

# The Uncertainty Analysis of SWAT Simulated Streamflow and Water Quality Applied to Chungju Dam Watershed of South Korea

**15 June 2011**

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# ***Purpose of this study***

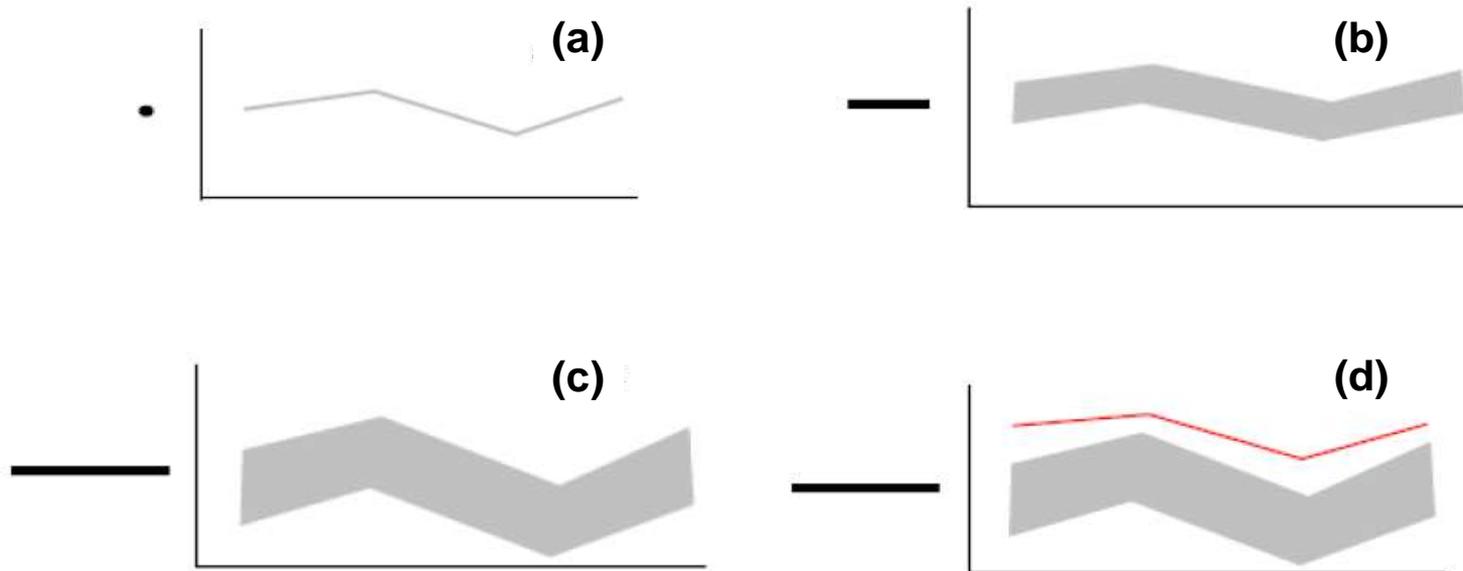
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- ✓ SWAT (Soil and Water Assessment Tool, Arnold et al., 1998) model is a very useful tool for both making decisions and research purposes of watershed management .
- ✓ To fulfill this applicability, the model should pass through a careful & well-done calibration.
- ✓ If the model is calibrated using streamflow data at the watershed outlet, can the model be called as calibrated one? What about the case of multisite calibration?
- ✓ What if we add streamflow data from stations inside the watershed? Will the new model give correct results from various parameter set in the watershed? → **Perhaps NOT** (Abbaspour et al., 2007).
- ✓ **Thus, we need to assess and understand the model uncertainty occurred by parameter set. This is possible through SWAT-CUP (Soil and Water Assessment Tool-Calibration Uncertainty Program) Modeling.**

# Prediction Uncertainty



## ◆ Parameter Uncertainty vs. Simulation Uncertainty



-  Parameter Uncertainty
-  Prediction Uncertainty
-  Measured Value

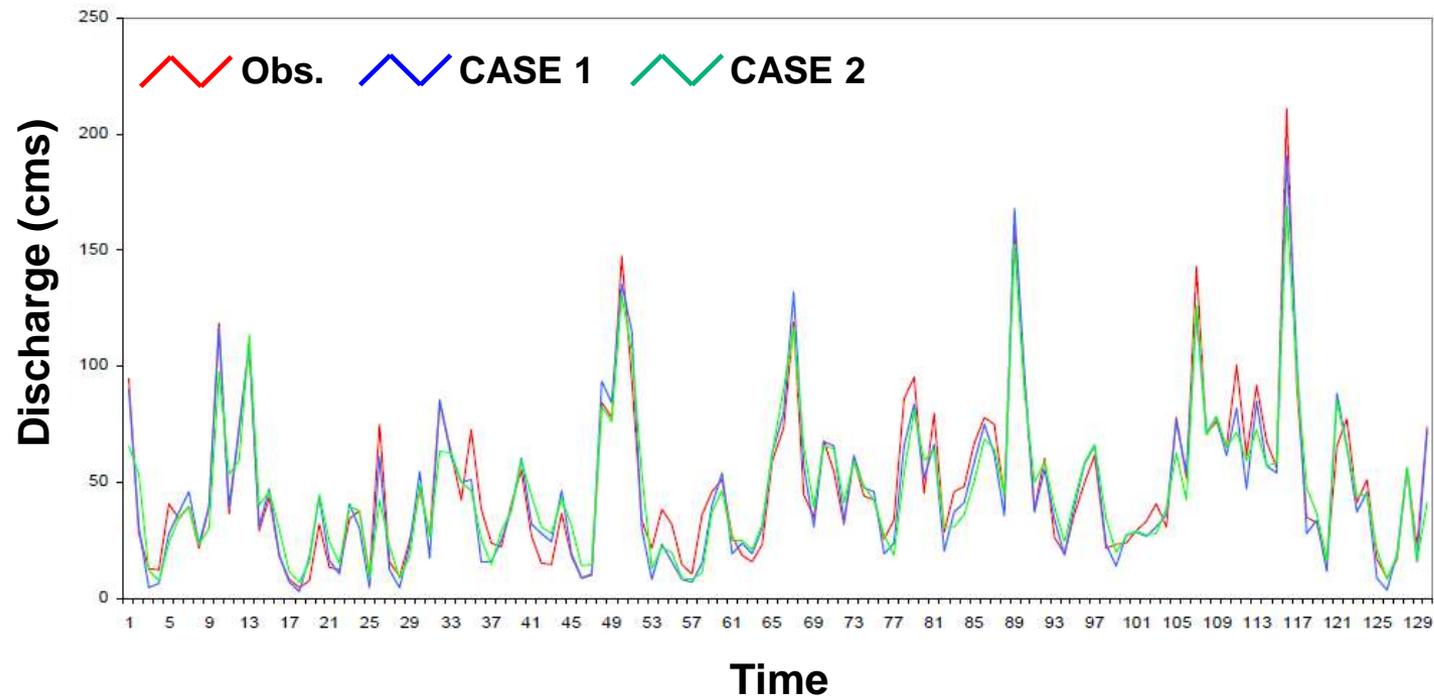
(Karim C. Abbaspour, 2009, SWAT-CUP User manual)

# Prediction Uncertainty



## ◆ Combination of Non-unique Parameter Uncertainty vs. Simulation Uncertainty

	GW_DELAY	CH_N2	CN2	REVAPMN	SOL_AWC
CASE 1	3.46	0.0098	50	0.8	0.11
CASE 2	0.34	0.131	20	2.4	0.23

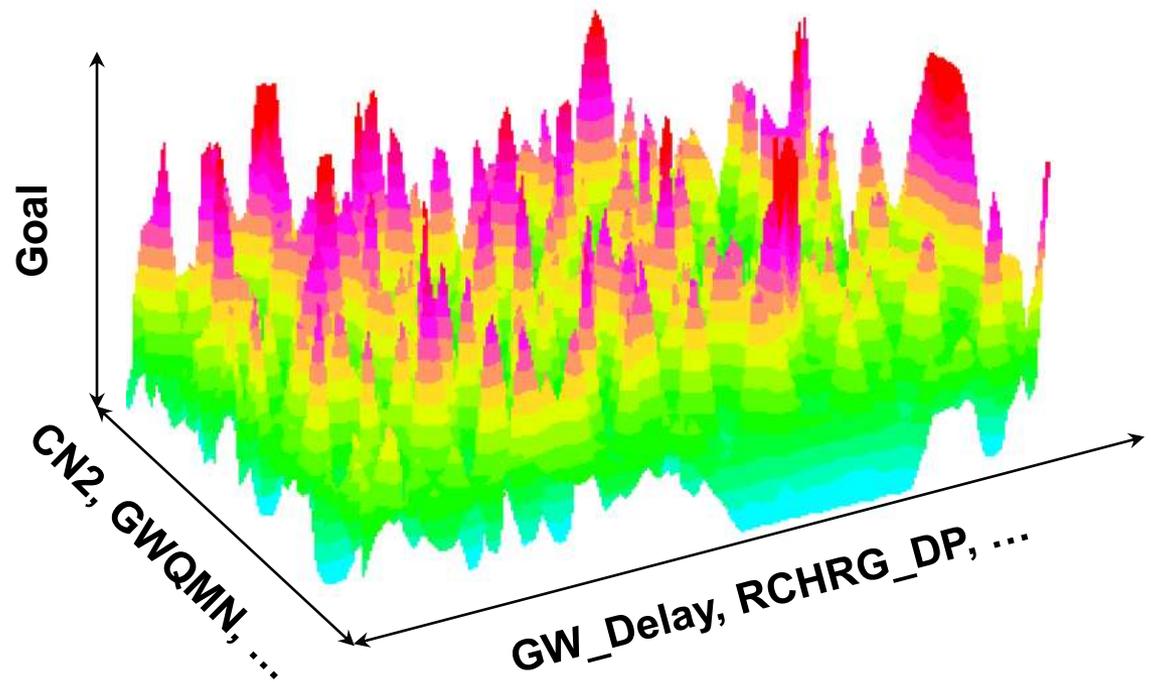
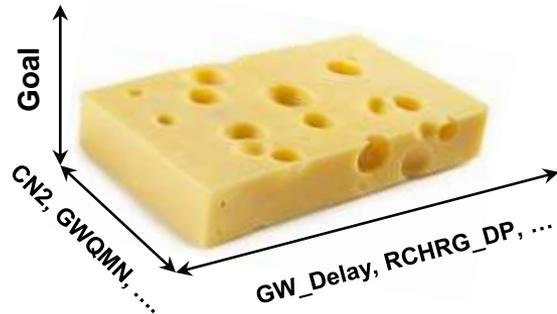


(Karim C. Abbaspour, 2009, SWAT-CUP User manual)

# Prediction Uncertainty

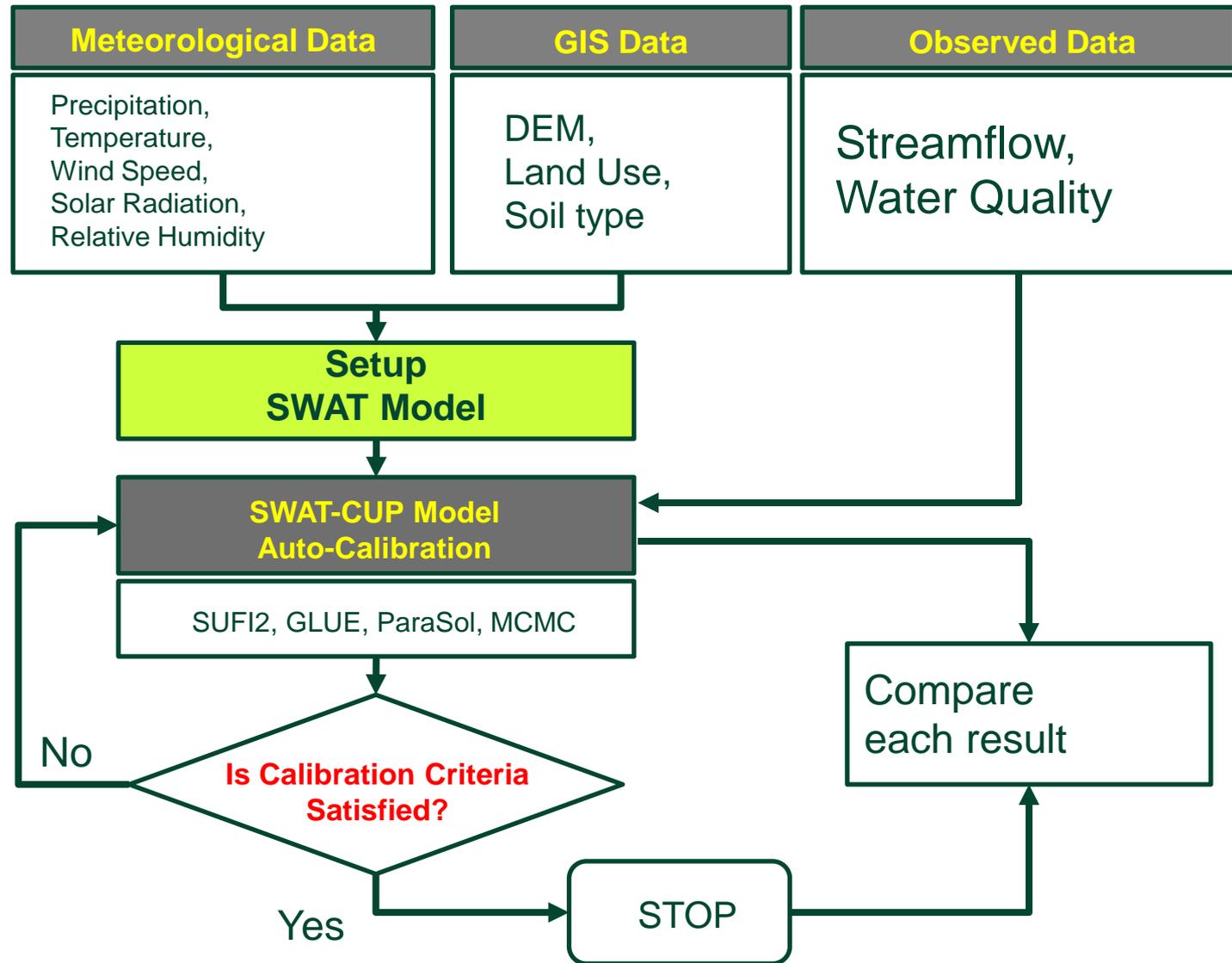


## ◆ Swiss Cheese Effect



(Karim C. Abbaspour, 2009, SWAT-CUP User manual)

# Study Procedure



# Study Area

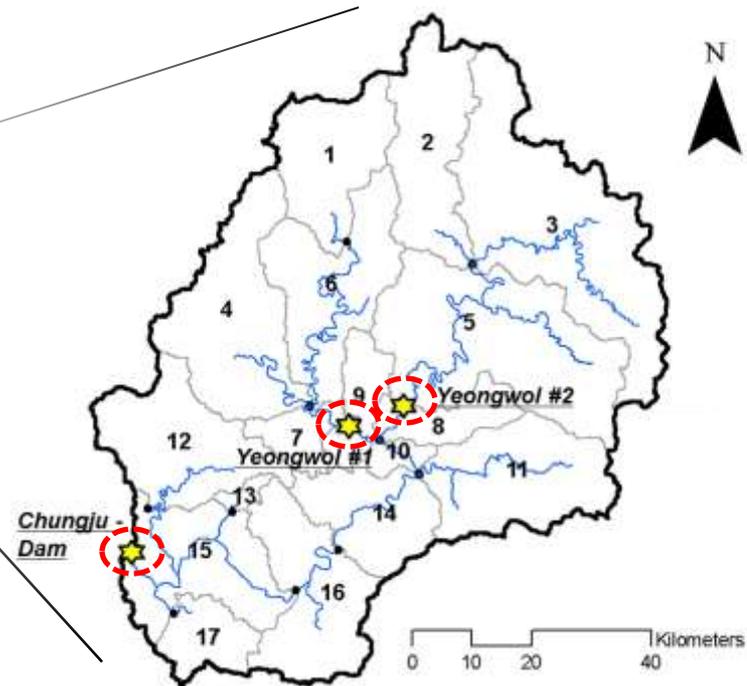


## ◆ Chungju-Dam Watershed



### Legend

-  Watershed Boundary
-  Subbasin
-  Stream
-  Calibration Points



- ✓ Watershed Area : 6,661.3 km<sup>2</sup>
- ✓ Annual Average Precipitation : 1,359.5 mm
- ✓ Forest Area : 82.2 %
- ✓ Annual Average Temperature : 9.4 °C

# Input and Measured Data



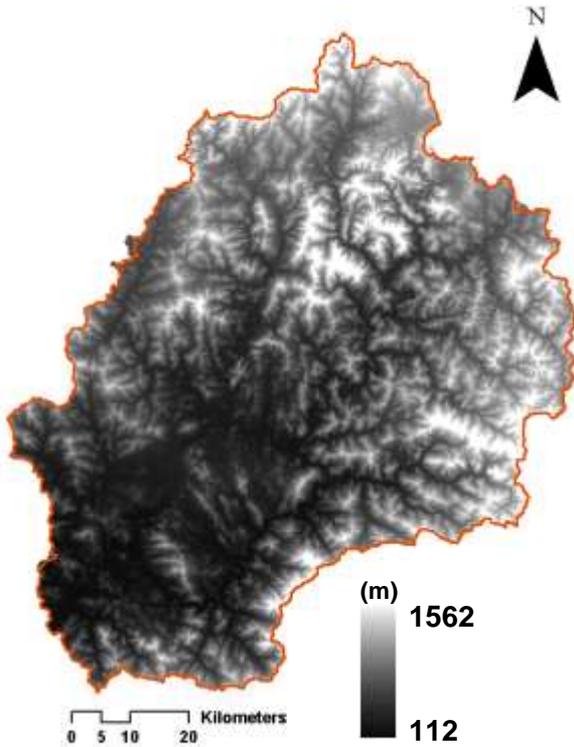
## ◆ Data Set for SWAT model

Data Type	Source	Scale / Periods	Data Description / Properties
Terrain	Korea National Geography Institute	30 m	Digital Elevation Model ( <b>DEM</b> )
Soil	Korea Rural Development Administration	1/25,000	Soil classification and physical properties viz. texture, porosity, field capacity, wilting point, saturated conductivity, and soil depth
Land use	2004 Landsat TM Satellite Image	1/25,000	Landsat land use classification
Weather	Korea Institute of Construction Technology / WAter Management Information System	1971-2009	<b>Daily</b> precipitation, minimum and maximum temperature, mean wind speed and relative humidity data

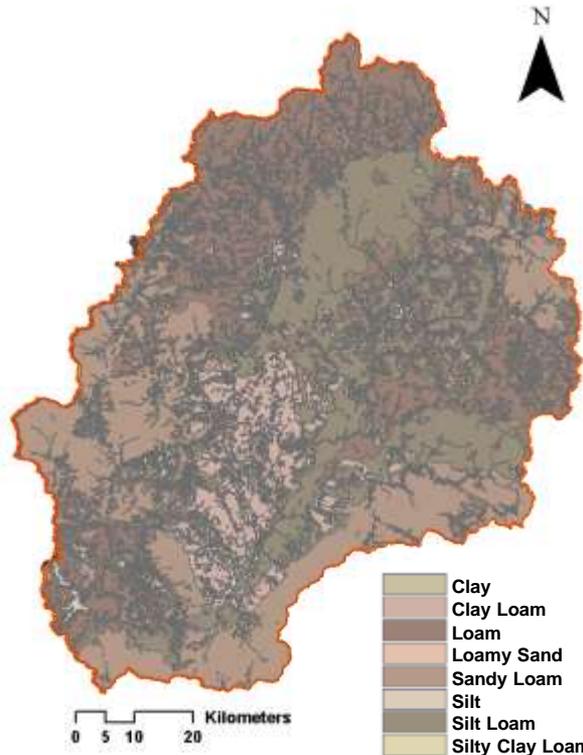
# GIS Input Data



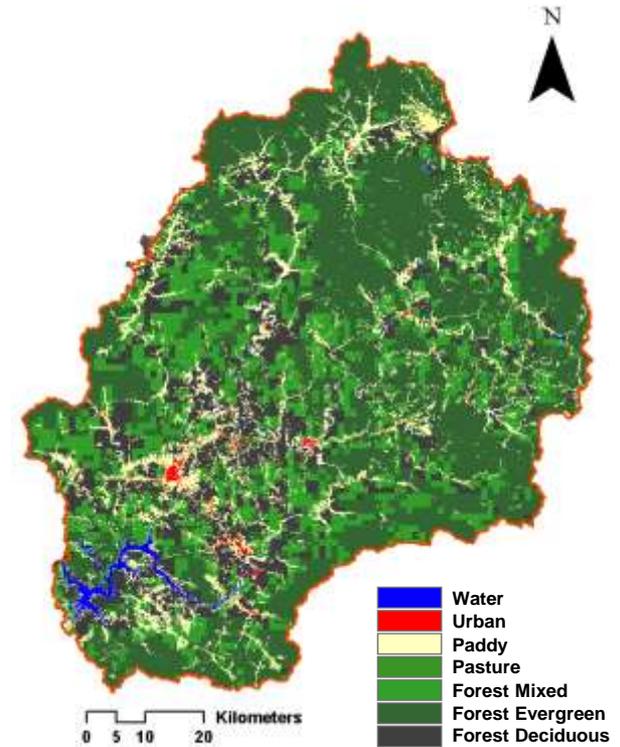
## ◆ SWAT Input Data



(a) DEM



(b) Soil



(c) Landuse

# Model theory



## ◆ SWAT (Soil and Water Assessment Tool)

✓ Water Balance Equation :

$$SW_t = SW_0 + \sum_{i=1}^t (R_{day} - Q_{surf} - E_a - w_{seep} - Q_{gw})$$

$SW_t$  = Final soil water content (mm)

$SW_0$  = Initial soil water content on day  $i$  (mm)

$R_{day}$  = Amount of precipitation on day  $i$  (mm)

$Q_{surf}$  = Amount of surface runoff on day  $i$  (mm)

$E_a$  = Amount of evapotranspiration on day  $i$  (mm)

$W_{seep}$  = Amount of water entering the vadose zone from the soil profile on day  $i$  (mm)

$Q_{gw}$  = Amount of return flow on day  $i$  (mm)

# Model theory



## ◆ SWAT-CUP (SWAT Calibration Uncertainty Program)

- ✓ Developed by **Eawag\*** Swiss Federal Institute, to analyze the prediction uncertainty of SWAT model calibration and validation results
  
- ✓ **Equipped Algorithms :**
  - a. **SUF12** (Abbaspour, et al., 2007) : **S**equential **U**ncertainty **F**itting ver.2, the parameter uncertainty accounts for all sources of uncertainties such as uncertainty in driving variables (e.g., rainfall), conceptual model, parameters, and measured data.
  
  - b. **GLUE** (Beven and Binley, 1992) : **G**eneralized **L**ikelihood **U**ncertainty **E**stimation is based on the estimation of the weights or probabilities associated with different parameter sets, based on the use of a subjective likelihood measure to derive a posterior probability function, which is subsequently used to derive the predictive probability of the output variables.

\*Eidgenössische Anstalt für Wasserversorgung, Abwasserreinigung und Gewässerschutz

# Model theory



## ◆ SWAT-CUP (SWAT Calibration Uncertainty Program)

- ✓ Developed by **Eawag\*** Swiss Federal Institute, to analyze the prediction uncertainty of SWAT model calibration and validation results
  
- ✓ **Equipped Algorithms :**
  - c. **ParaSol** (van Griensven and Meixner, 2006) : **Parameter Solution** method aggregates objective functions (OF) into a global optimization criterion (GOC) and then minimizes these OF's or a GOC using the SCE-UA (Shuffled Complex Evolution, Duan, et al., 1992) algorithm.
  
  - d. **MCMC** : **Markov Chain Monte Carlo** generates samples from a random walk which adapts to the posterior distribution (Kuczera and Parent, 1998). This simple techniques from this class is the Metropolis Hasting algorithm (Gelman et al. 1995), which is not applied in this study.

\*Eidgenössische Anstalt für Wasserversorgung, Abwasserreinigung und Gewässerschutz

# Model theory



## ◆ SWAT-CUP (SWAT Calibration Uncertainty Program)

### ✓ Remarkable Words :

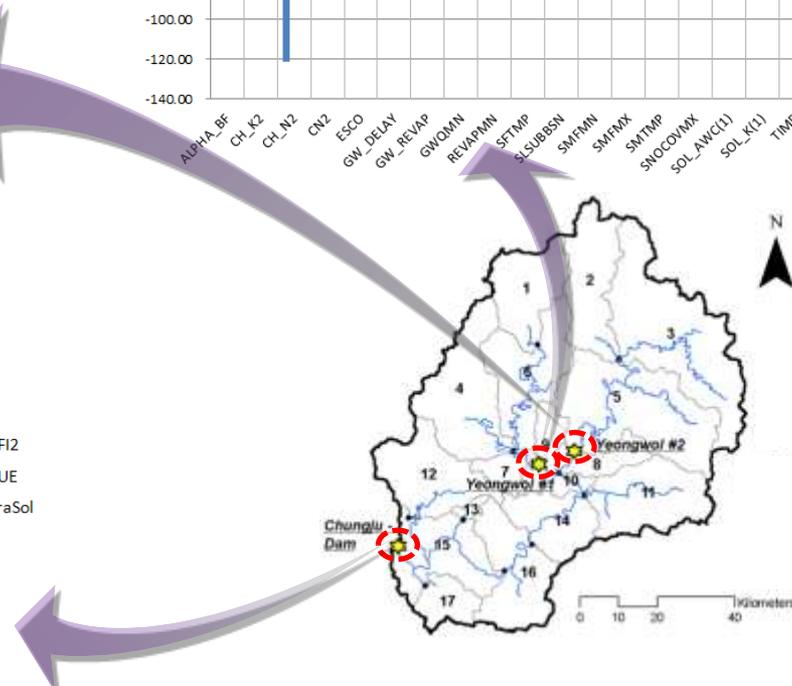
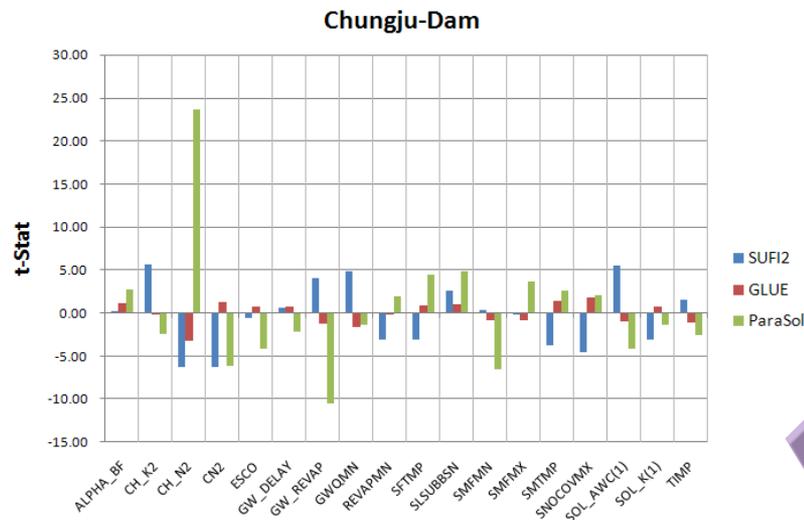
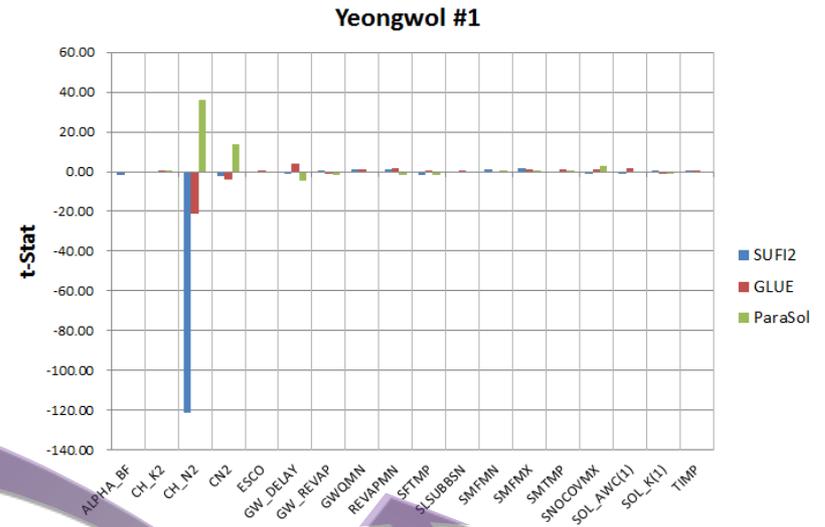
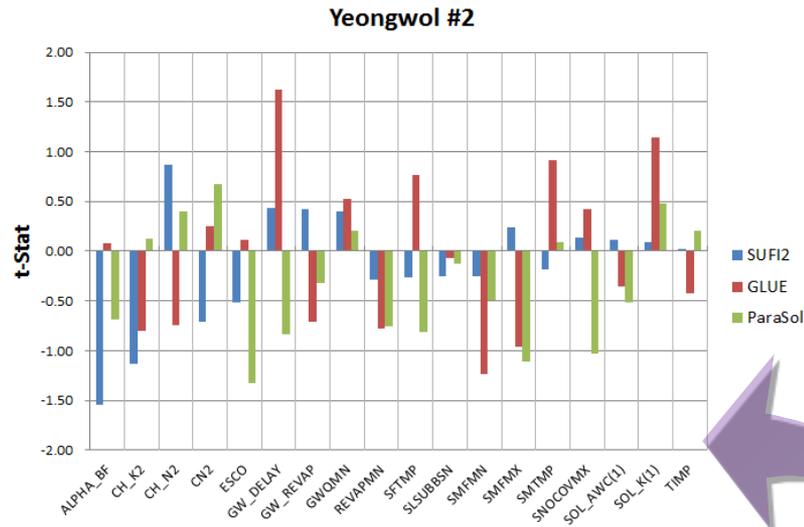
- a. **95PPU** : **95 Percent Prediction Uncertainty**, This value is calculated at the 2.5% and 97.5% levels of an output variable, disallowing 5% of the very bad simulations.
- b. **Objective Function** : Coefficient of determination ( $R^2$ ), Nash-Sutcliffe (1970) coefficient... Etc.
- c. **p-factor** : The percentage of observations covered by the 95PPU.
- d. **r-factor** : Relative width of 95% probability band.
- e. **t-Stat** : Provides a measure of sensitivity, larger absolute values are more sensitive.
- f. **P-Value** : Determined the significance of the sensitivity. A values close to zero has more significance.

- A P-factor of 1 and R-factor of zero is a simulation that exactly corresponds to measured data. (Karim C. Abbaspour, 2009, SWAT-CUP User maunal)

# Sensitivity Analysis (SA)



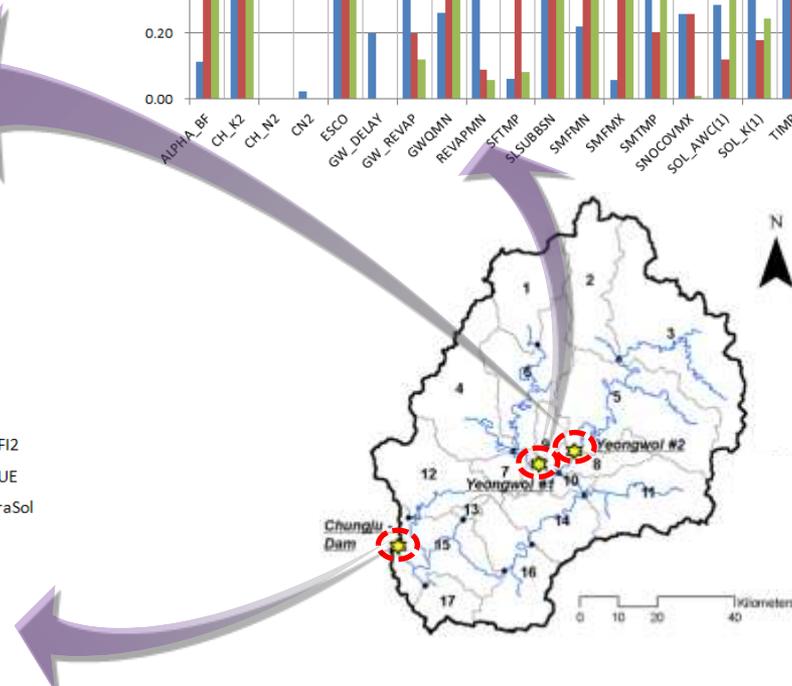
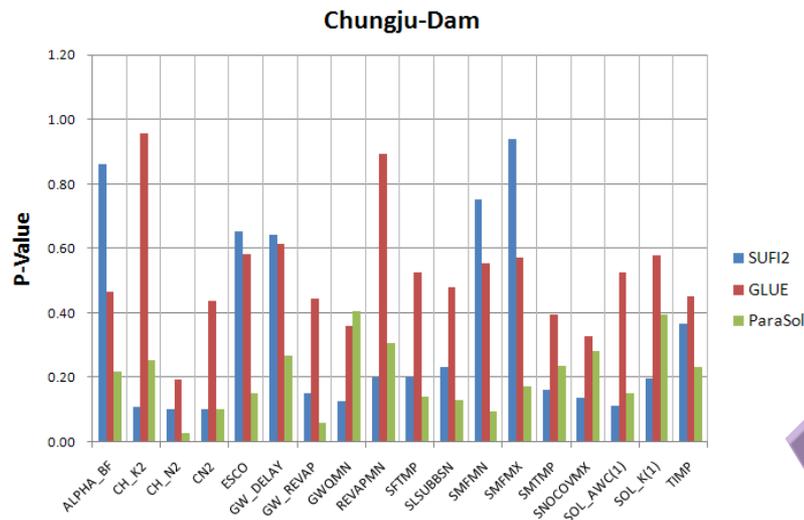
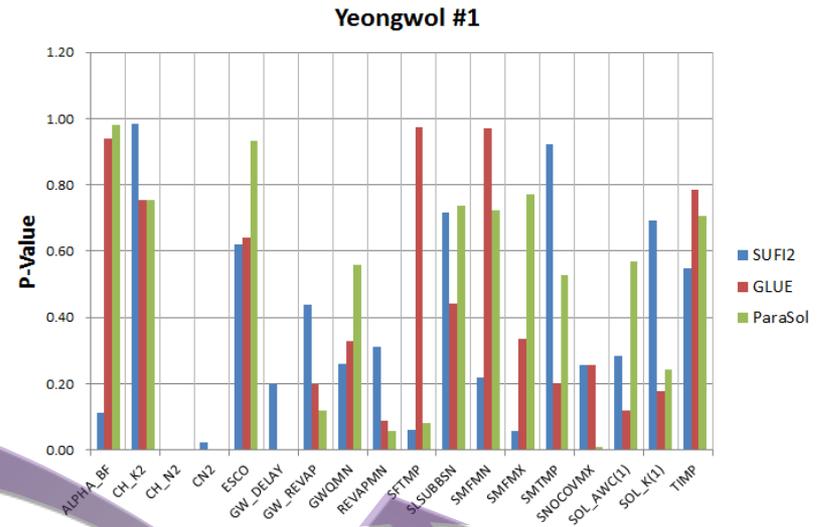
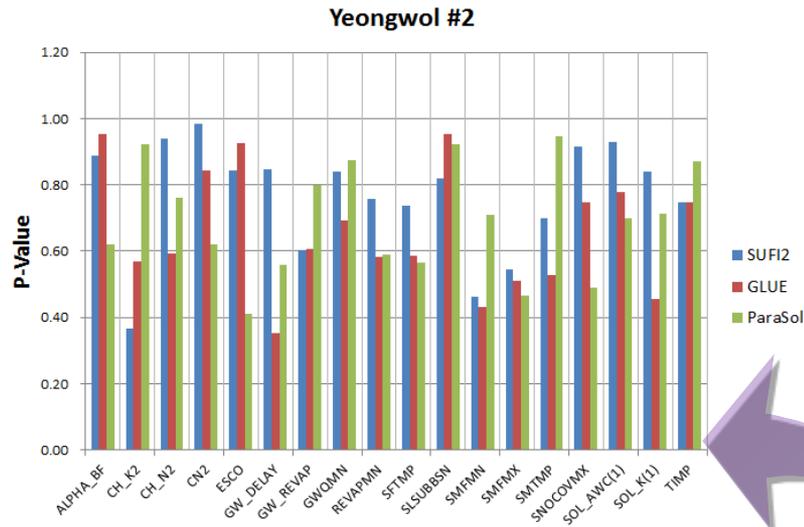
## ◆ t-Stat



# Sensitivity Analysis (SA)



## ◆ P-Value

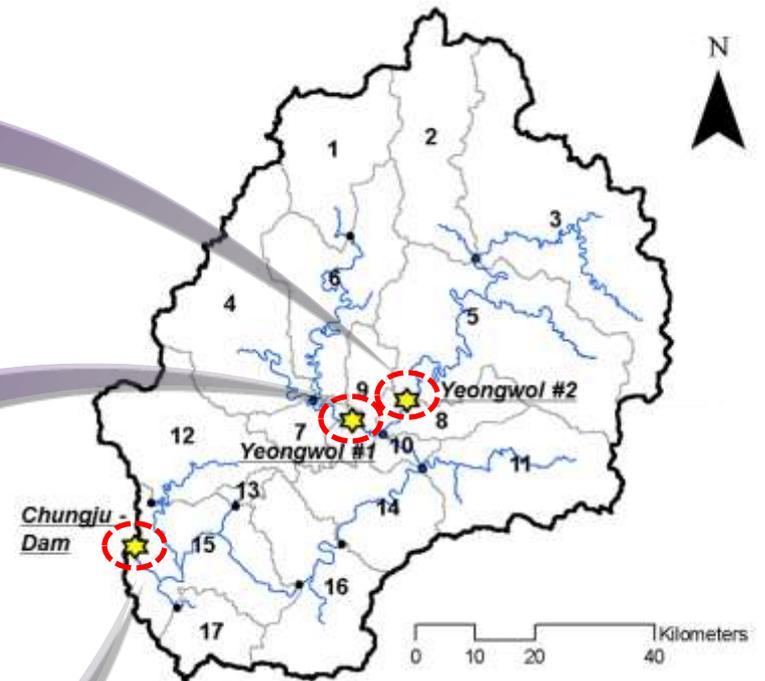
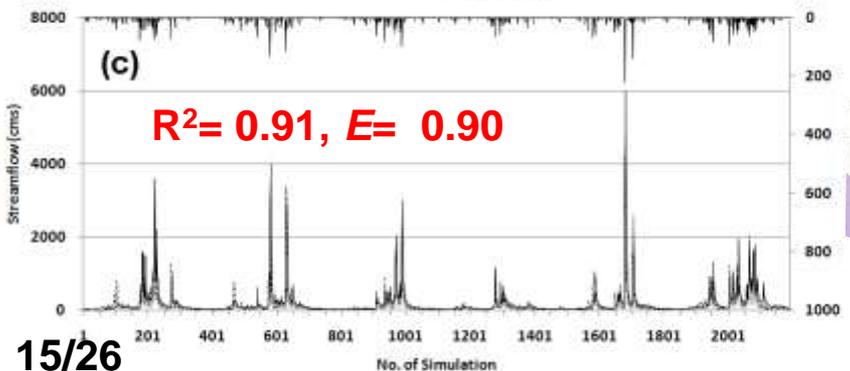
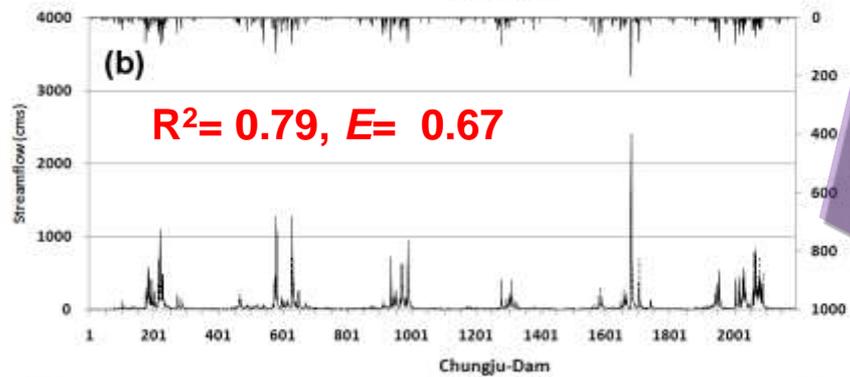
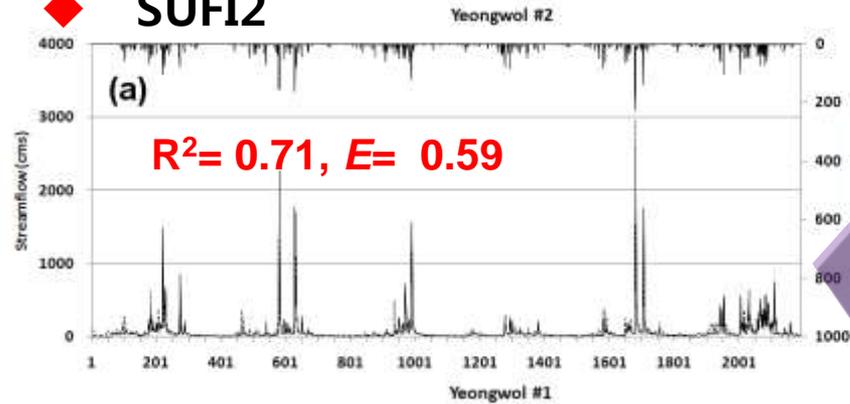


# Calibration and Validation



## ◆ SUFI2

$R^2$  : Determination Coefficient  
E : Model Efficiency

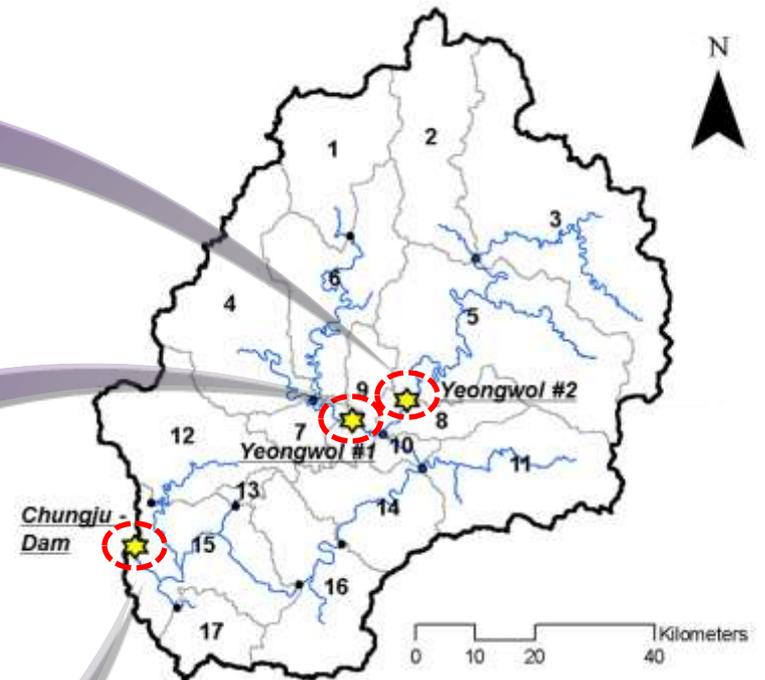
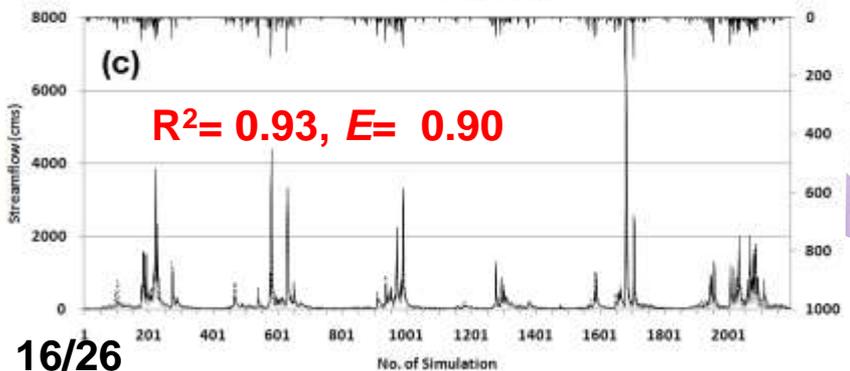
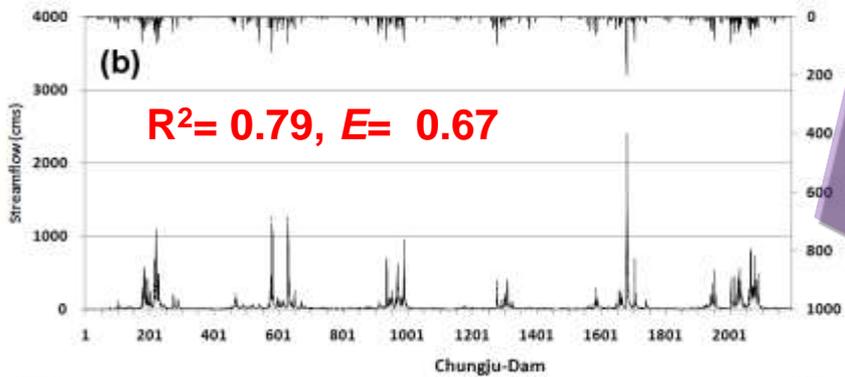
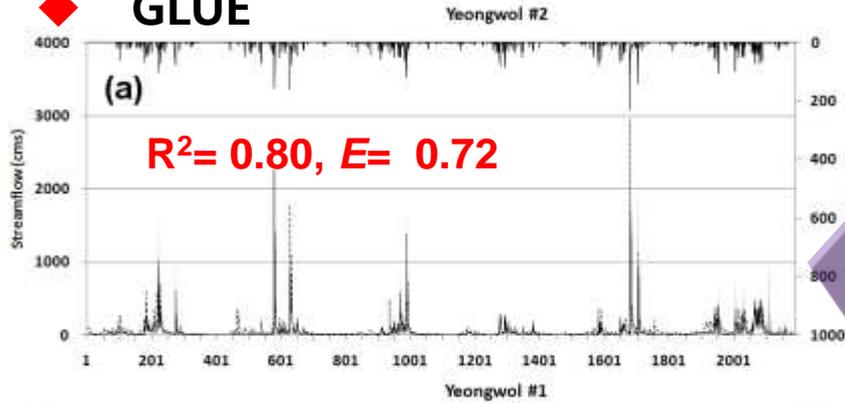


# Calibration and Validation



## ◆ GLUE

$R^2$  : Determination Coefficient  
E : Model Efficiency

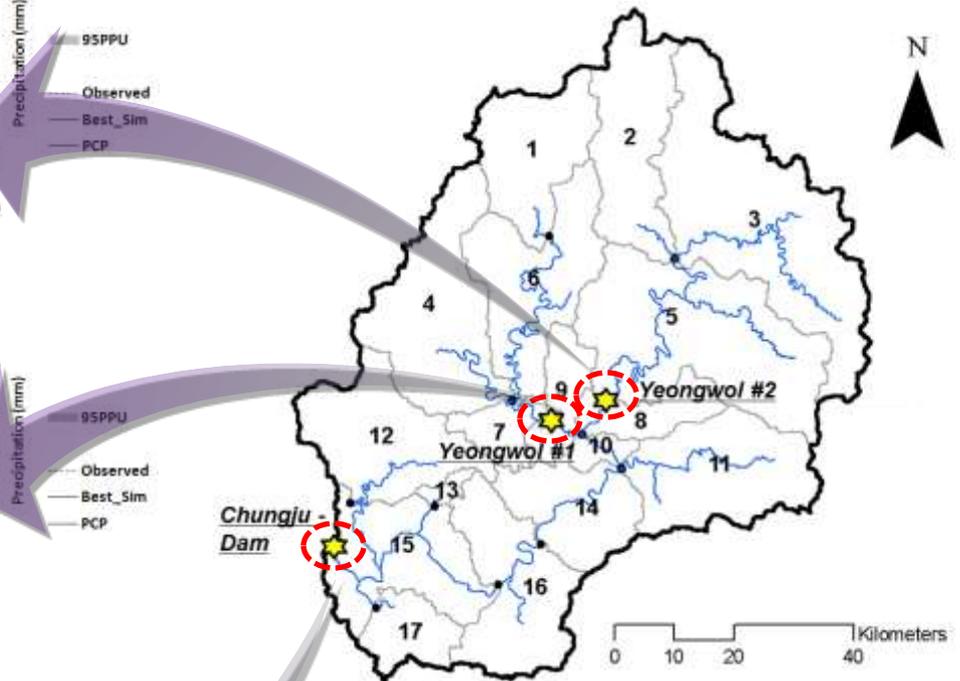
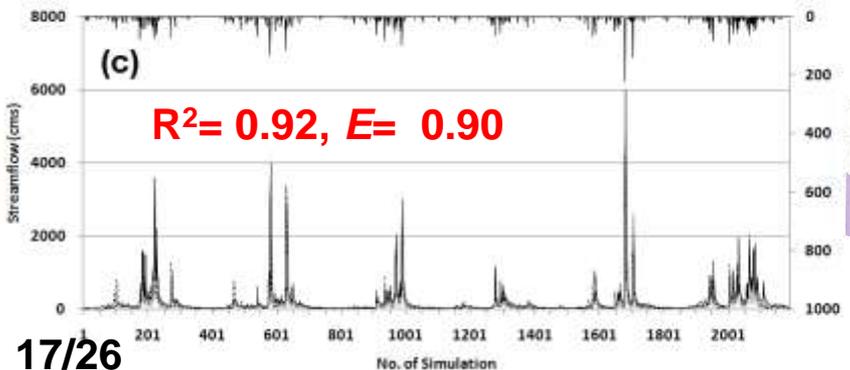
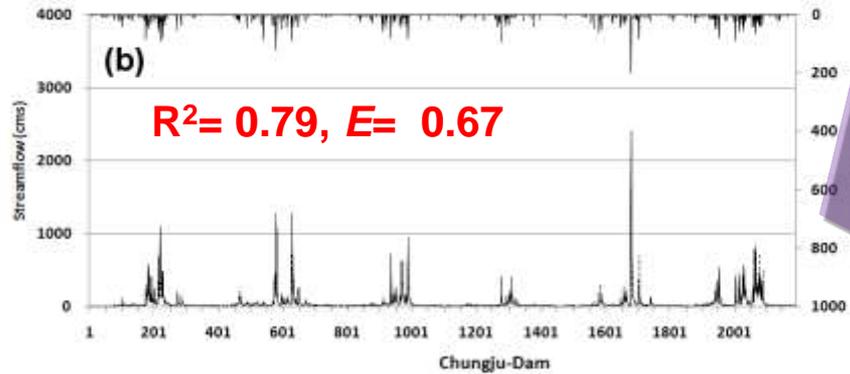
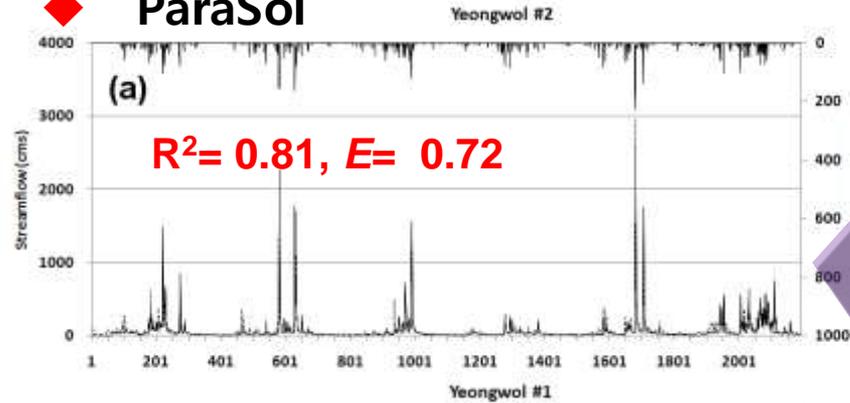


# Calibration and Validation



## ◆ ParaSol

$R^2$  : Determination Coefficient  
E : Model Efficiency

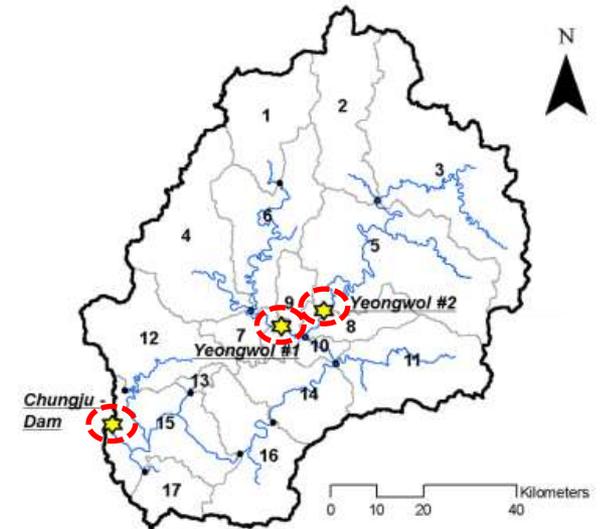


# Calibration and Validation



## ◆ Objective Function and 95PPUs for streamflow

Subbasin	$R^2$			E		
	No. 5	No. 7	No. 15	No. 5	No. 7	No. 15
SUFI2	0.71	0.79	0.91	0.59	0.67	0.90
GLUE	0.80	0.79	0.93	0.72	0.67	0.90
ParaSol	0.81	0.79	0.92	0.72	0.67	0.90



Subbasin	p-factor			r-factor		
	No. 5	No. 7	No. 15	No. 5	No. 7	No. 15
SUFI2	0.33	0.66	0.79	0.30	0.38	0.52
GLUE	0.26	0.56	0.44	0.30		
ParaSol	0.02	0.14	0.07	0.03	0.03	0.05

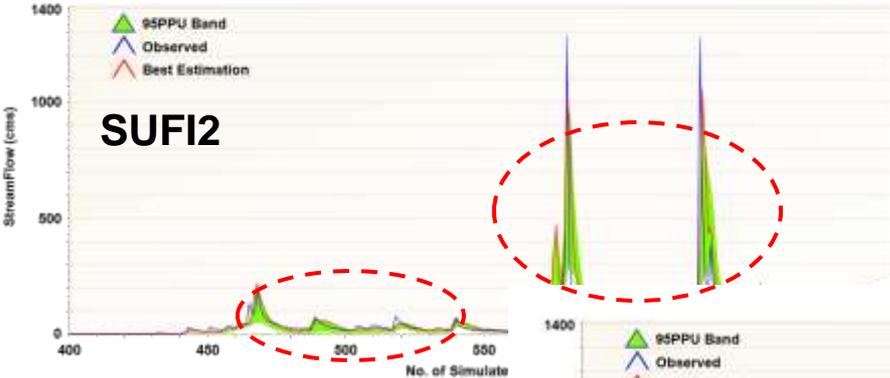
**SUFI2 was the Best**

# Calibration and Validation



## ◆ Comparing Each Result in Random Section

Sub\_basin No.7



The 95PPU bands (model uncertainty): green color range were caused by the variable parameter set range.

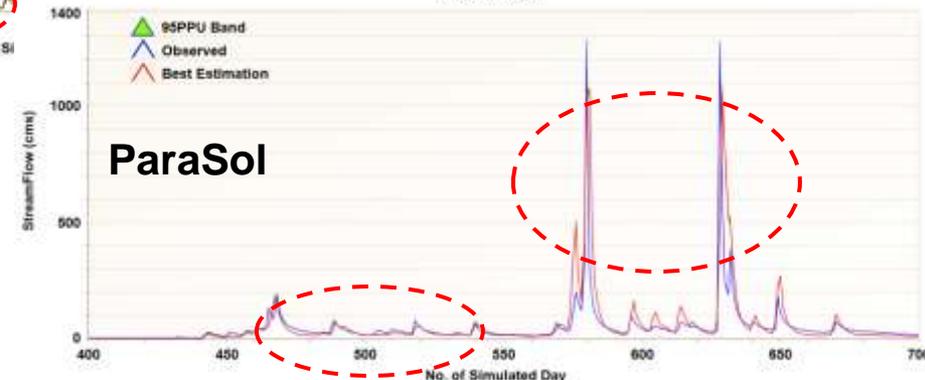
Sensitive and well distributed ↑

Sub\_basin No.7



The SUFI2 was the most suitable way to find the SWAT Uncertainty under the condition that the parameter range was specified. → Responded to parameter set more sensitive than any others.

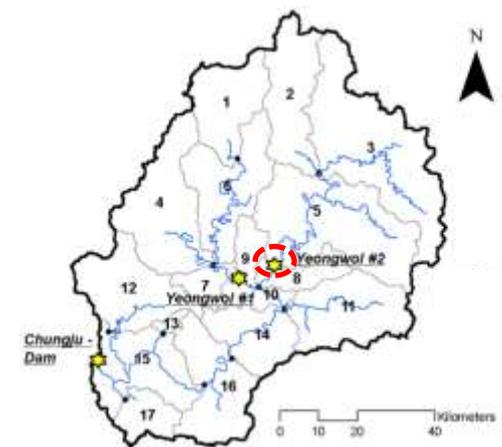
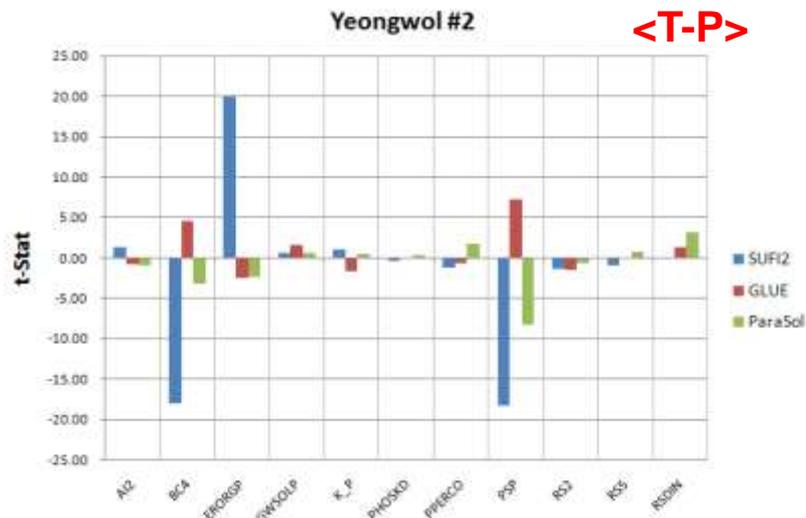
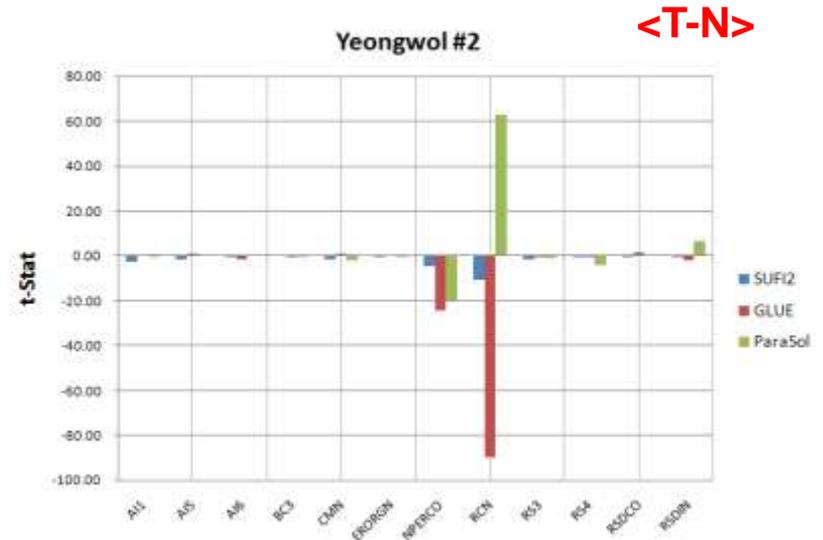
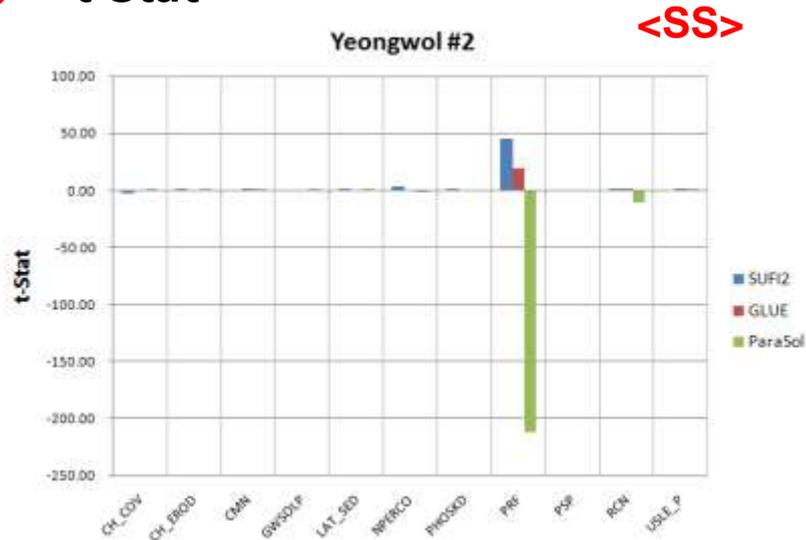
Sub\_basin No.7



# Sensitivity Analysis (SA)



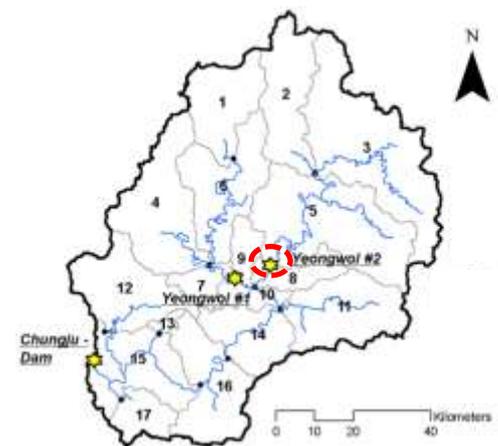
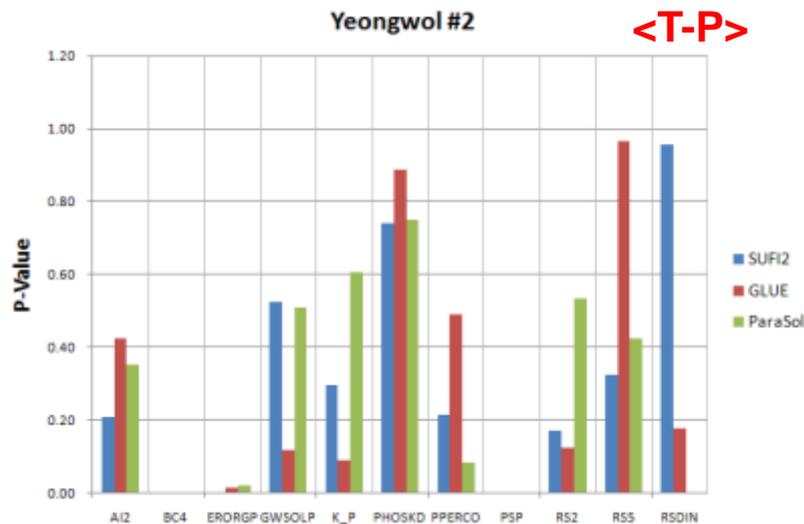
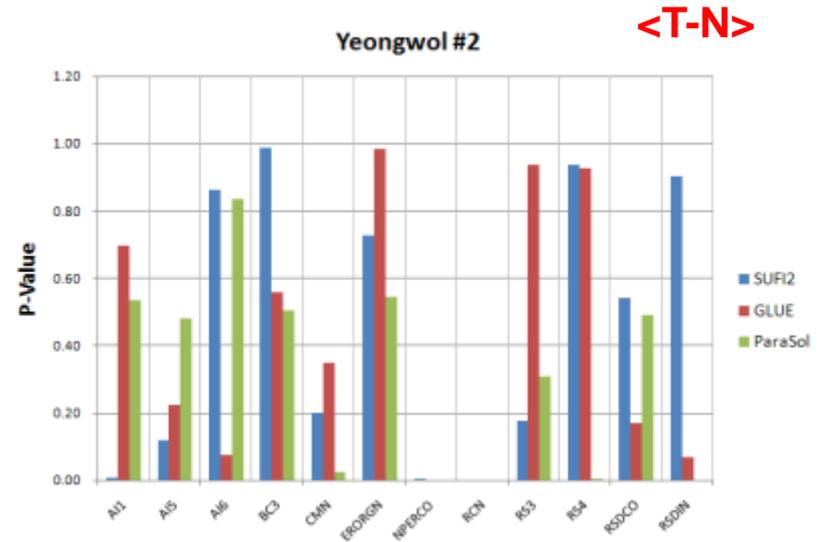
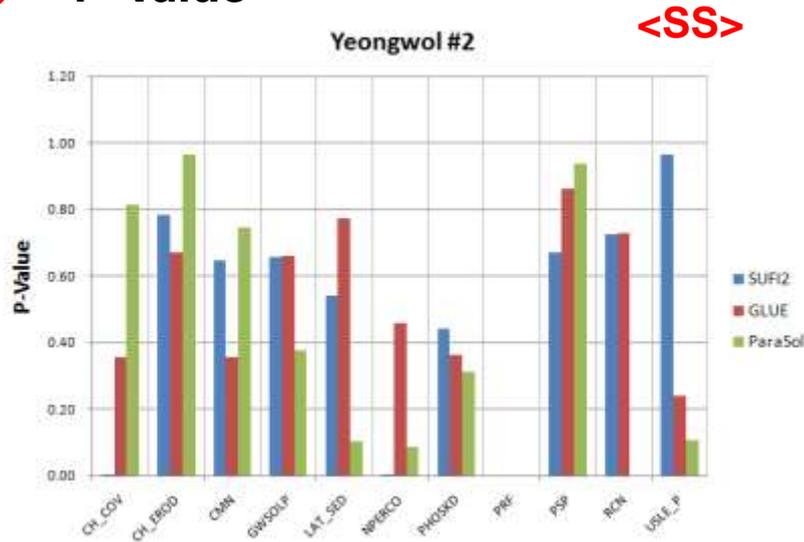
## ◆ t-Stat



# Sensitivity Analysis (SA)



## ◆ P-Value



# Calibration and Validation

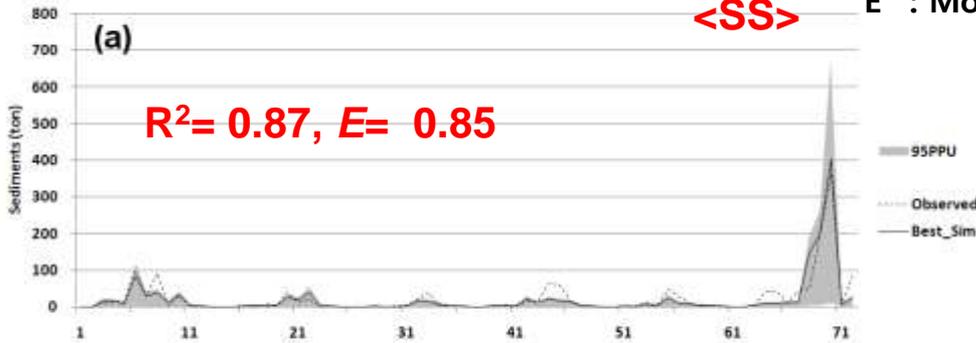


## ◆ SUFI2

$R^2$  : Determination Coefficient  
E : Model Efficiency

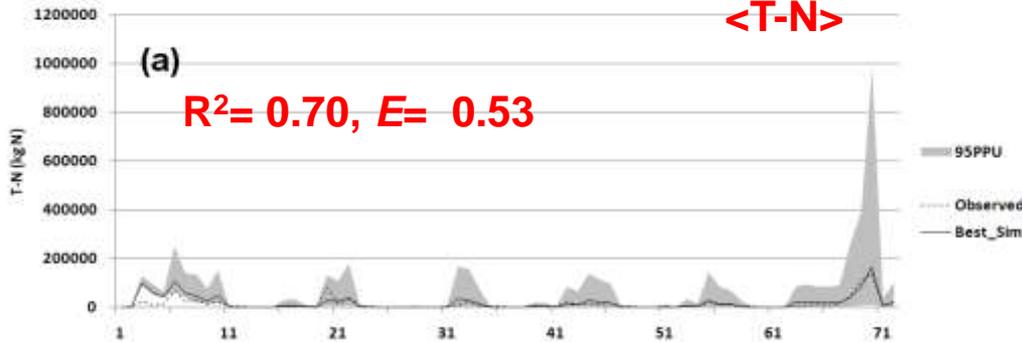
Yeongwol #2

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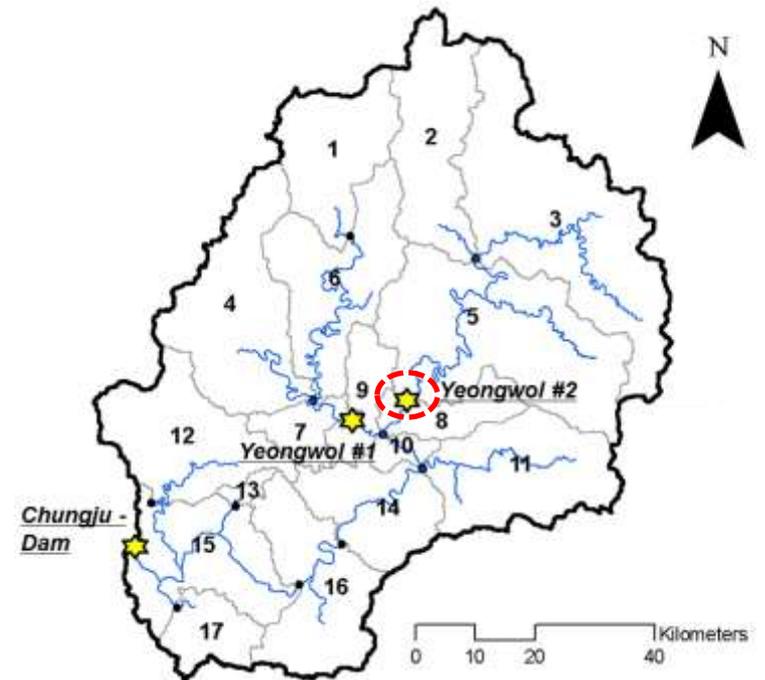
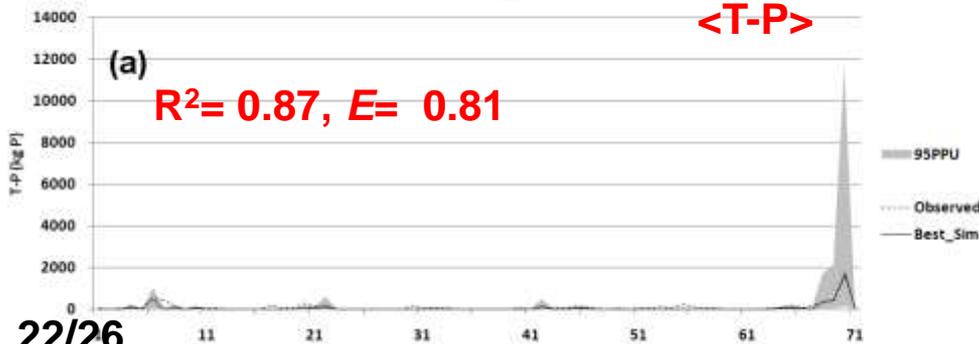
Yeongwol #2

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Yeongwol #2

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# Calibration and Validation

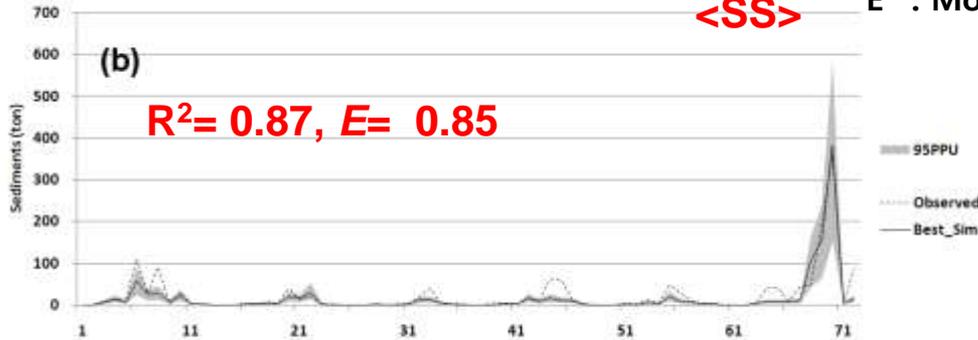


## ◆ GLUE

$R^2$  : Determination Coefficient  
E : Model Efficiency

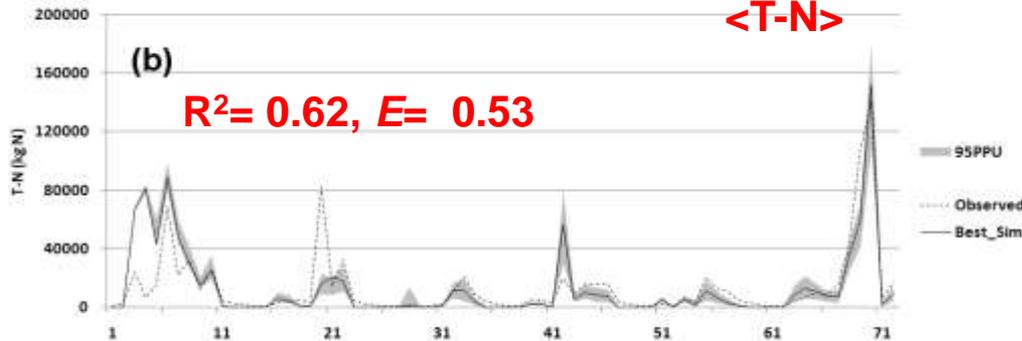
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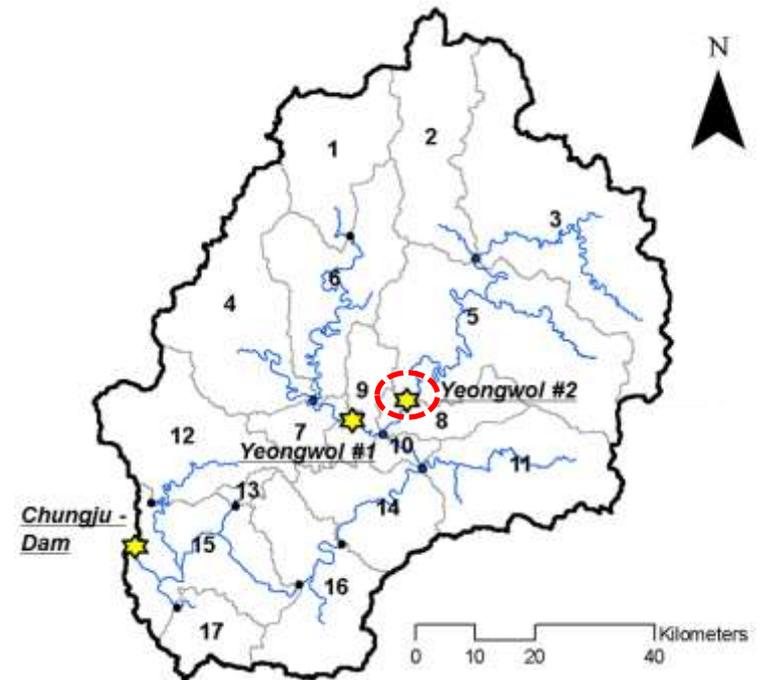
Yeongwol #2

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# Calibration and Validation



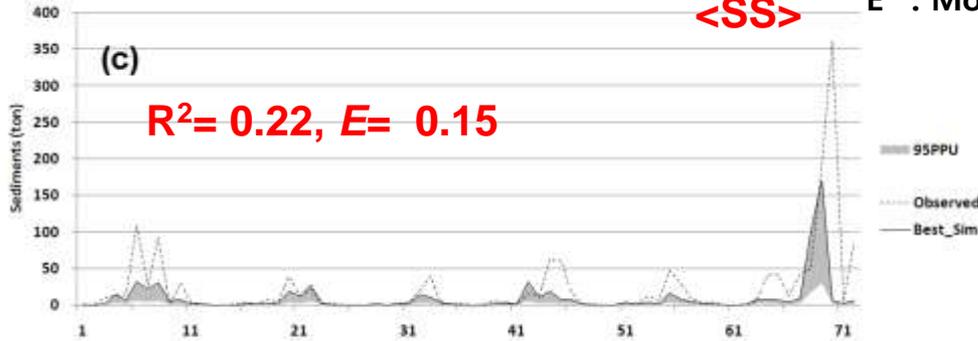
## ◆ ParaSol

Yeongwol #2

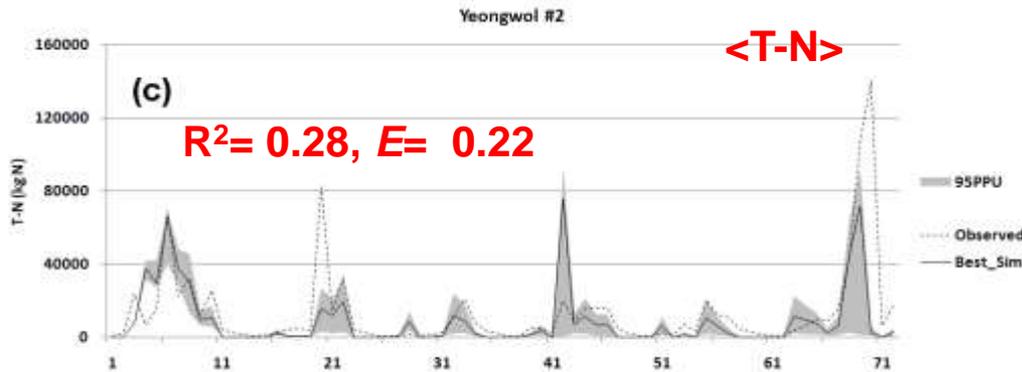
$R^2$  : Determination Coefficient

E : Model Efficiency

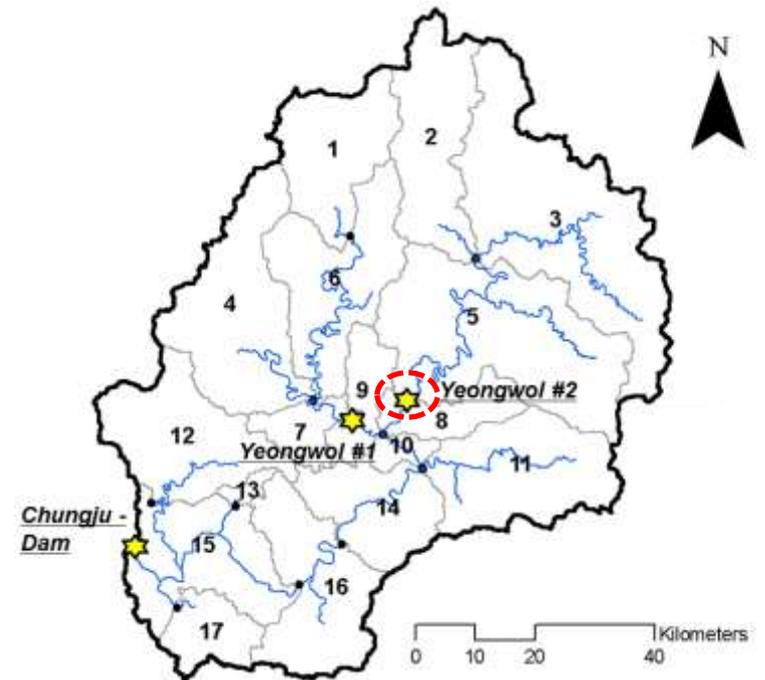
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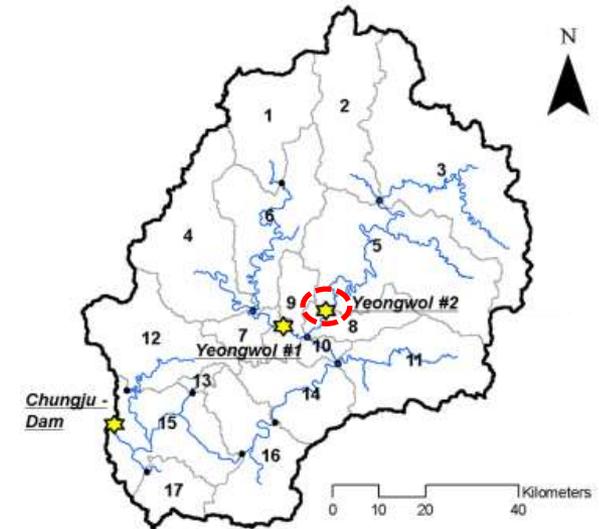


# Calibration and Validation



## ◆ Objective Function and 95PPUs for Water Quality

	<b>R<sup>2</sup></b>			<b>E</b>		
	SS	T-N	T-P	SS	T-N	T-P
SUFI2	0.87	0.70	0.87	0.85	0.53	0.81
GLUE	0.87	0.62	0.87	0.85	0.53	0.82
ParaSol	0.22	0.28	0.06	0.15	0.22	-0.09



	<b>p-factor</b>			<b>r-factor</b>		
	SS	T-N	T-P	SS	T-N	T-P
SUFI2	0.67	0.54	0.23	0.53	2.73	1.30
GLUE	0.40	0.17	0.10	0.35		
ParaSol	0.19	0.22	0.07	0.15	0.22	0.15

**SUFI2 was the Best**

# Summary and Conclusion



- ✓ This study tried to evaluate the prediction uncertainty of SWAT model for streamflow and water quality.
  - As a result, there was no significant difference in the  $R^2$ , Nash-Sutcliffe coefficient (NSE) values for each procedure.
  - However, the p-factor and r-factor indicated that the numerical 95PPUs bands showed clear distinction in this analysis. In this study, ParaSol algorithm showed the lowest p-factor and r-factor, while SUFI-2 algorithm was the highest in the p-factor and r-factor.
  - The SUFI2 algorithm showed the most sensitive and evenly distributed 95PPUs bands for streamflow and water quality.
  - **With the SUFI2 algorithm, we could assess the most sensitive results and reduce model uncertainty effectively.**
  - **This study gave us an obvious information that the evaluation of model uncertainty caused by SWAT hydrologic modeling could be predictable and quantified by SWAT-CUP.**

This work was supported by Mid-career Researcher Program through NRF grant funded by the MEST (No. 2009-0080745).

# “ Thank You ”

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Soil & Water  
Assessment Tool

**SWAT**



Dept. of Civil and Environmental System Eng.,  
Konkuk University, Seoul, South Korea