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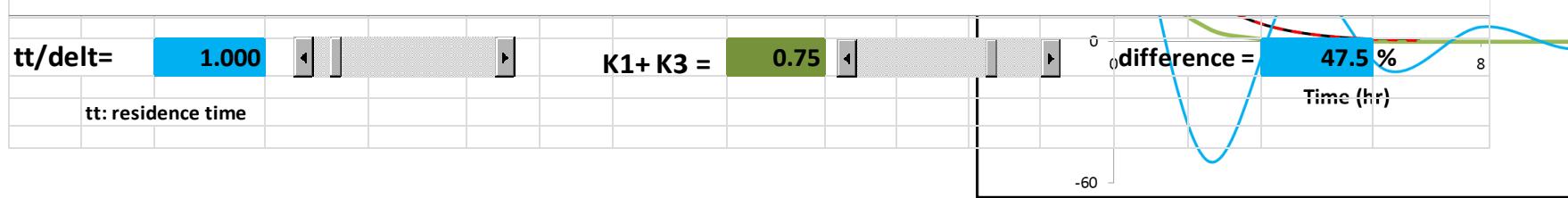
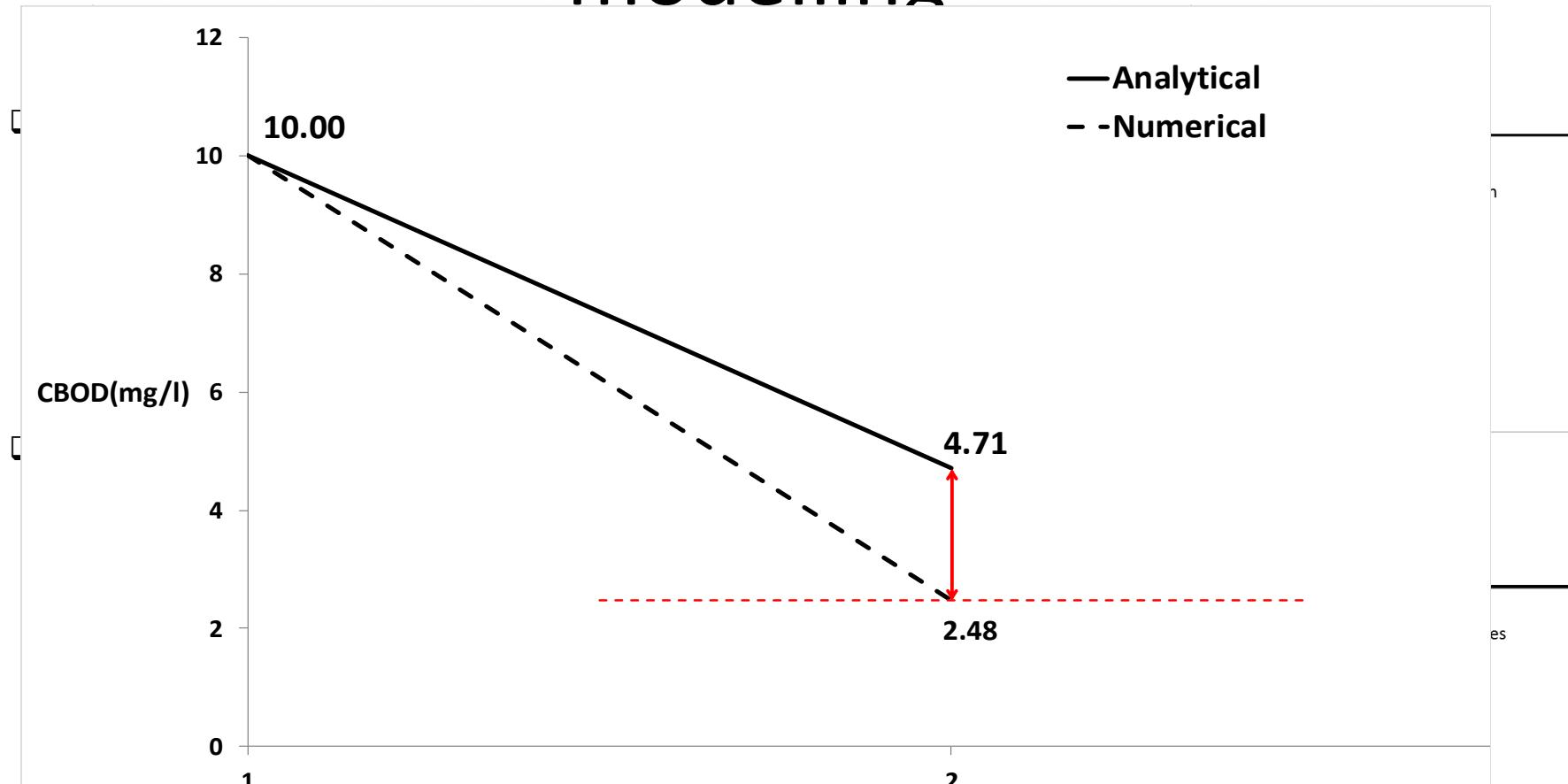
IMPROVED SOLUTION METHODS FOR INSTREAM WATER QUALITY SIMULATIONS IN SWAT

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SWAT for instream water quality modelling

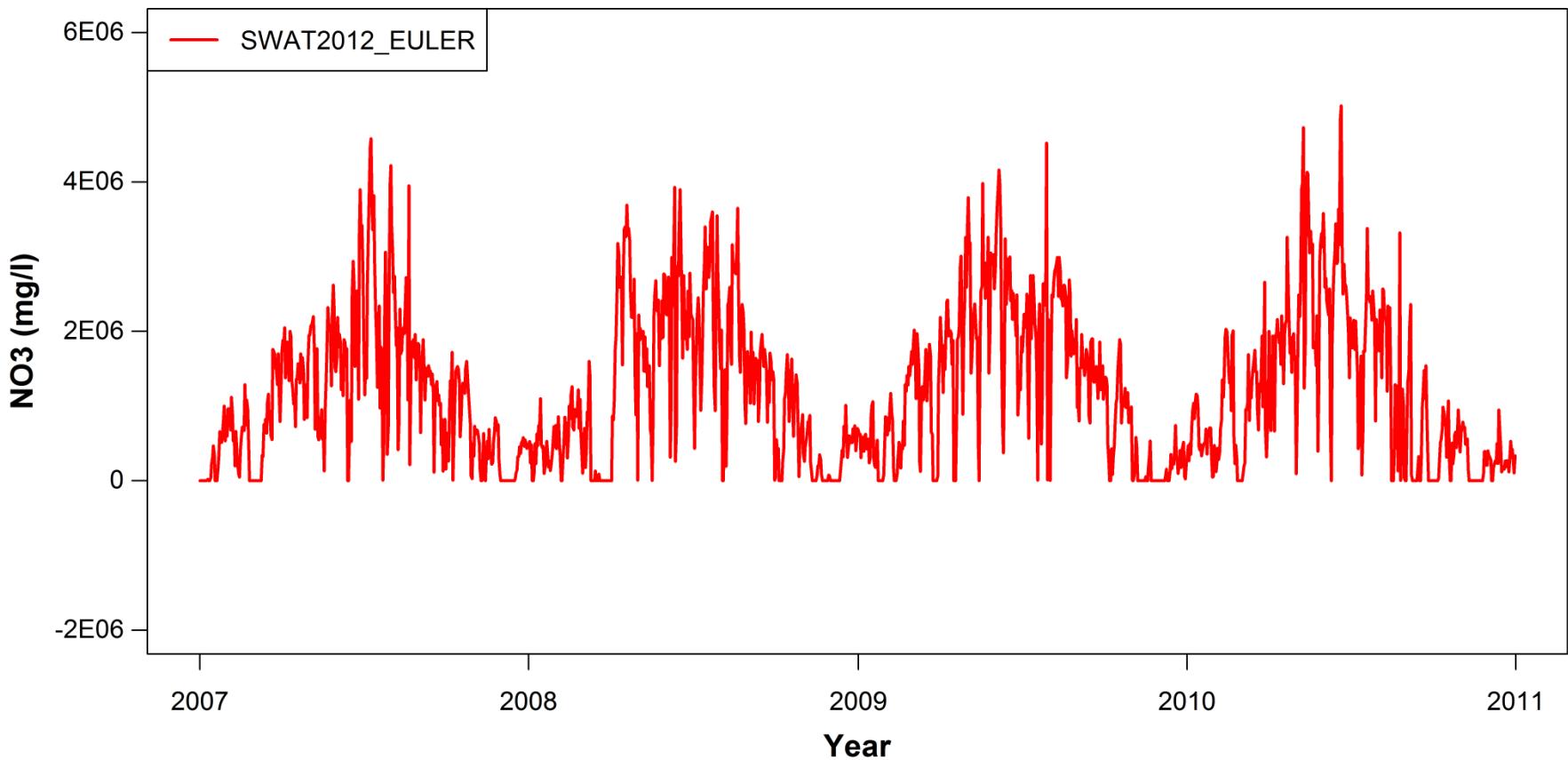


Outline

- Instabilities in SWAT2012 WQ module
- Improved quasi-analytical solution method for instream WQ simulation of SWAT
- Results from case study (Zenne River, Belgium)

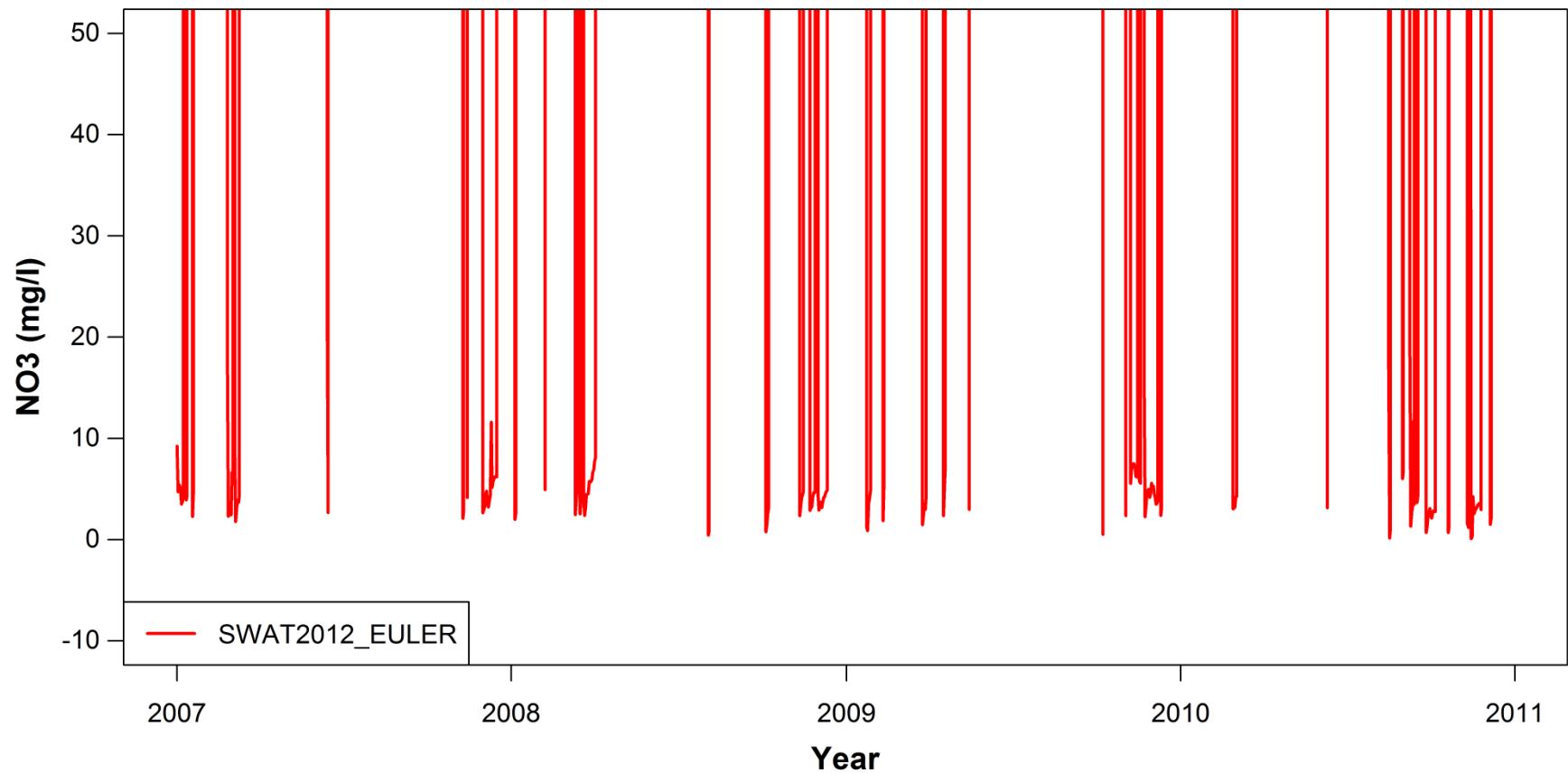
Instabilities/inaccuracy of Euler approach in SWAT WQ module

- Default parameters



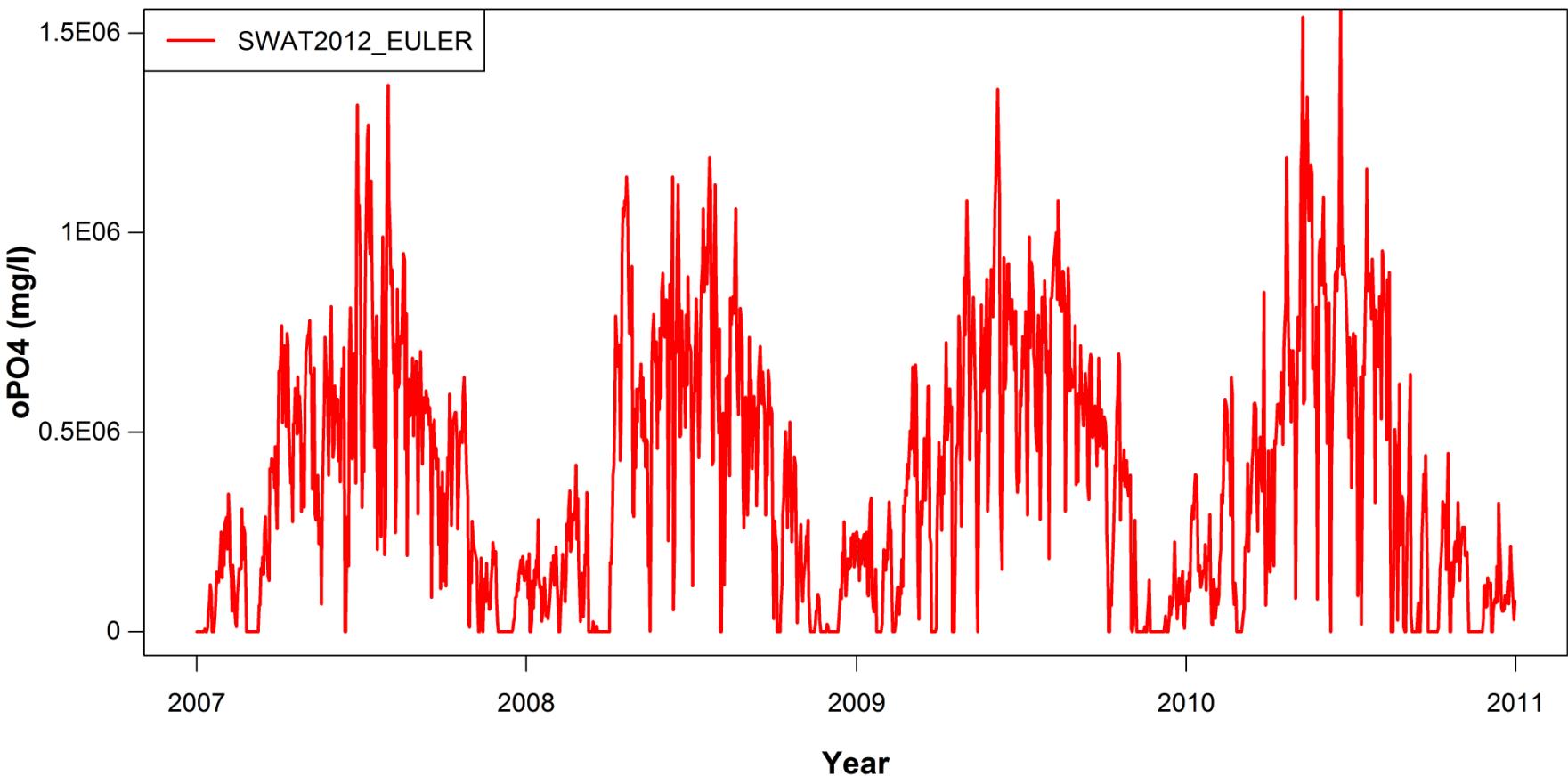
Instabilities/inaccuracy of Euler approach in SWAT WQ module

- Default parameters-zoomed



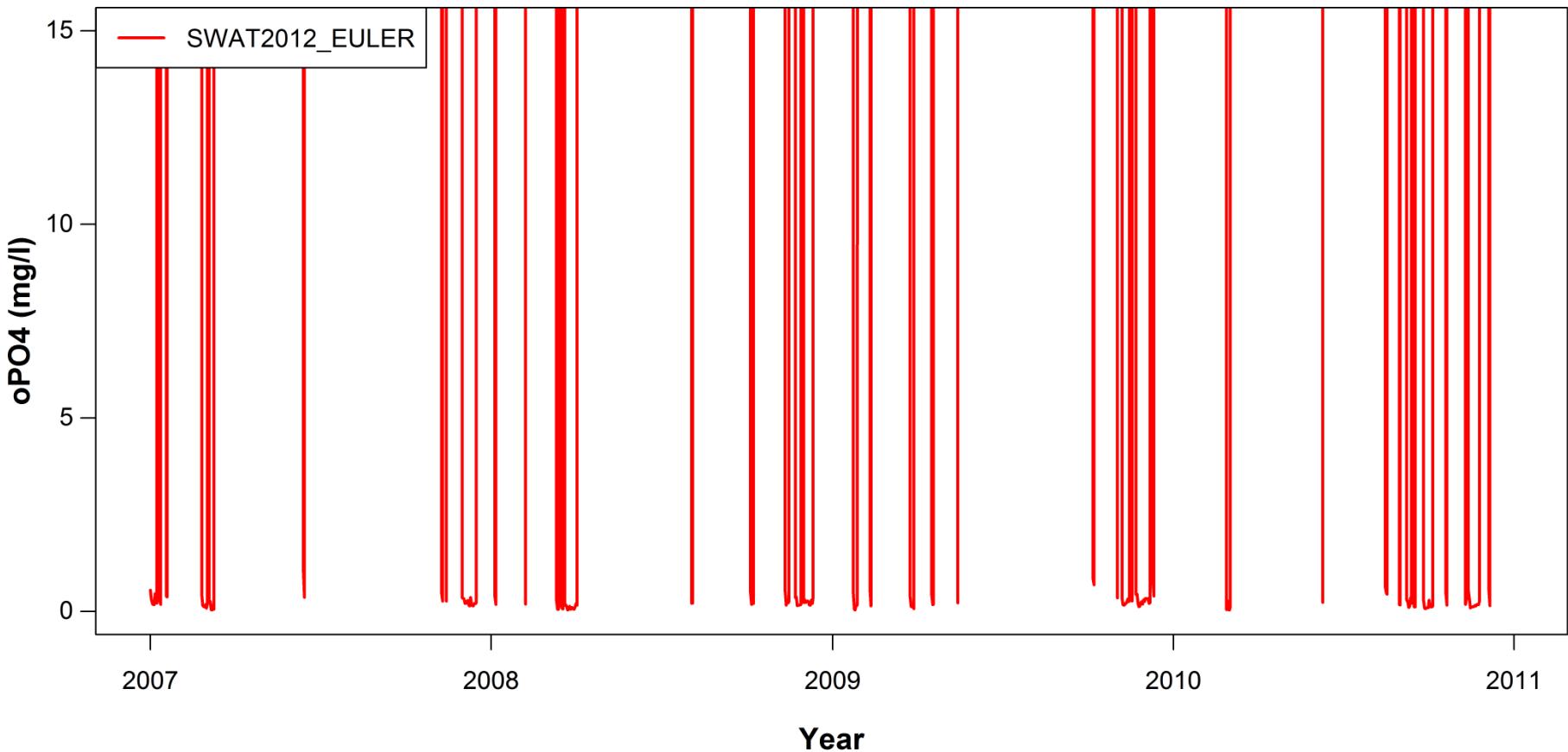
Instabilities/inaccuracy of Euler approach in SWAT WQ module

□ Default parameters



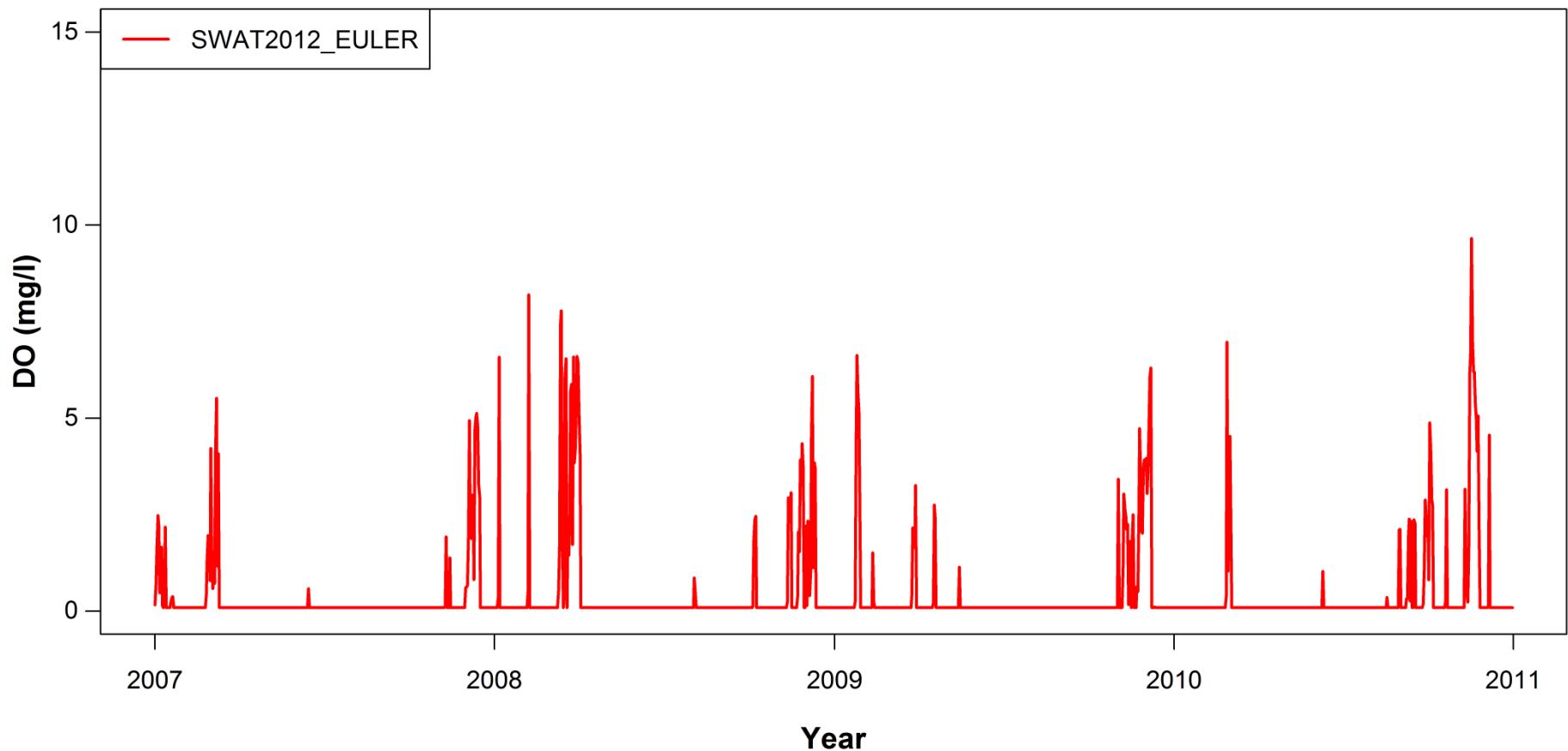
Instabilities/inaccuracy of Euler approach in SWAT WQ module

- Default parameters-zoommed



Instabilities/inaccuracy of Euler approach in SWAT WQ module

- Default parameters



New improved quasi-analytical method

□ Basis

- Continuity
- CSTR
- Dynamic

$$\frac{dC}{dt} + \frac{Q_{in}}{V} C(1 - r) + \textcolor{blue}{Ck - m} = \frac{Q_{im}}{V} (C_{im} - rC)$$

□ Analytical solution

- First order ordinary differential equation
- Assumptions

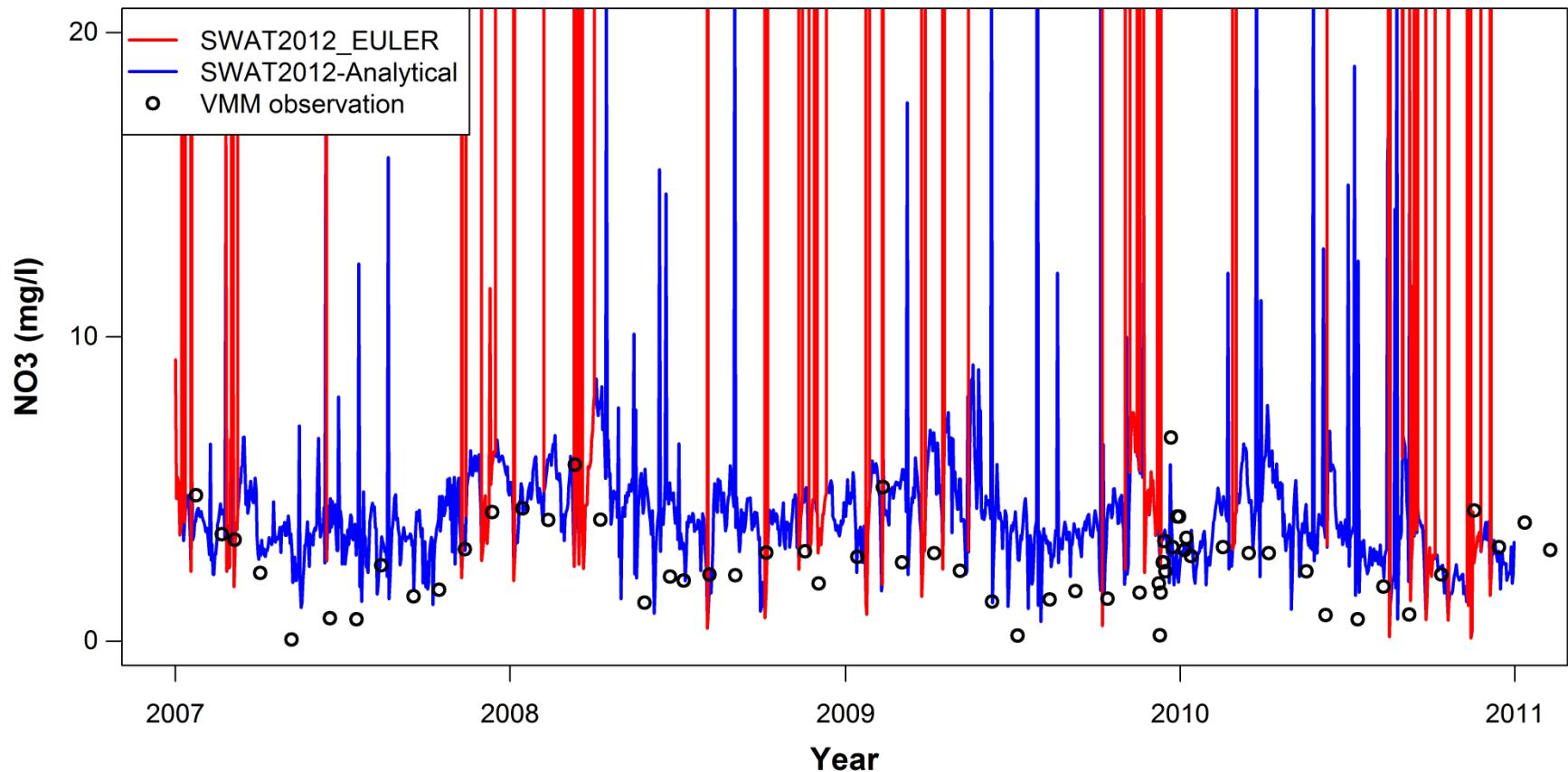
$$C_{t+\Delta t} = C_t e^{-\Delta t * \left(\frac{1}{t_{res}} + k\right)} + \left(\frac{C_{in,t+\Delta t}}{t_{res}} + m\right) * \frac{1}{\left(\frac{1}{t_{res}} + k\right)} \left[1 - e^{-\Delta t * \left(\frac{1}{t_{res}} + k\right)}\right]$$

□ Stability ??

□ Accuracy??

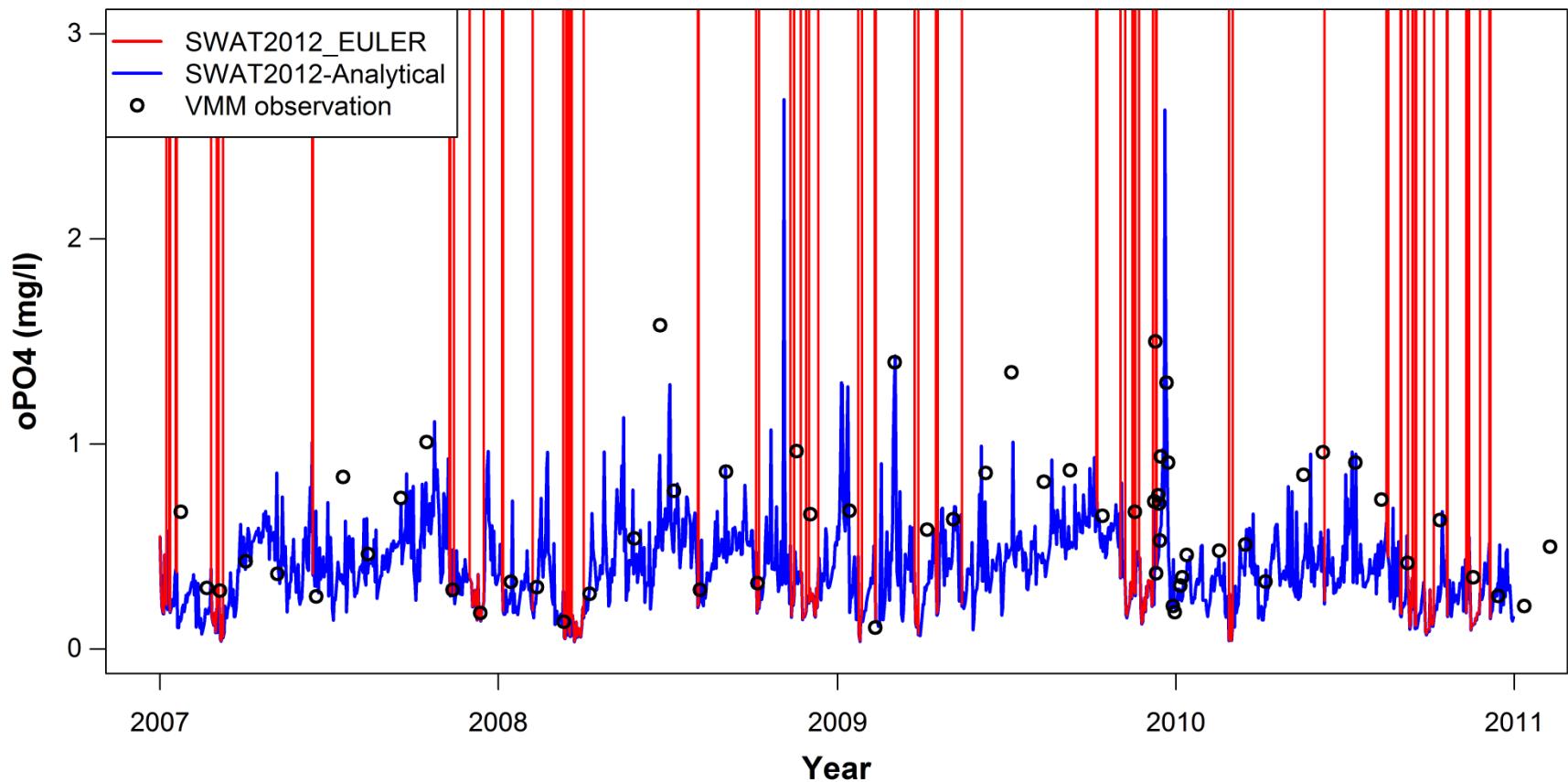
Better simulation/pattern by quasi-analytical method than EULER

- Default parameters



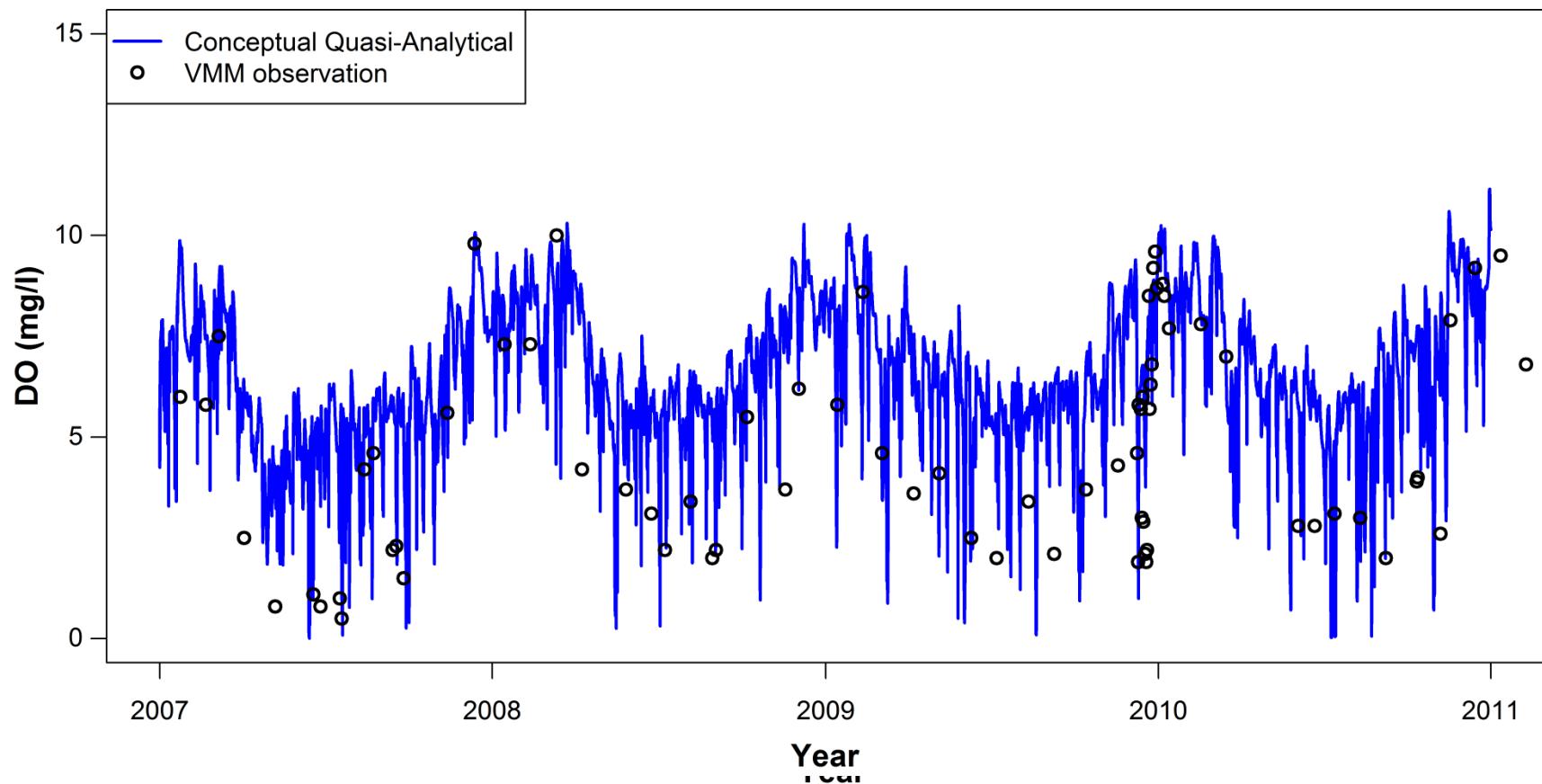
Stability comparison of the methods in SWAT2012

□ Default parameters



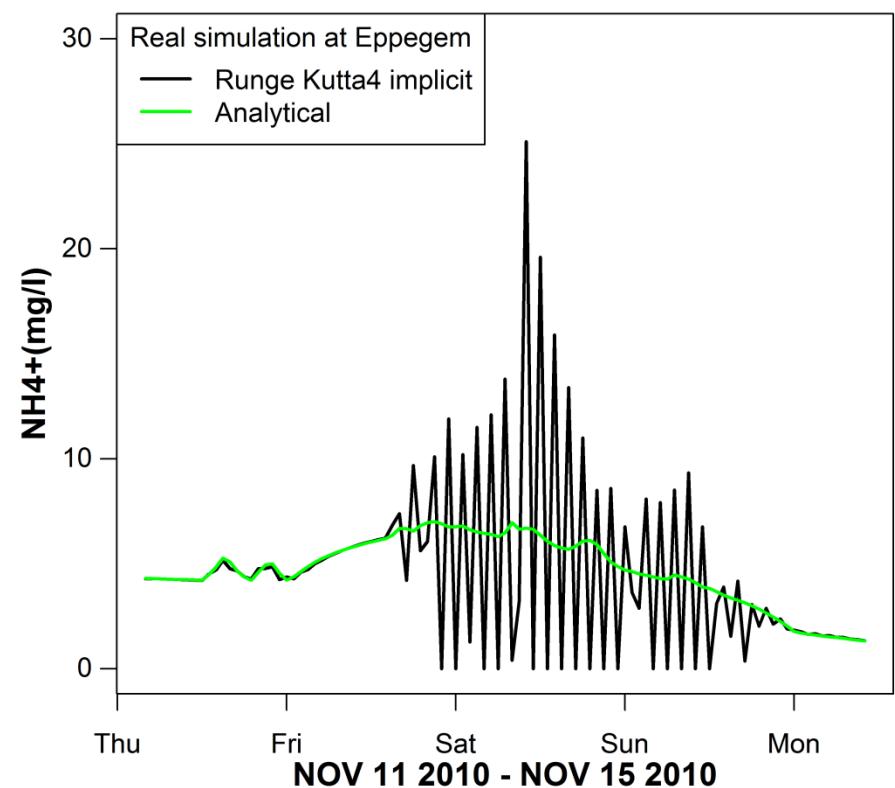
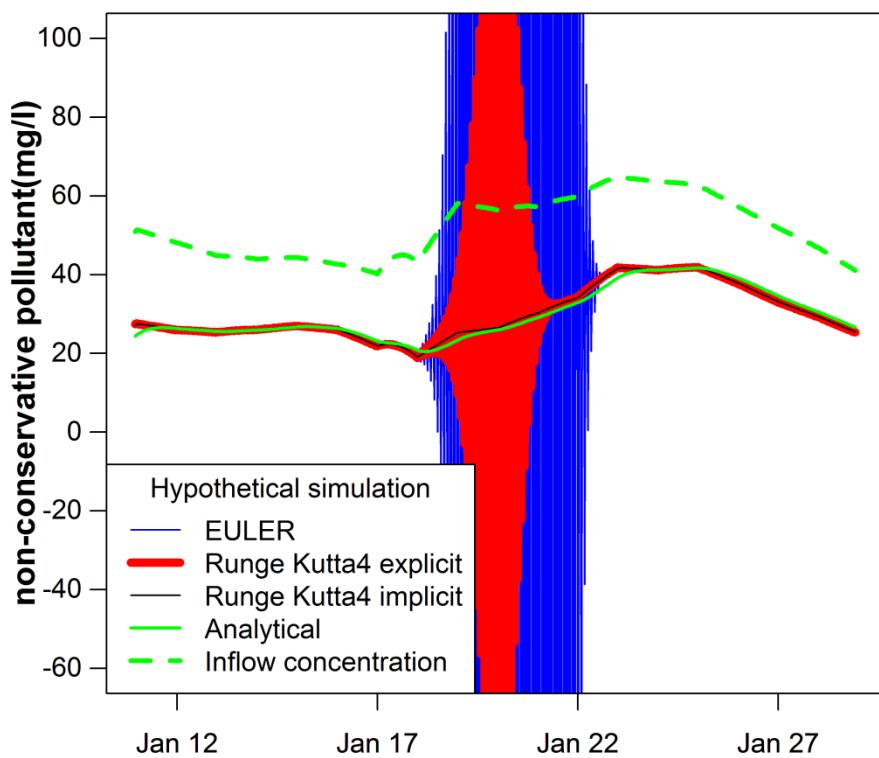
Stability comparison of the methods in SWAT2012

□ Default parameters



Instability comparison with other advanced numerical methods

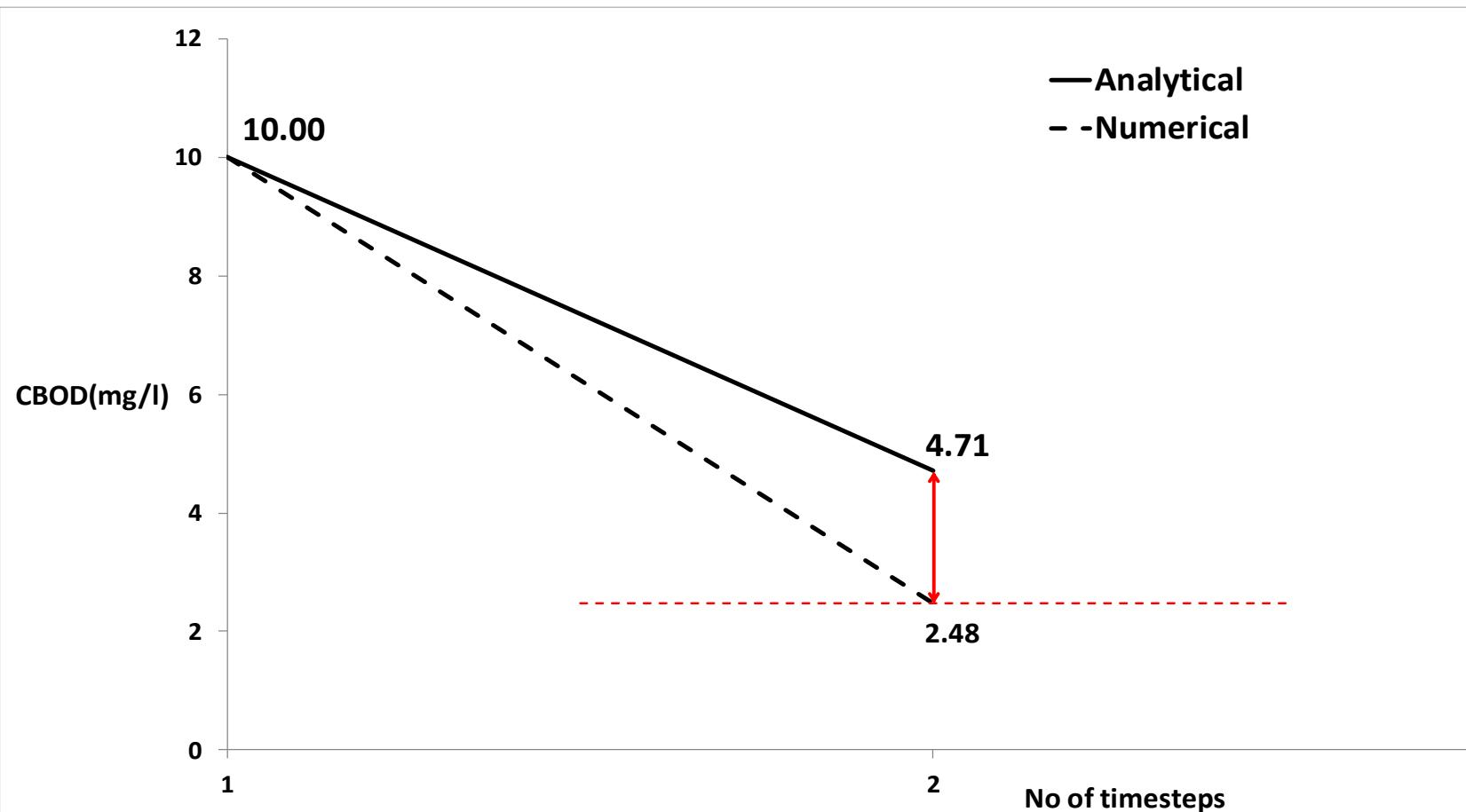
- Hypothetical case
- Real case (Zenne, Belgium)



Conclusions

- The new Quasi-analytical approach:
 - Is unconditionally stable
 - Is better than or as good as the advanced numerical methods
 - Less calibration effort
 - Better accuracy for low flow simulations, navigation canals
 - Increases reliability of instream WQ simulation of SWAT

Instabilities in the numerical solution method



tt/delt= 1.000 ◀ ▶ **K1+ K3 =** 0.75 ◀ ▶ **difference =** 47.5 %

Instabilities and residence time for Euler's method

