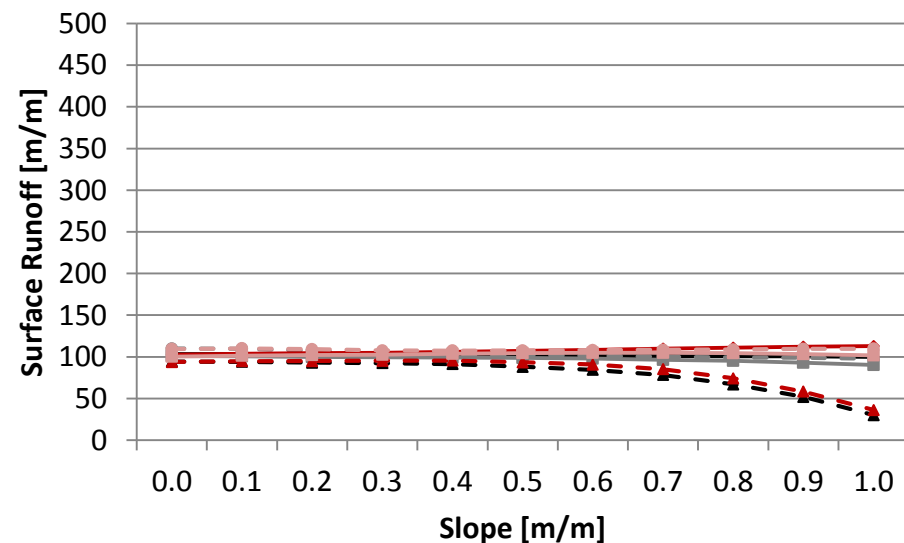
## Fallow Land



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## Rangeland



Brown Soil
  Limestone Soil
  Yellow Brown Soil
  Yellow Soil

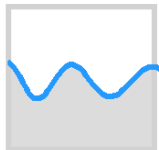
# Development of a new CN correction algorithm for slopes up to 100%

## Desenvolvimento de um novo algoritmo de correção da CN para declividades até 100%

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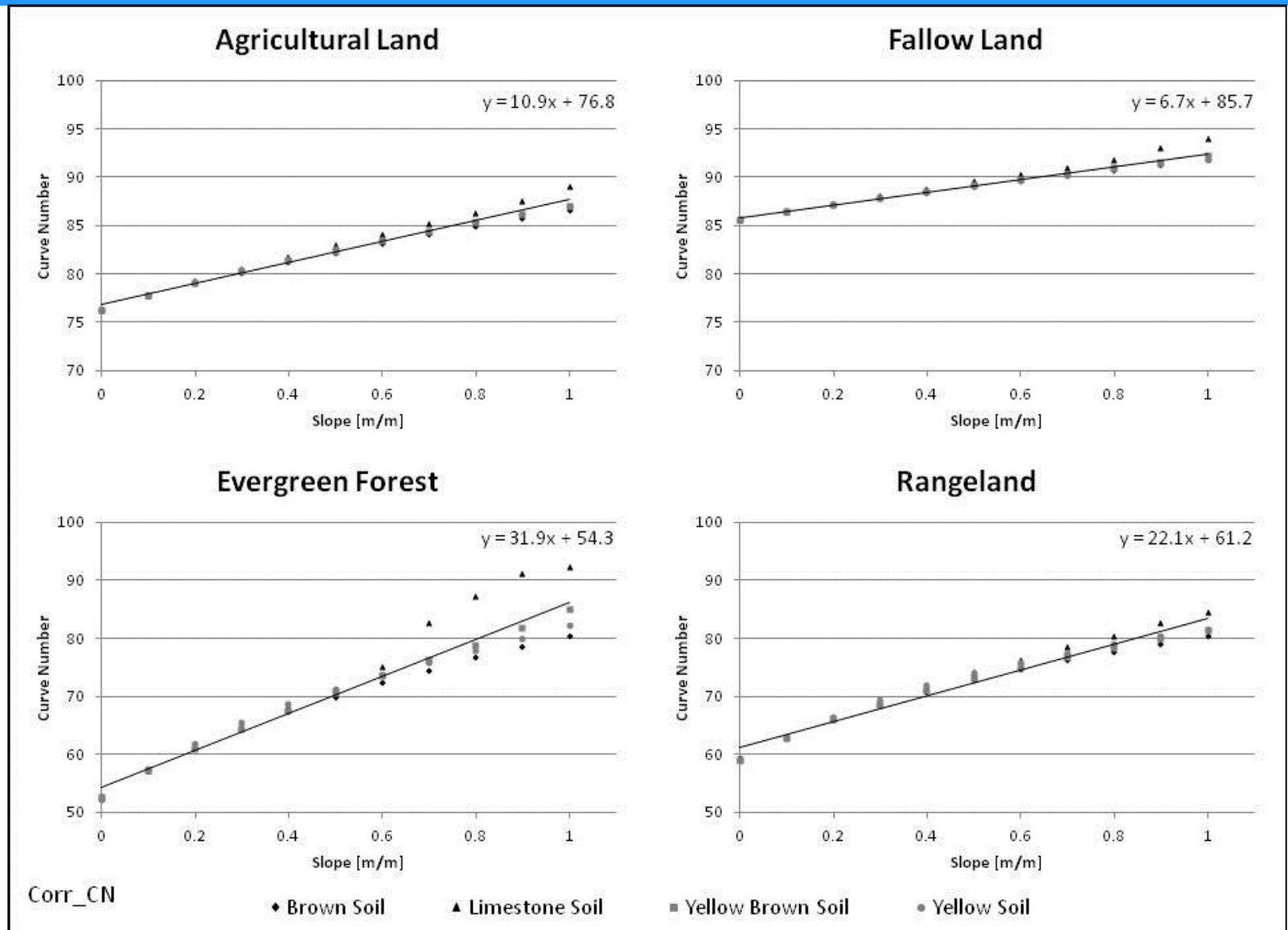
Data analysis of different studies, e.g.:

- Haggard et al., 2005
- Huang et al., 2006
- El Kateb et al., 2013
  
- Data analysis from these studies suggests a linear increase of surface runoff with slope by 1.5% of the annual precipitation sum per 10% slope increment on agricultural land
  
- With this, for the test dataset (1116 mm/a), the surface runoff increase per 10% slope increment was defined as 16.7 mm
  
- The curve numbers to meet the desired increase rate were determined with an iterative approach using the single-HRU models



# Ideal curve number values for the Slope Correction Algorithm

## Valores ideais da CN para o Algoritmo de Correção da Declividade

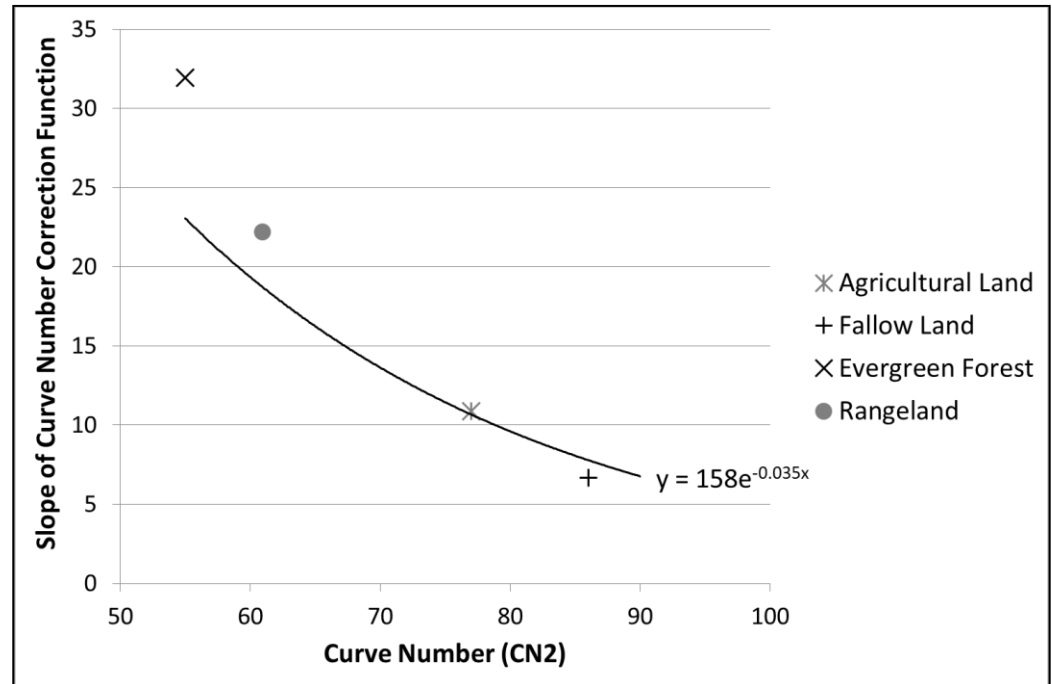




# Development of a CN correction algorithm for slopes up to 100%

## Desenvolvimento de algoritmo de correção da CN para declividades até 100%

- To adjust the rate of CN correction for different land uses, the initial CN was used
- With the adjustment of the correction function, also the lower surface runoff increase rates for forest and shrubland could be implemented
- With this the CN correction equation can be written as:



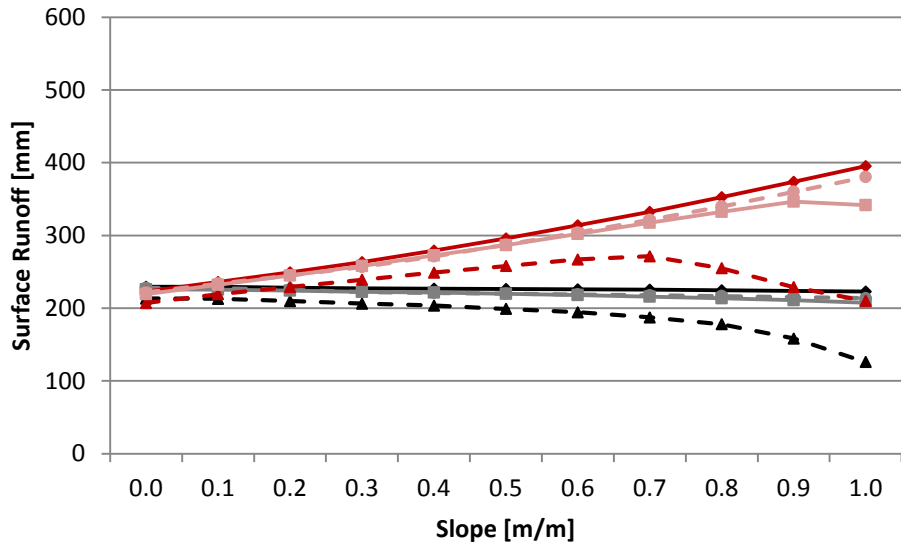
$$CN_{korr} = a \cdot slp + CN2 \cdot (1 - 0.05 \cdot a)$$

with

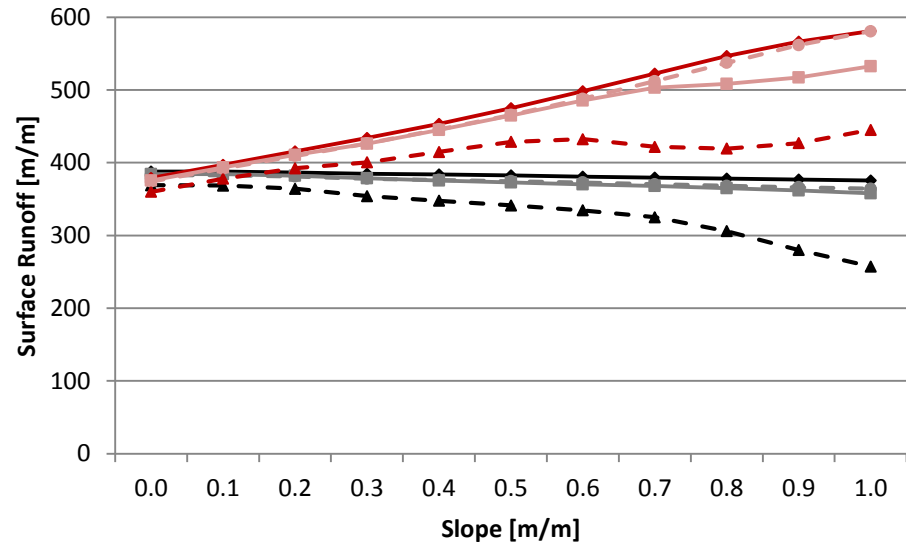
$$a = 158 \cdot \exp(-0.035 \cdot CN2)$$

# New CN Slope Correction Algorithm – Novo Algoritmo de Correção da Declividade da CN

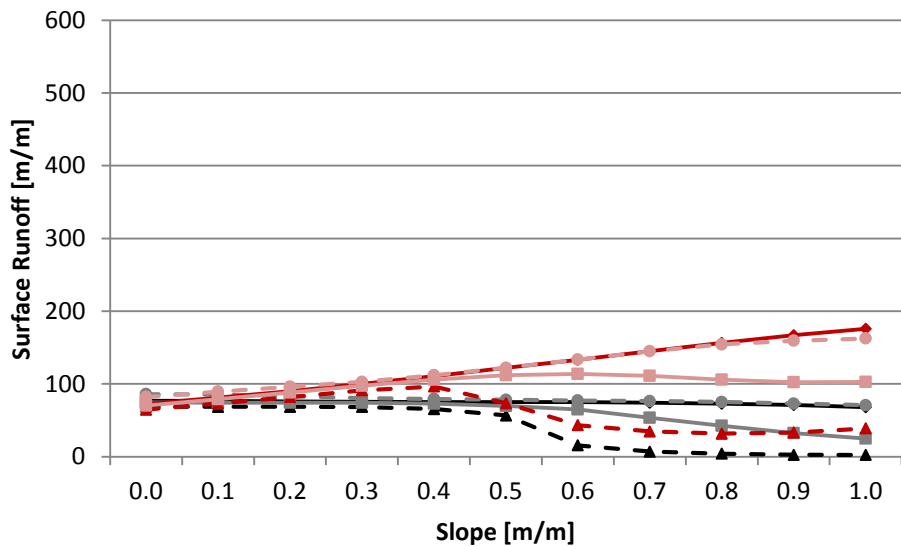
## Agricultural Land



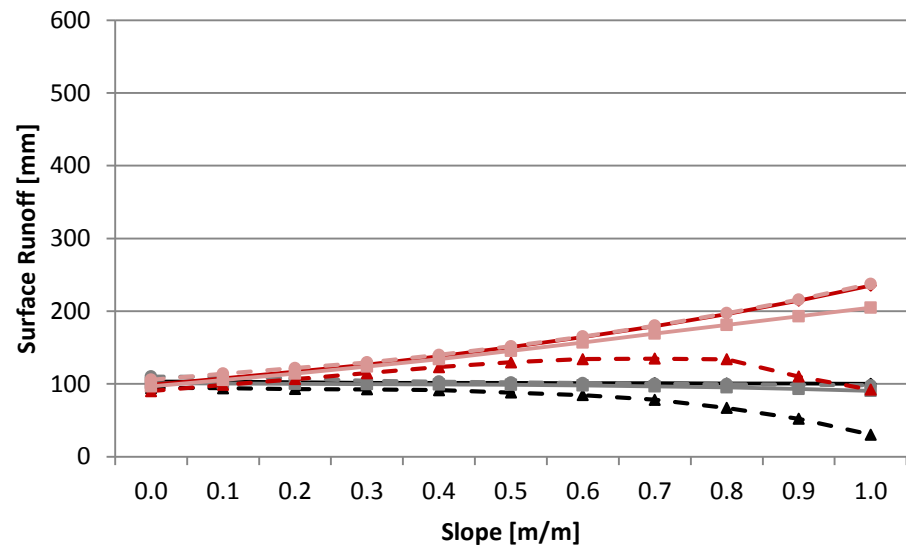
## Fallow Land



## Evergreen Forest



## Rangeland

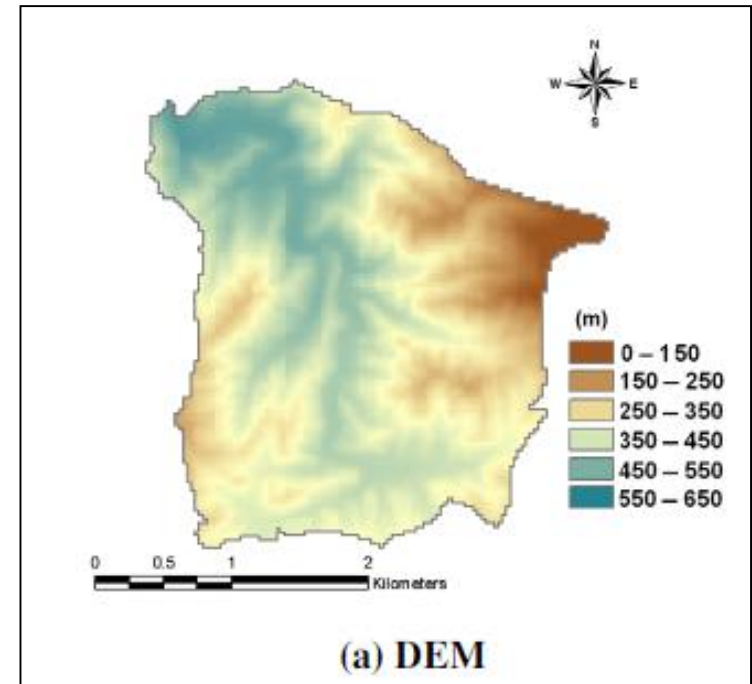
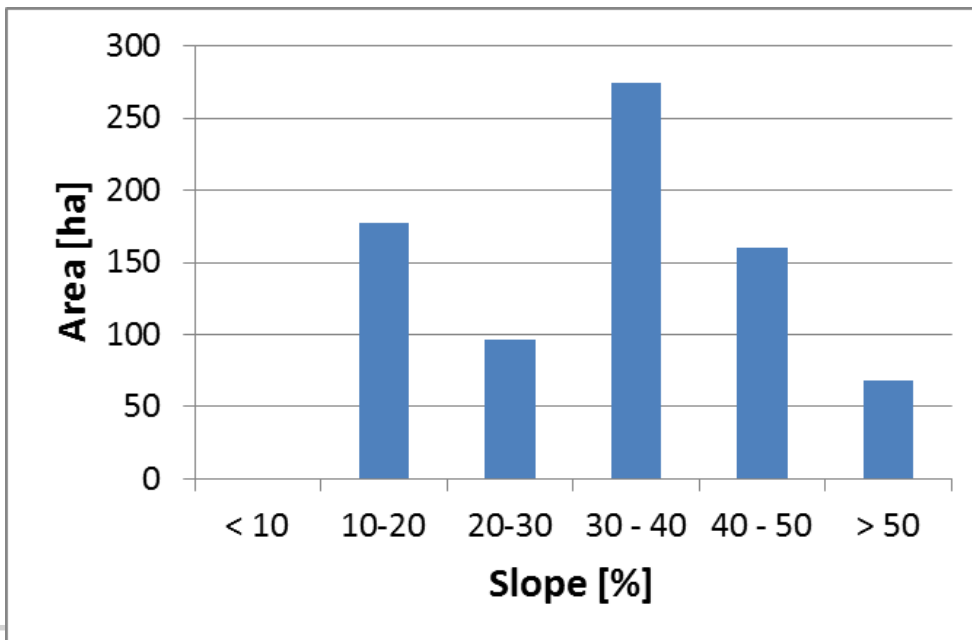


Brown Soil
  Limestone Soil
  Yellow Brown Soil
  Yellow Soil

# Test of the New CN Correction Algorithm

## Teste do Novo Algoritmo de Correção da CN

- Steep-sloping watershed in the northwest of South Korea
- Area: 7.8 km<sup>2</sup>
- Mainly forested (~70%)
- Annual Precipitation: 1210 mm



Source: Joh et al., 2011

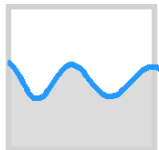
# Test of the New CN Correction Algorithm

## Teste do Novo Algoritmo de Correção da CN

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### **Method:**

- Implementation of the different slope correction algorithms in the source code of SWAT
- Separate calibration of streamflow for every slope correction algorithm
- No calibration of the curve number (CN2)



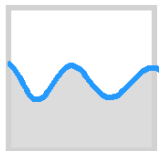
# Test of the New CN Correction Algorithm

## Teste do Novo Algoritmo de Correção da CN

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Evaluation statistics (2004-2006):

Statistical Parameter	unmodified	Williams, 1995	Huang et al., 2006	New Algorithm
R <sup>2</sup>	0.935	0.934	0.936	0.935
NSE	0.803	0.827	0.821	0.842
RSR	0.444	0.416	0.423	0.398
PBIAS	16.28	22.85	19.66	11.18

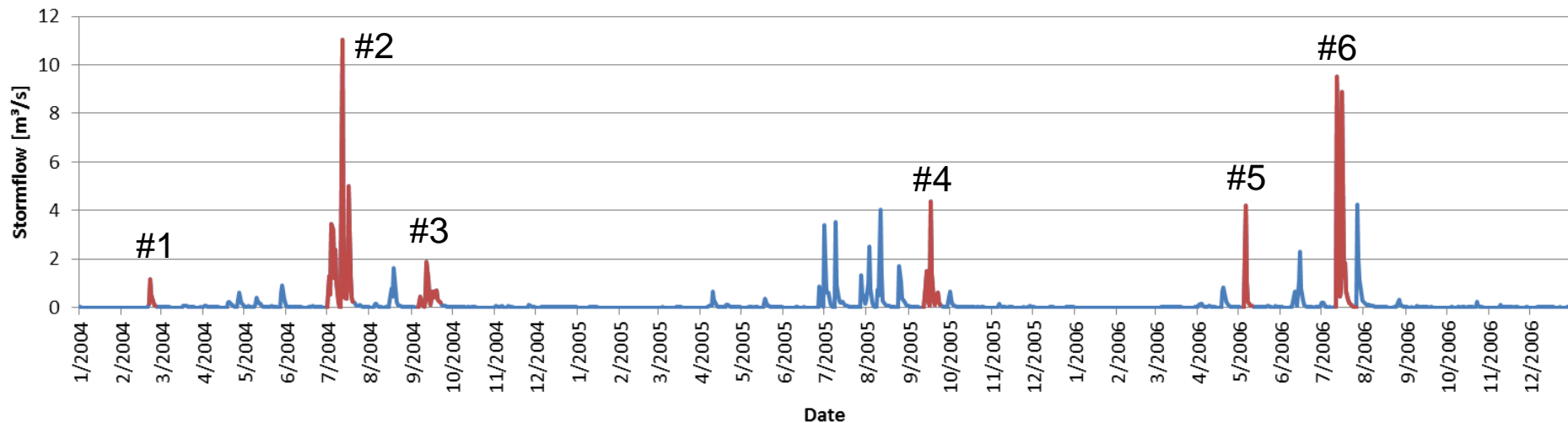


# Test of the New CN Correction Algorithm

## Teste do Novo Algoritmo de Correção da CN

- Event-based validation:  
Application of a baseflow filter (Arnold & Allen, 1999)

RMSE	Event #1	Event #2	Event #3	Event #4	Event #5	Event #6
unmodified	0.0644	0.7072	0.1411	<b>0.1491</b>	0.1432	0.7267
Williams, 1995	0.0606	0.4011	0.1755	0.1990	0.1505	0.6734
Huang et al., 2006	0.0833	0.6769	0.1978	0.1519	0.1452	0.7027
New Algorithm	<b>0.0490</b>	<b>0.3765</b>	<b>0.1184</b>	0.1511	<b>0.1082</b>	<b>0.6120</b>

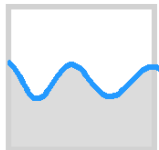


# Conclusion

## Conclusão

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- A new approach for the correction of the curve number for slopes up to 100% was developed
- The newly developed slope correction for the curve number yields solid results for a steep-sloping Korean watershed
- Additional tests of the algorithm in other mountainous catchments towards its general applicability necessary
- Further improvement and validation of the algorithm can be supported by field experiments
- The water balance on steep slopes in SWAT behaves not always plausibly
- The development of this algorithm is a step towards better representation of landscape processes in SWAT







Thank you for your  
attention!

Muito obrigado por  
sua atenção!

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+49 431 880-1238



# Literature Cited

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