

SWAT-CUP

SWAT Calibration and Uncertainty Procedures

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Content

- **Issues in calibrating distributed models**
- **SWAT-CUP**

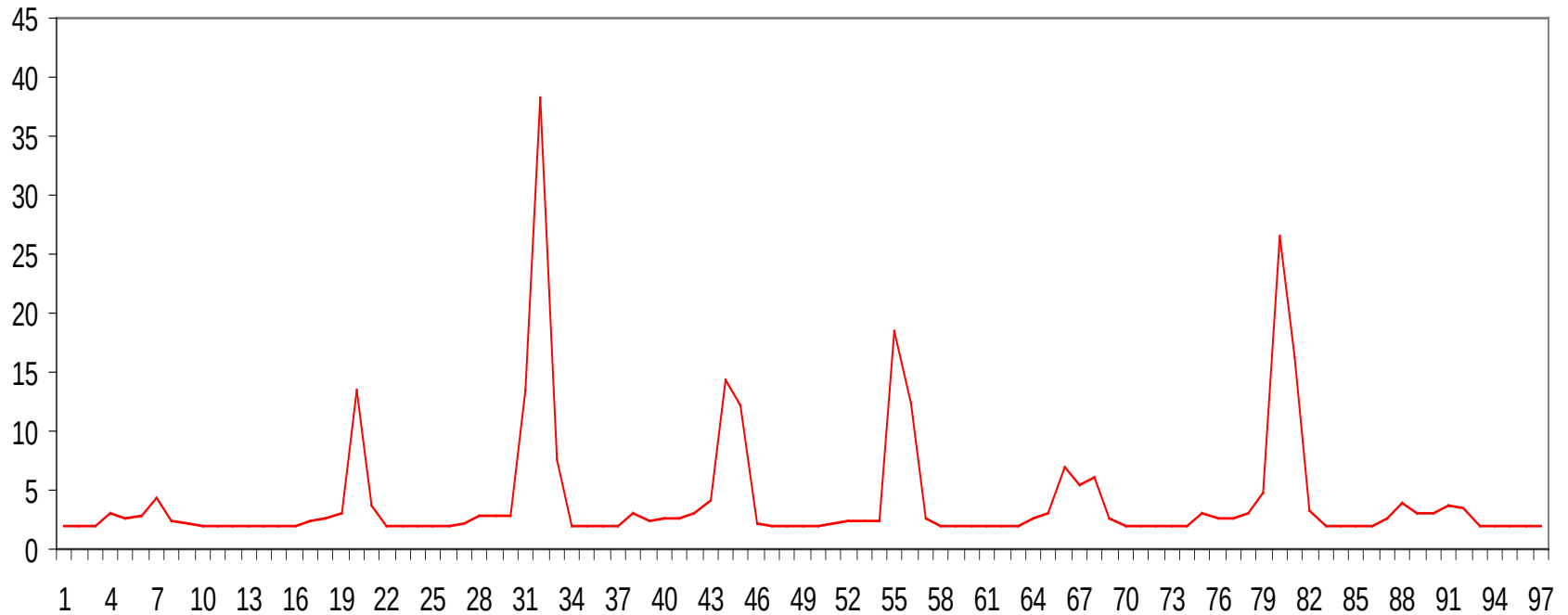
Modeling steps

- Calibration,
- Validation,
- Sensitivity analysis,
- Uncertainty analysis

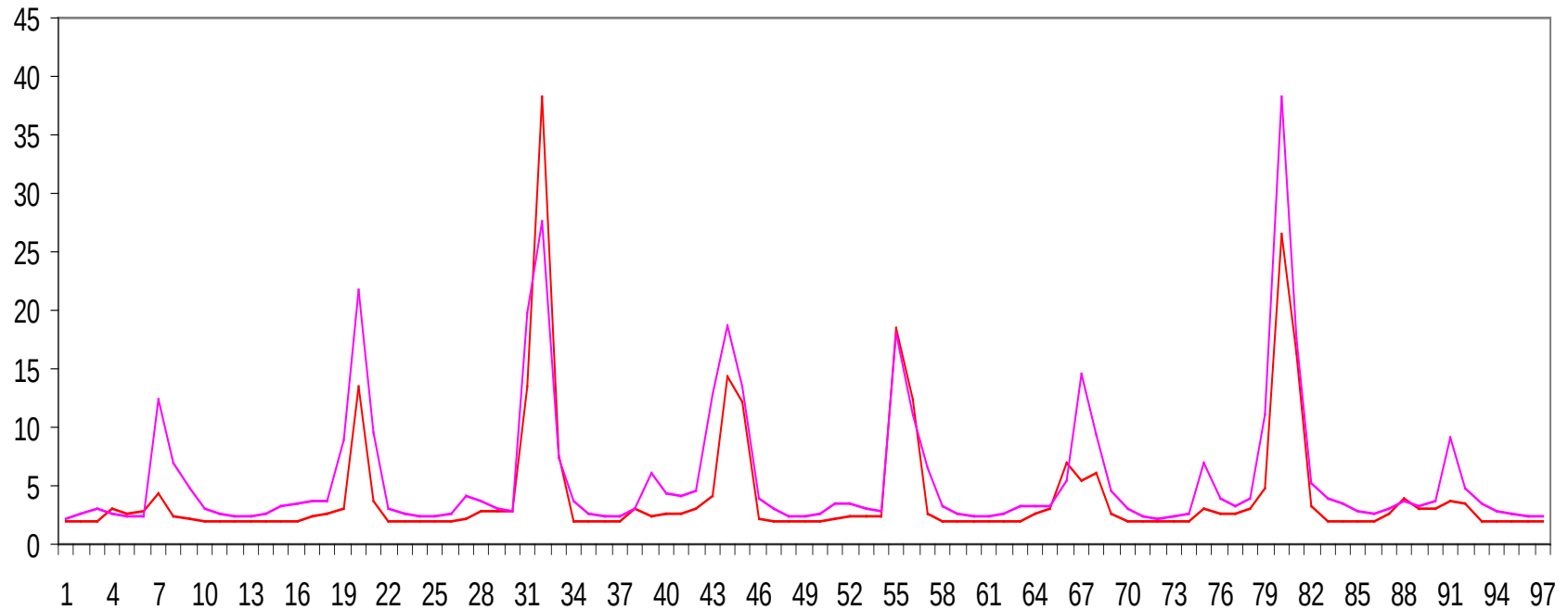
Modeling steps

- Calibration and **uncertainty analysis**
- Validation,
- Sensitivity analysis,

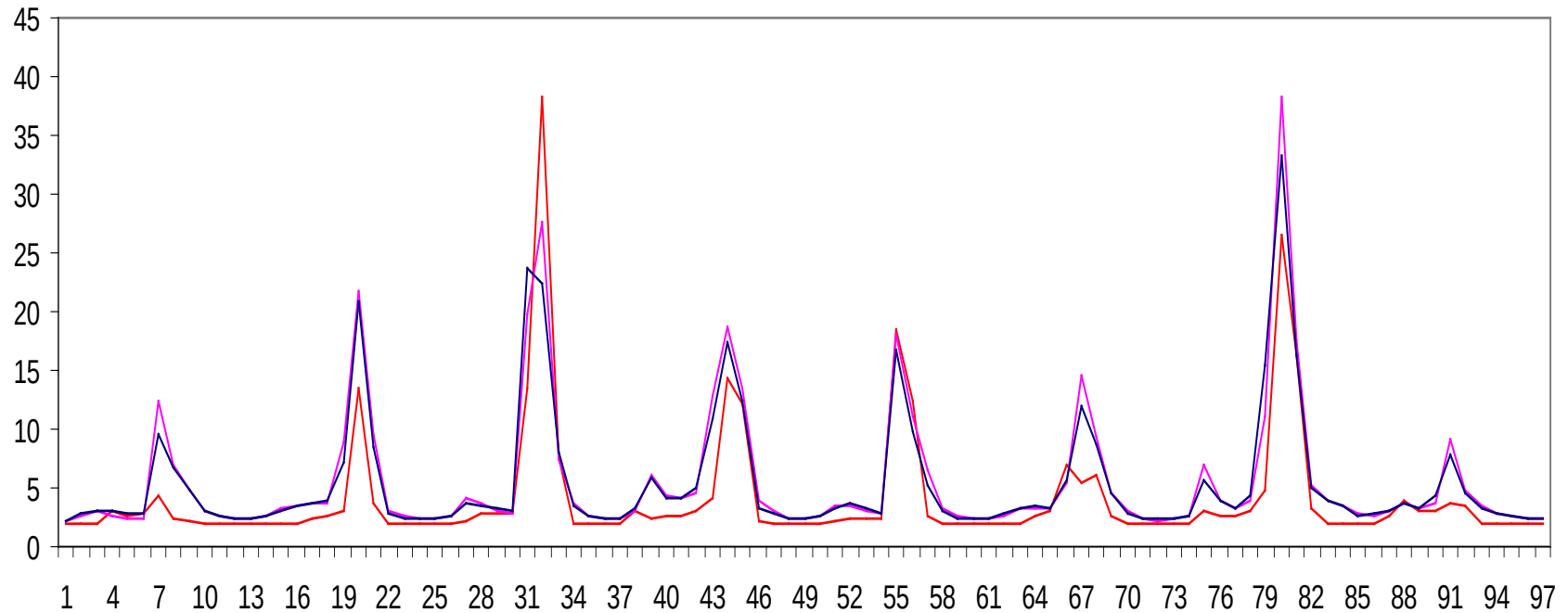
Calibration is subjective



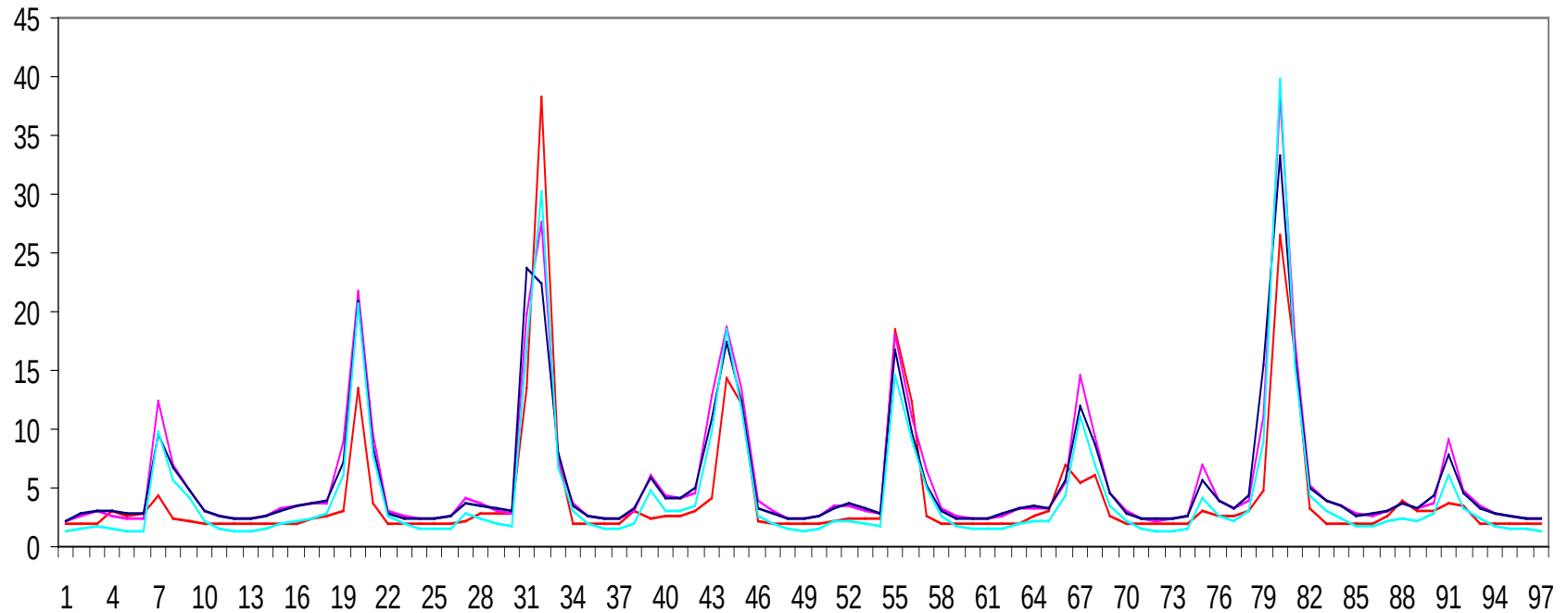
Calibration is subjective



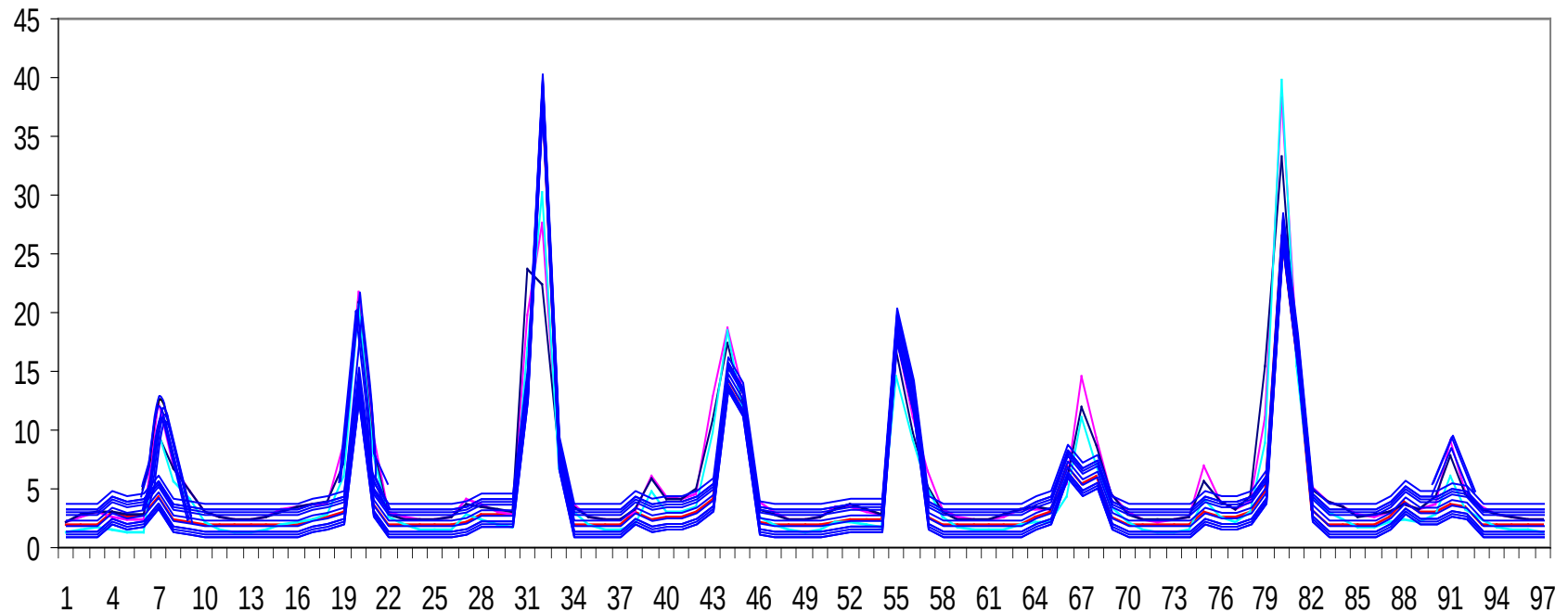
Calibration is subjective



Calibration is subjective



Calibration is subjective



Issues in Calibration of Distributed Models

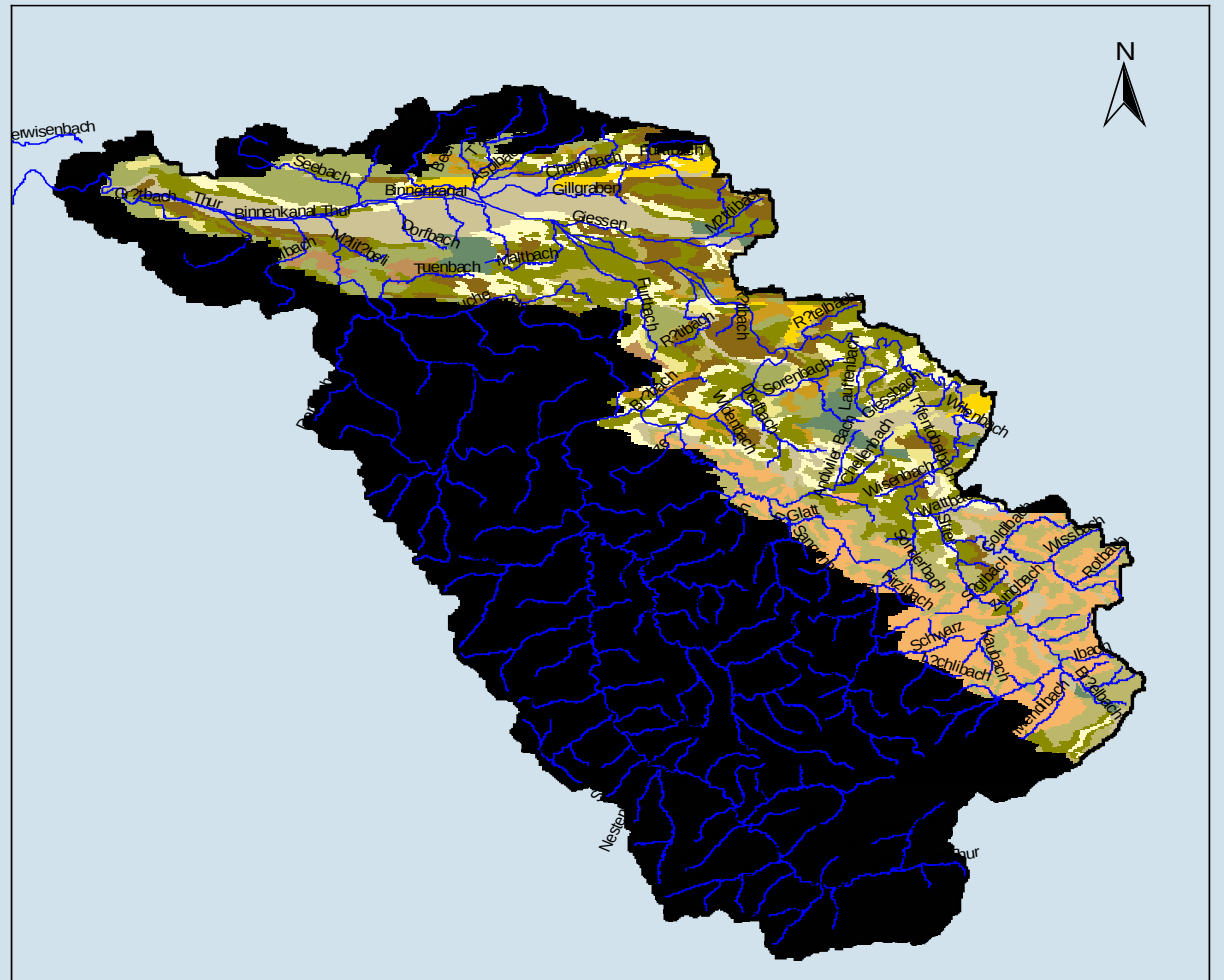
- 1- Parameterization
- 2- Objective function definition
- 3- Uniqueness problem
- 4- Parameter conditionality

1. Parameterization

Thur Basin Soil Map

Legend

-  Streams
-  Watershed Boundary
- Soils**
 -  DrumlinlandschL3
 -  DrumlinlandschL4
 -  Hoehel_Molasse2
 -  Hoehel_Molasse3
 -  Kalkbraunerde
 -  Leicht_Moraen_G1
 -  Leicht_Moraen_G2
 -  Leicht_Moraen_G3
 -  Leicht_Moraen_G4
 -  Parabraunerde
 -  Seen
 -  Siedlung
 -  Tief_Mola_MoraH1
 -  Tief_Mola_MoraH2
 -  Tief_Mola_MoraH3
 -  Tief_Mola_MoraH4
 -  mountain



Scale 0 9 18 Miles

1. Parameterization

**x__<parname>.<ext>__<hydrogrp>__<soltext>__<landuse>__<subbsn>__
__<Slope>**

Where

x	= Code to indicate the type of change to be applied to the parameter: v – means the existing parameter value is replaced by a given value, a – means the given value is added to the existing parameter value, and r– means the existing parameter value is multiplied by (1+the given value);
<parname>	= SWAT parameter name;
<ext>	= SWAT file extension code for the file containing the parameter;
<hydrogrp>	= soil hydrological group ('A','B','C' or 'D');
<soltext>	= soil texture;
<landuse>	= name of the landuse category;
<subbsn>	= sub-basin number or crop index.

Soil Parameters

Parameter identifiers	Description
r__SOL_K(1).sol	K of Layer 1 of all HRUs
r__SOL_K(1,2,4-6).sol	K of Layer 1,2,4,5, and 6 of all HRUs
r__SOL_K().sol	K of All layers and all HRUs
r__SOL_K(1).sol__D	K of layer 1 of HRUs with hydrologic group D
r__SOL_K(1).sol____FSL	K of layer 1 of HRUs with soil texture FSL
r__SOL_K(1).sol____FSL__PAST	K of layer 1 of HRUs with soil texture FSL and landuse PAST
r__SOL_K(1).sol____FSL__PAST__1-3	K of layer 1 of subbasin 1,2, and 3 with HRUs containing soil texture FSL and landuse PAST

Management Parameters

Parameter identifiers	Description
v__HEAT_UNITS{rotation no,operation no}	Management parameters that are subject to operation/rotation must have both specified

Crop Parameters

Parameter identifiers	Description
v__T_OPT{30}.CROP.DAT	Parameter T_OPT for crop number 30 in the crop.dat file
v__PLTNFR(1){3}.CROP.DAT	Nitrogen uptake parameter #1 for crop number 3 in crop.dat file

Rainfall Parameters

Parameter identifiers	Description
<code>v__precipitation(1){1977300}.pcp</code>	(1) means column number 1 in the pcp file {1977300} specifies year and day
<code>v__precipitation(1-3){1977300}.pcp</code>	(1-3) means column 1, 2, and 3 {1977300} specifies year and day
<code>v__precipitation() {1977300,1977301}.pcp</code>	() means all columns (all stations) {1977300,1977301} means 1977 days 300 and 301
<code>v__precipitation() {1977001- 1977361,1978001- 1978365,1979003}.pcp</code>	() means all columns from day 1 to day 361 of 1977, and from day 1 to day 365 of 1978, and day 3 of 1979

2. Objective function definition

Different objective functions produce different calibration results

S-MSR

$$g(\mathbf{B}) = w_1 \sum_{i=1}^{n_1} (Q_o - Q_s)_i^2 + w_2 \sum_{i=1}^{n_2} (S_o - S_s)_i^2 + \dots$$

M-MSR

$$g(\mathbf{B}) = \sum_{i=1}^{n_1} (Q_o - Q_s)_i^2 * \sum_{i=1}^{n_2} (S_o - S_s)_i^2 * \dots$$

NS

$$g(\mathbf{B}) = \left[1 - \frac{\sum_{i=1}^{n_1} (O_i - P_i)^2}{\sum_{i=1}^{n_1} (O_i - \bar{O})^2} \right]$$

2. Objective function definition

R^2

$$g(\mathbf{B}) = \left[\frac{\sum_{i=1}^n (O_i - \bar{O})(P_i - \bar{P})}{\sqrt{\sum_{i=1}^n (O_i - \bar{O})^2} \sqrt{\sum_{i=1}^n (P_i - \bar{P})^2}} \right]^2$$

χ^2

$$\chi^2 = \frac{\sum_i (Q_m - Q_s)_i^2}{\sigma_Q^2}$$

bR^2

$$g(\mathbf{B}) = \begin{cases} |b| \cdot R^2 & \text{for } b \leq 1 \\ |b|^{-1} \cdot R^2 & \text{for } b > 1 \end{cases}$$

2. Objective function definition

The SSQR method aims at the fitting of the frequency distributions of the observed and the simulated series. After independent ranking of the measured and the simulated values, new pairs are formed and the SSQR is calculated as

$$SSQR = \sum_{j=1,n} [Q_{j,measured} - Q_{j,simulated}]^2$$

SSQR

2. Objective function definition

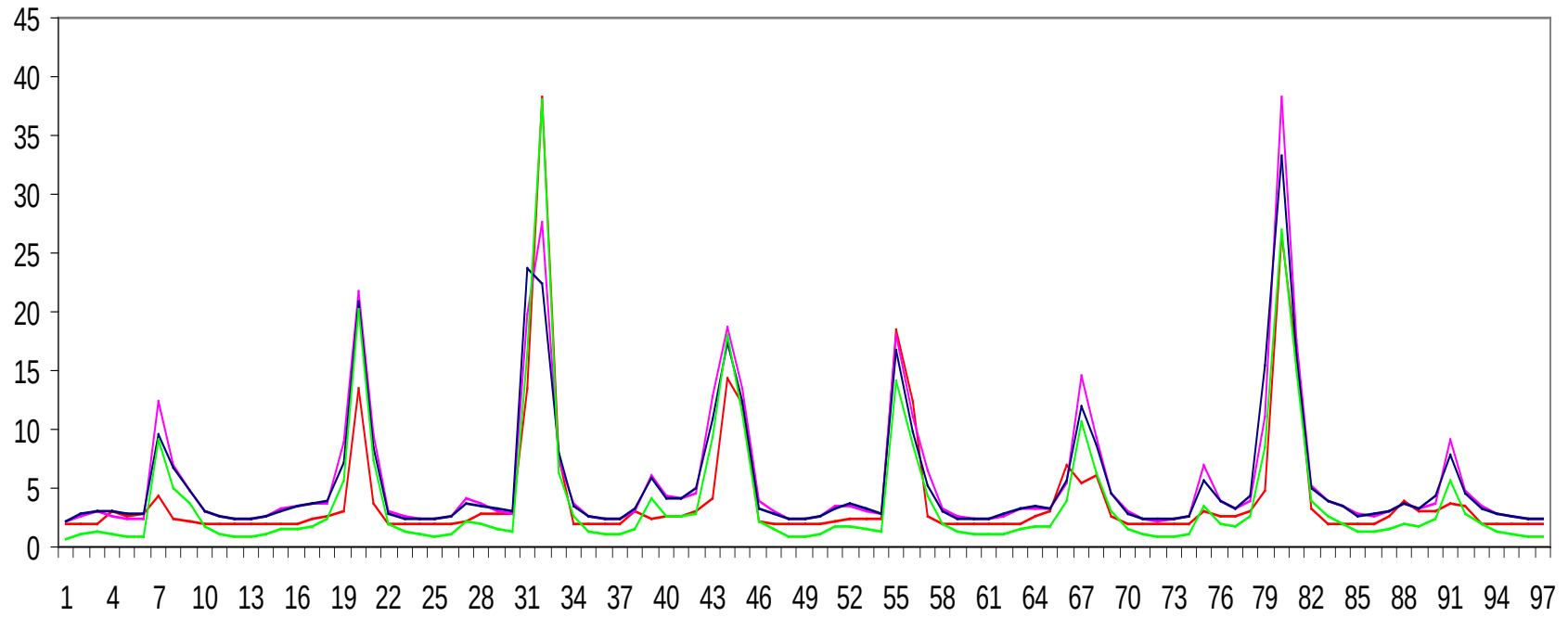
Likelihood function in a Bayesian inference using Box-Cox transformation and continuous time auto regressive function:

$$f_{Y^M|\theta}(y|\theta) = \frac{1}{\sqrt{2\pi}} \frac{1}{\sigma} \exp\left(-\frac{1}{2} \frac{[g(y_{t_0}) - g(y_{t_0}^M(\theta))]^2}{\sigma^2}\right) \cdot \left| \frac{dg}{dy} \right|_{y=y_{t_0}}$$

$$\cdot \prod_{i=1}^n \left[\frac{1}{\sqrt{2\pi}} \frac{1}{\sigma \sqrt{1 - \exp\left(-2 \frac{t_i - t_{i-1}}{\tau}\right)}} \exp\left(-\frac{1}{2} \frac{\left[\begin{array}{c} g(y_{t_i}) - g(y_{t_i}^M(\theta)) \\ - [g(y_{t_{i-1}}) - g(y_{t_{i-1}}^M(\theta))] \exp\left(-\frac{t_i - t_{i-1}}{\tau}\right) \end{array} \right]^2}{\sigma^2 \left(1 - \exp\left(-2 \frac{t_i - t_{i-1}}{\tau}\right)\right)} \right) \cdot \left| \frac{dg}{dy} \right|_{y=y_{t_i}} \right]$$

*Yang et al., 2007, WRR,
JHydrol*

2. Objective function definition



RMSE	R2	NS	bR2
29.90	0.79	0.67	0.54
29.70	0.75	0.67	0.42
23.50	0.84	0.83	0.45
21.10	0.90	0.80	0.62
23.30	0.84	0.80	0.75

3. Uniqueness problem

Direct (deterministic) Modelling:



Inverse Modelling:



3. Uniqueness problem



So, different parameter sets can give you equally good calibration results

CN2	ALPHA_BF	REVAPMN	GW_REVAP	RCHRG_DP	SOL_AWC	SOL_K	SOL_BD
-0.20	0.25	83.4	0.05	0.09	-0.19	0.57	-0.13
0.11	0.59	66.0	0.05	0.19	-0.25	0.45	-0.19
0.33	0.35	86.1	0.07	0.19	-0.04	0.30	0.08
0.29	0.50	32.8	0.07	0.29	-0.16	0.29	-0.07

4. Parameter Conditionality

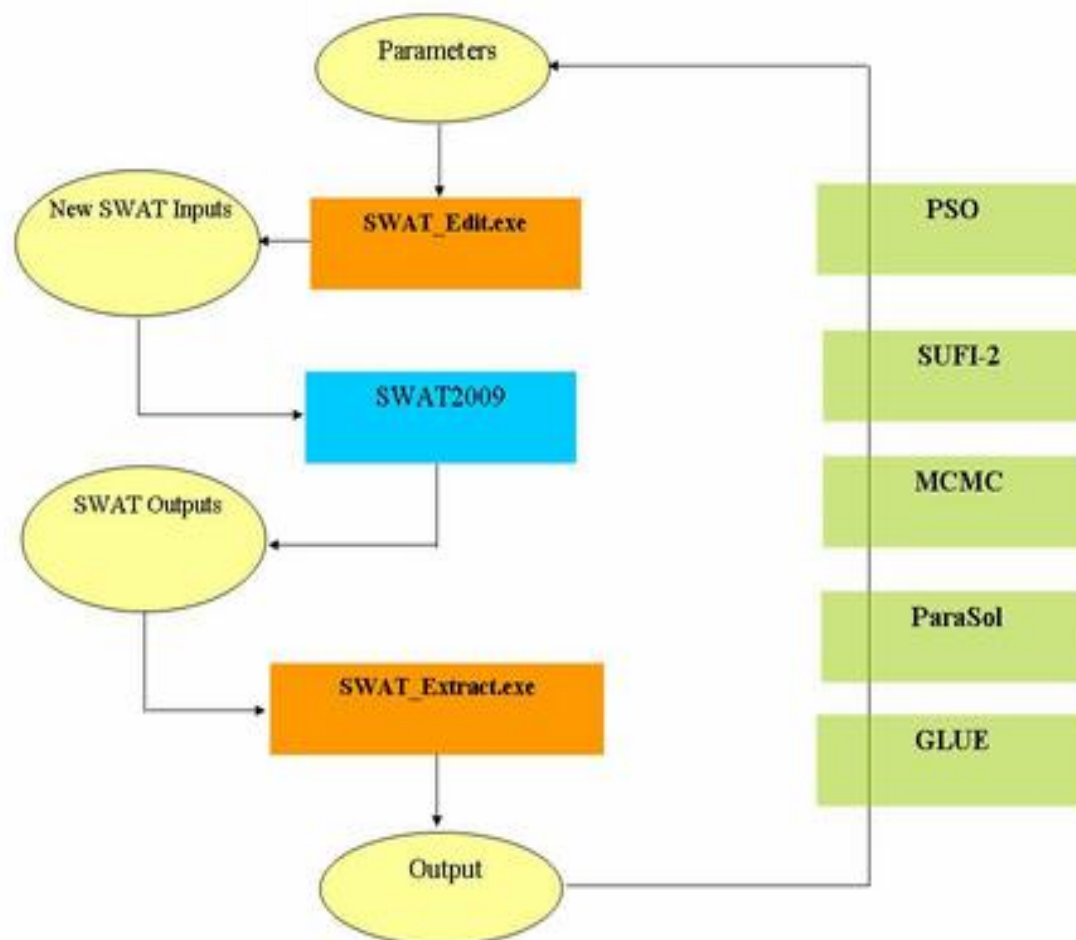
(B)

- watershed parameterization
- type of the objective function
- weights in the objective function
- conceptual model (model structure)
- experimental procedure (to collect the calibrating data)
- input (driving or forcing) data
- number and type of variables (in the objective function)
- location of outlets
-

SWAT-CUP

SWAT-CUP

SWAT-CUP is a computer program for calibration of SWAT models. SWAT-CUP is a public domain program, and as such may be used and copied freely. The program links GLUE, ParaSol, SUFI2, MCMC, and PSO procedures to SWAT. It enables sensitivity analysis, calibration, validation, and uncertainty analysis of a SWAT model. The overall program structure is as shown in the Figure below.





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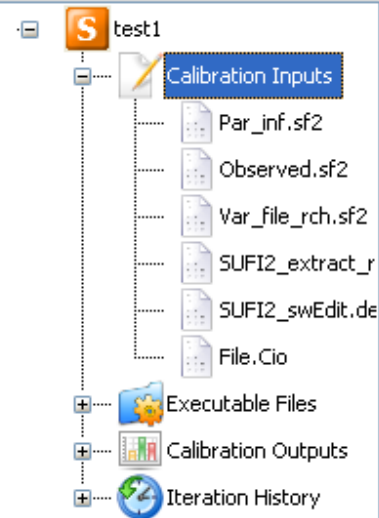
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test



Calibration Inputs

Par_inf.sf2

Observed.sf2

Var_file_rch.sf2

SUF2_extract_r

SUF2_swEdit.de

File.Cio



Executable Files



Calibration Outputs



Iteration History

Par_inf.sf2

**Par_inf.sf2**

Sufi2 parameters information

Test_example_2009

Number_of_Parameters= 14

Number_of_LH_sims= 20

r_CN2.mgt_____PAST	-0.3	0.3
r_CN2.mgt_____1,4	-0.2	0.2
r_ALPHA_BF.gw	0.0	0.1
v_GW_DELAY.gw	10.0	45.0
v_CH_N2.rte	0.0	0.1
v_CH_K2.rte	5.0	40.0
v_ALPHA_BNK.rte	0.0	1.0
r_SOL_AWC(1).sol_____1,2	0.02	0.4
r_SOL_AWC(1).sol_____3,4	0.02	0.4
r_SOL_K(1).sol_____1,2	-0.5	0.8
r_SOL_K(1).sol_____3,4	-0.5	0.8
r_SOL_BD(1).sol_____1,2	-0.1	0.1
r_SOL_BD(1).sol_____3,4	-0.1	0.1
v_SFTMP.bsn	-2.0	2.0

v_GW_DELAY.gw	45	29.813421	40.136478		
v_ALPHA_BF.gw	45	0.320068	0.579920		
v_GW_REVAP.gw	45	0.0	0.163754		
v_RCHRG_DP.gw	45	0.038500	0.233160		
r_SOL_K().sol	45	-0.300590	0.512008		
v_ESCO.hru	45	0.391444	0.749038		
v_SLSUBBSN.hru	45	18.260817	40.833183		
v_CH_K2.rte	45	0.0	6.095049		
r_HRU_SLP.hru	45	0.263282	0.633366		
r_CN2.mgt	61	0.556328	1.020978		
v_REVAPMN.gw	61	5.263700	10.631983		
v_GW_REVAP.gw	61	0.083167	0.249507		
v_RCHRG_DP.gw	61	0.264409	0.532161		
r_SOL_K().sol	61	-0.927616	0.049724		
r_SOL_BD().sol	61	0.356627	1.013543		
v_ESCO.hru	61	0.02	0.235157		
v_SLSUBBSN.hru	61	0.0	19.965151		
v_OV_N.hru	61	0.287933	0.670415		
r_CH_N2.rte	61	-0.066399	0.582939		
v_ALPHA_BNK.rte	61	0.0	0.221242		
r_CN2.mgt	5-11,13,14,16,18,22,23,27-30,33-35,39-41,44,47,48,50-57,59,60,63			0.348061	0.5437
r_CN2.mgt	12,15,24	-0.002354	0.682160		
r_CN2.mgt	1,2,3,4	-0.081239	0.245297		
r_CN2.mgt	17,22,31,32,36		0.435100	0.610310	
r_CN2.mgt	27,42,49,46,43		0.127156	0.425522	
r_CN2.mgt	52	-0.324336	0.006194		
v_GW_REVAP.gw	1,2,3,4	0.129748	0.389252		
v_GW_REVAP.gw	17,22,31,32,36		0.059568	0.217864	
v_GW_REVAP.gw	52	0.0	0.087147		
r_SOL_AWC().sol	5-16,18-25,26-30,33-35,37-41,44,47,48,50-57,59,60,63			0.070241	0.280667
r_SOL_AWC().sol	1,2,3,4	-0.118537	0.181741		
r_SOL_AWC().sol	27,42,49,46,43		0.100708	0.336324	
r_SOL_AWC().sol	52	-0.007669	0.250197		
v_ALPHA_BNK.rte	5-16,18-25,26-30,33-35,37-41,44,47,48,50-57,59,60,63			0.321167	0.628545
v_SMTMP.bsn	2.482387	5.280932			



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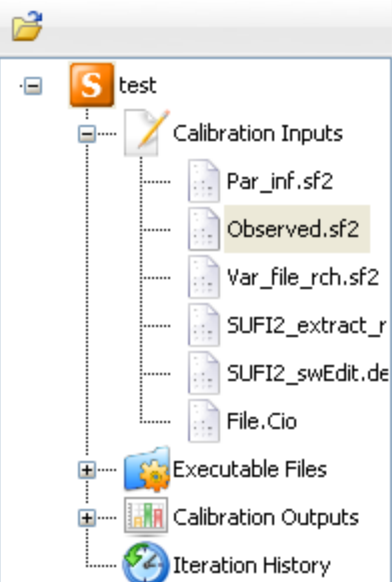
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Par_inf.sf2

Observed.sf2

**Observed.sf2**

Observed Data

```
no_obs_vars= 5
Obj_Fn_Type(1=mult,2=sum,3=r2,4=chi2,5=NS,6=br2,7=Ssq)= 5
behavioral_threshold= .45

q_1
var_weight= 1
var_Threshold= -1
wt_below_threshold= 1
wt_above_threshold= 1
pcnt_Error= 10
NO_Data= 21
4 q_1_1977.4 0.5913
5 q_1_1977.5 0.8188
6 q_1_1977.6 0.3899
7 q_1_1977.7 0.2955
8 q_1_1977.8 0.1019
9 q_1_1977.9 0.2147
10 q_1_1977.10 1.906
11 q_1_1977.11 0.4995
12 q_1_1977.12 0.3348
13 q_1_1978.1 0.5686
14 q_1_1978.2 0.7132
15 q_1_1978.3 0.4877
16 q_1_1978.4 0.5748
17 q_1_1978.5 2.199
18 q_1_1978.6 0.5848
19 q_1_1978.7 0.1127
20 q_1_1978.8 0.0012
21 q_1_1978.9 0.8347
```



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Par_inf.sf2

Observed.sf2

SUF12_extract_rch.def



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Calibration Inputs



Par_inf.sf2



Observed.sf2



Var_file_rch.sf2



SUF12_extract_r



SUF12_swEdit.de



File.Cio



Executable Files



Calibration Outputs



Iteration History

*SUF12_extract_rch.def*

swat_output_file= output.rch

no_vars_to_get= 3

var_column_no[no_vars_to_get]= 7 11 18

reaches_for_each_variable[no_vars_to_get]

no_reaches_to_get= 2

reach_no= 1 2

no_reaches_to_get= 2

reach_no= 1 3

no_reaches_to_get= 1

reach_no= 4

total_reaches_in_project= 4

beg_year= 1977

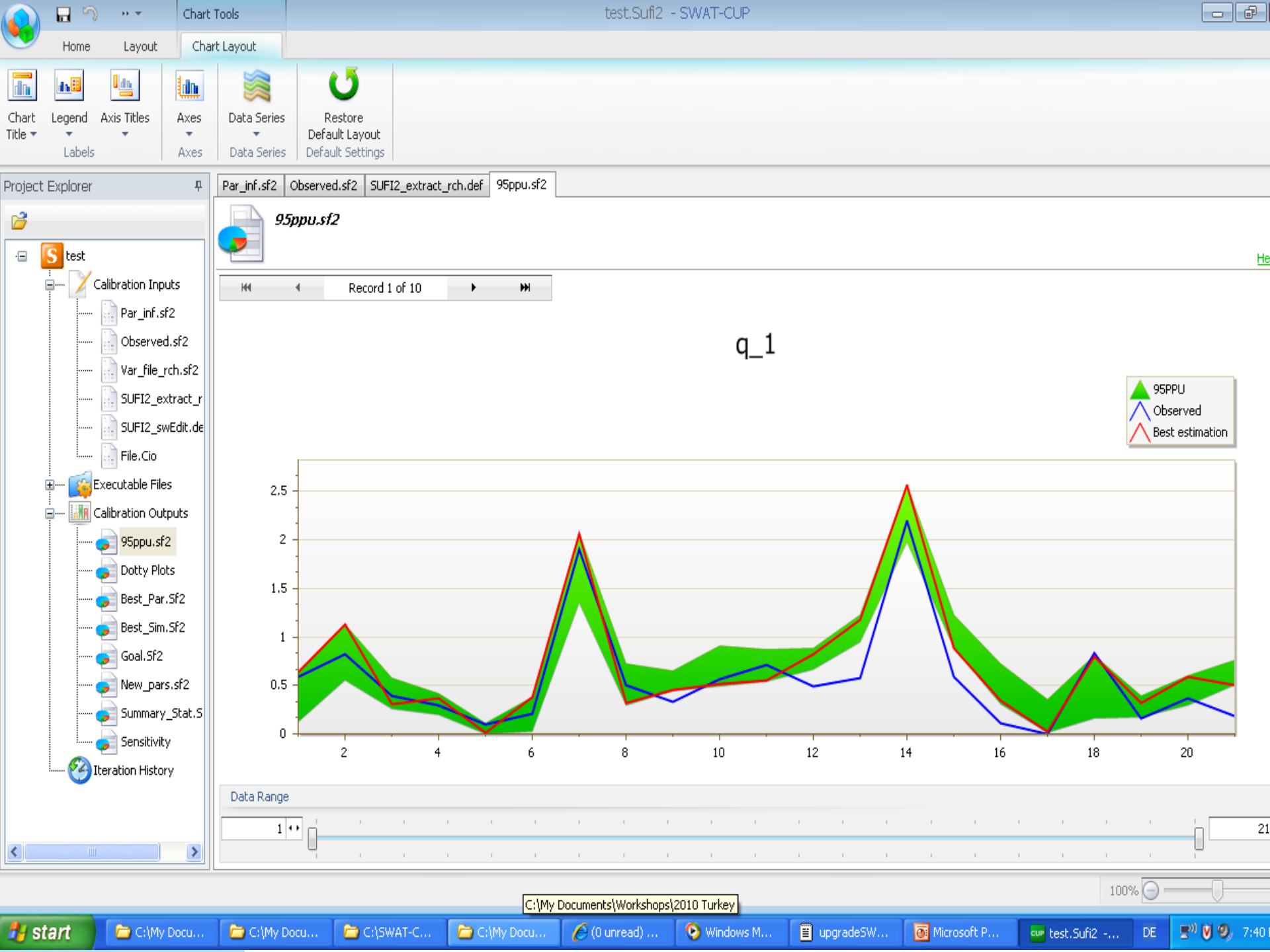
end_year= 1978

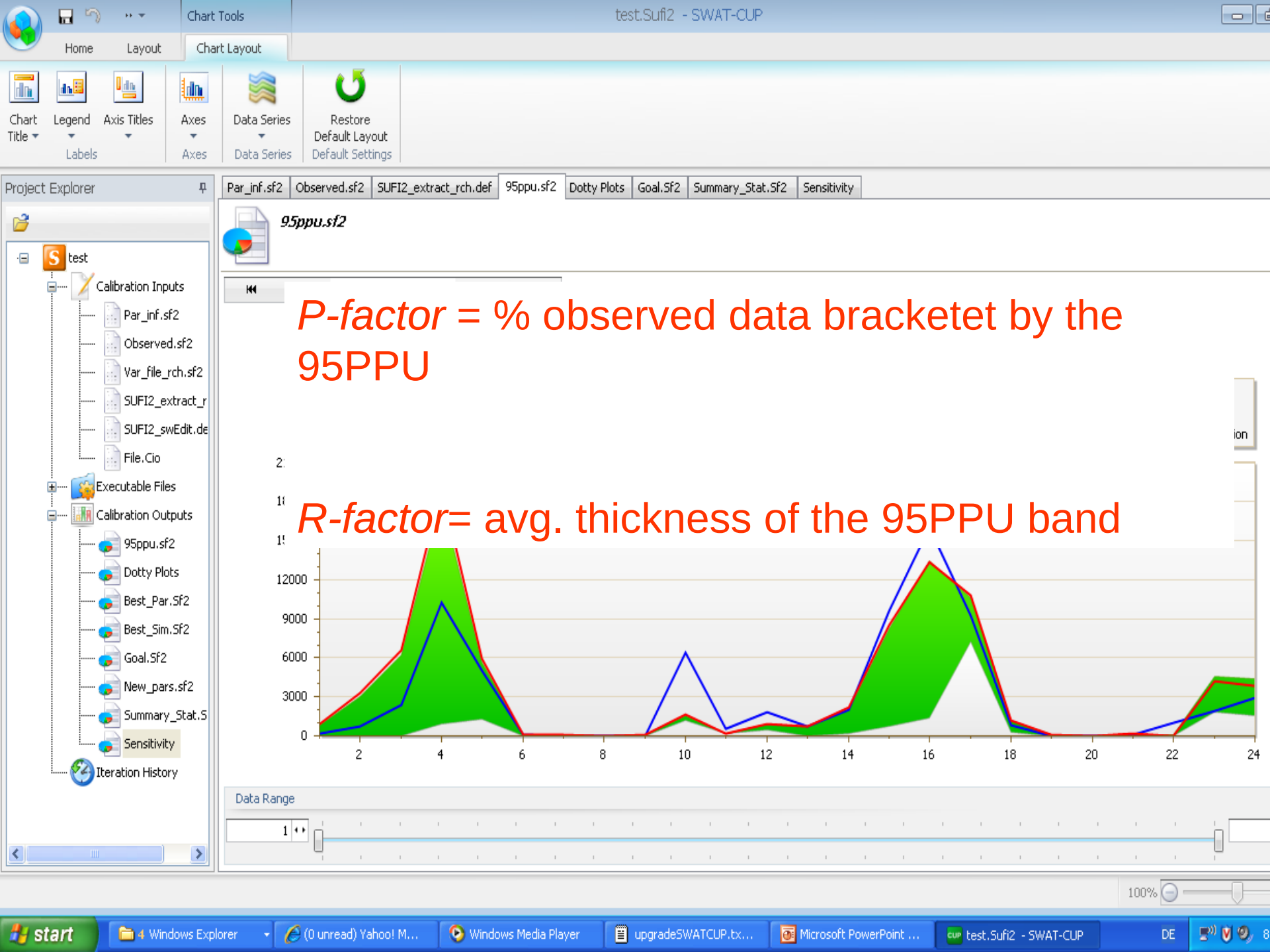
time_step(1d,2m,3y)= 2

/**** Remark

column_no= 7 discharge (m3/s)

column_no= 11 sed out (tn)







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SUF12_swEdit.de

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95ppu.sf2

Dotty Plots

Best_Par.Sf2

Best_Sim.Sf2

Goal.Sf2

New_pars.sf2

Summary_Stat.S

Sensitivity

Iteration History

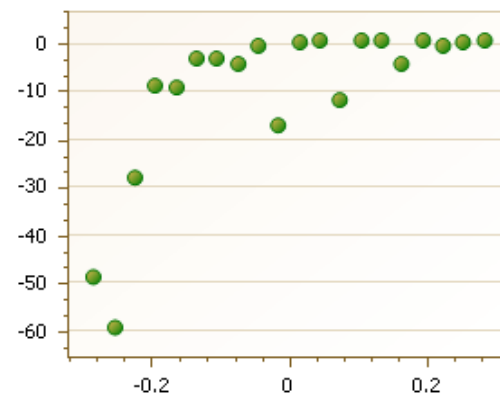
Par_inf.sf2 Observed.sf2 SUFI2_extract_rch.def 95ppu.sf2 Dotty Plots



Dotty Plots

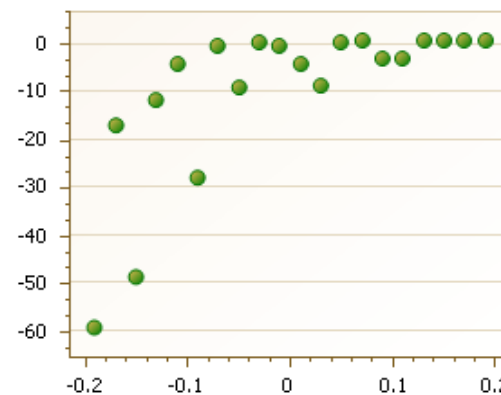


r_CN2.mgt_____PAST



r_ALPHA_BF.gw

r_CN2.mgt_____1,4

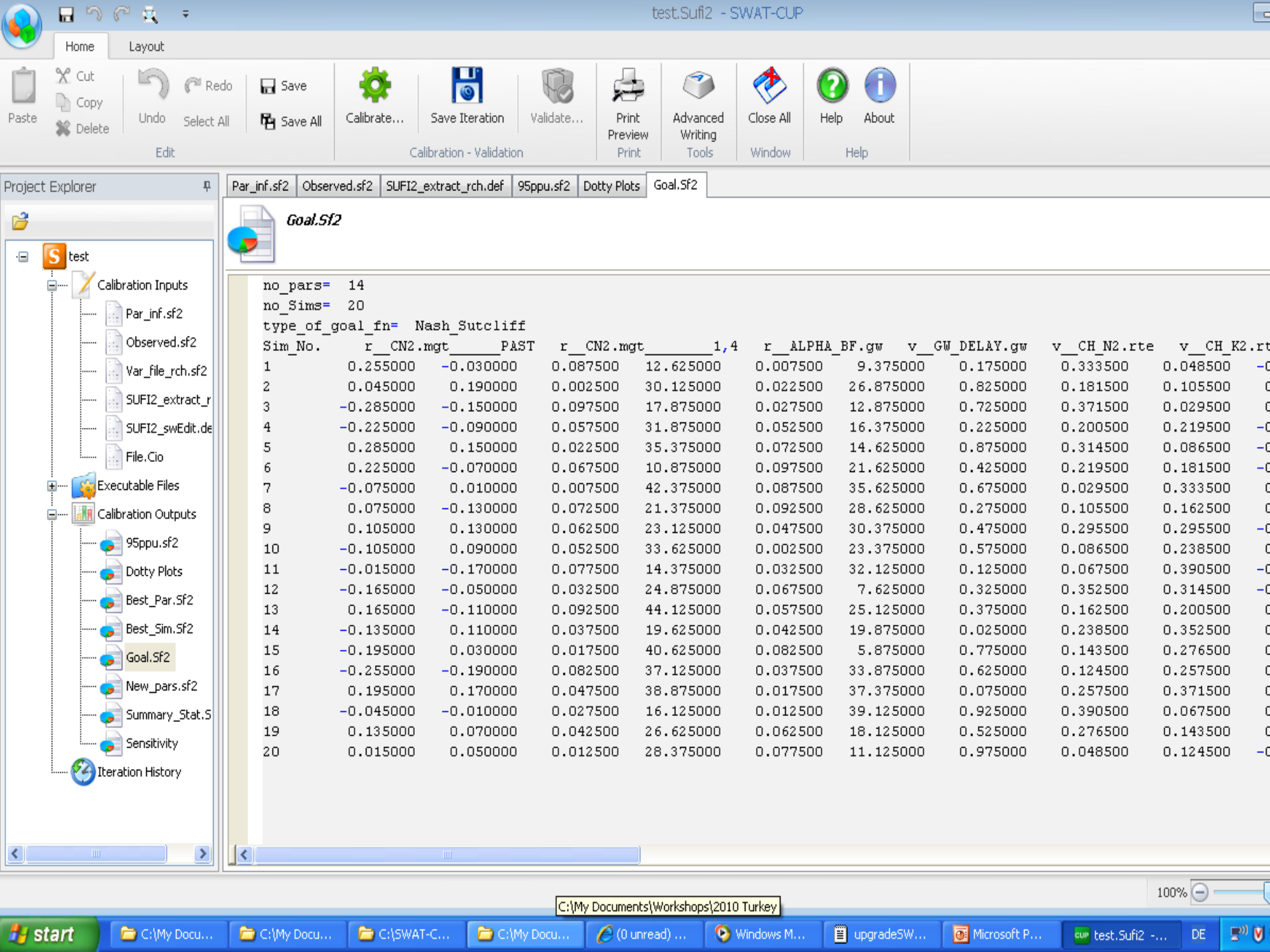


v_GW_DELAY.gw

Current Page No: none

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Dotty Plots

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Best_Sim.Sf2

Goal.Sf2

New_pars.sf2

Summary_Stat.S

Sensitivity

Iteration History

Par_inf.sf2

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SUF12_extract_rch.def

95ppu.sf2

Dotty Plots

Goal.Sf2

Summary_Stat.Sf2

*Summary_Stat.Sf2*

Goal_type= Nash_Sutcliffe (type 5) Best_sim_no= 5 Best_goal = 7.658981e-001

Variable	p_factor	r-factor	R2	NS	br2	MSE
q_1	0.62	0.70	0.90	0.80	0.8397	0.0561
q_2	0.58	0.63	0.94	0.86	0.9317	0.0977
S_1	0.50	0.31	0.74	0.70	0.4481	764768
s_3	0.63	0.65	0.75	0.65	0.7433	611138
N_4	0.52	9.31	0.82	0.82	0.6819	256179

-- Results for behavioral parameters

Variable	p_factor	r-factor	R2	NS	br2	MSE
q_1	0.52	0.35	0.90	0.80	0.8397	0.0561
q_2	0.29	0.22	0.94	0.86	0.9317	0.0977
S_1	0.29	0.19	0.74	0.70	0.4481	764768
s_3	0.29	0.23	0.75	0.65	0.7433	611138
N_4	0.48	0.73	0.82	0.82	0.6819	256179



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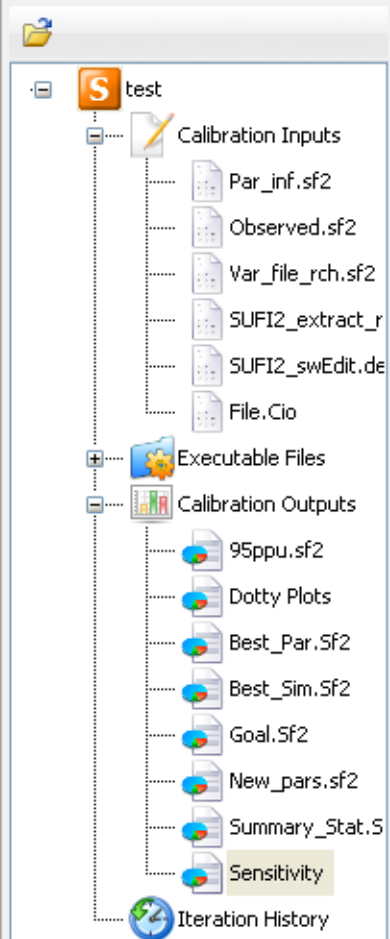
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Par_inf.sf2 | Observed.sf2 | SUFI2_extract_rch.def | 95ppu.sf2 | Dotty Plots | Goal.Sf2 | Summary_Stat.Sf2 | Sensitivity

**Sensitivity**

Parameter Name	t-Stat	P-Value
r_ALPHA_BF.gw	-1.570698190	0.177052024
v_CH_K2.rte	-0.884914156	0.416722277
v_GW_DELAY.gw	-0.685187837	0.523692215
v_CH_N2.rte	-0.410948069	0.698130054
r_SOL_AWC(1).sol_____	-0.279574449	0.791000307
r_SOL_K(1).sol_____	-0.160762679	0.878573818
v_SFTMP.bsn	-0.160692450	0.878626319
v_ALPHA_BNK.rte	-0.145360643	0.890104276
r_CN2.mgt_____1,4	-0.007925449	0.993982968
r_SOL_AWC(1).sol_____	0.119566045	0.909482520
r_SOL_BD(1).sol_____	0.446672588	0.673793633
r_SOL_BD(1).sol_____	0.792913927	0.463773734
r_SOL_K(1).sol_____	1.076260875	0.330977237
r_CN2.mgt_____PAST	2.717782435	0.041885535

Sensitivity Analysis

1. Global sensitivity analysis

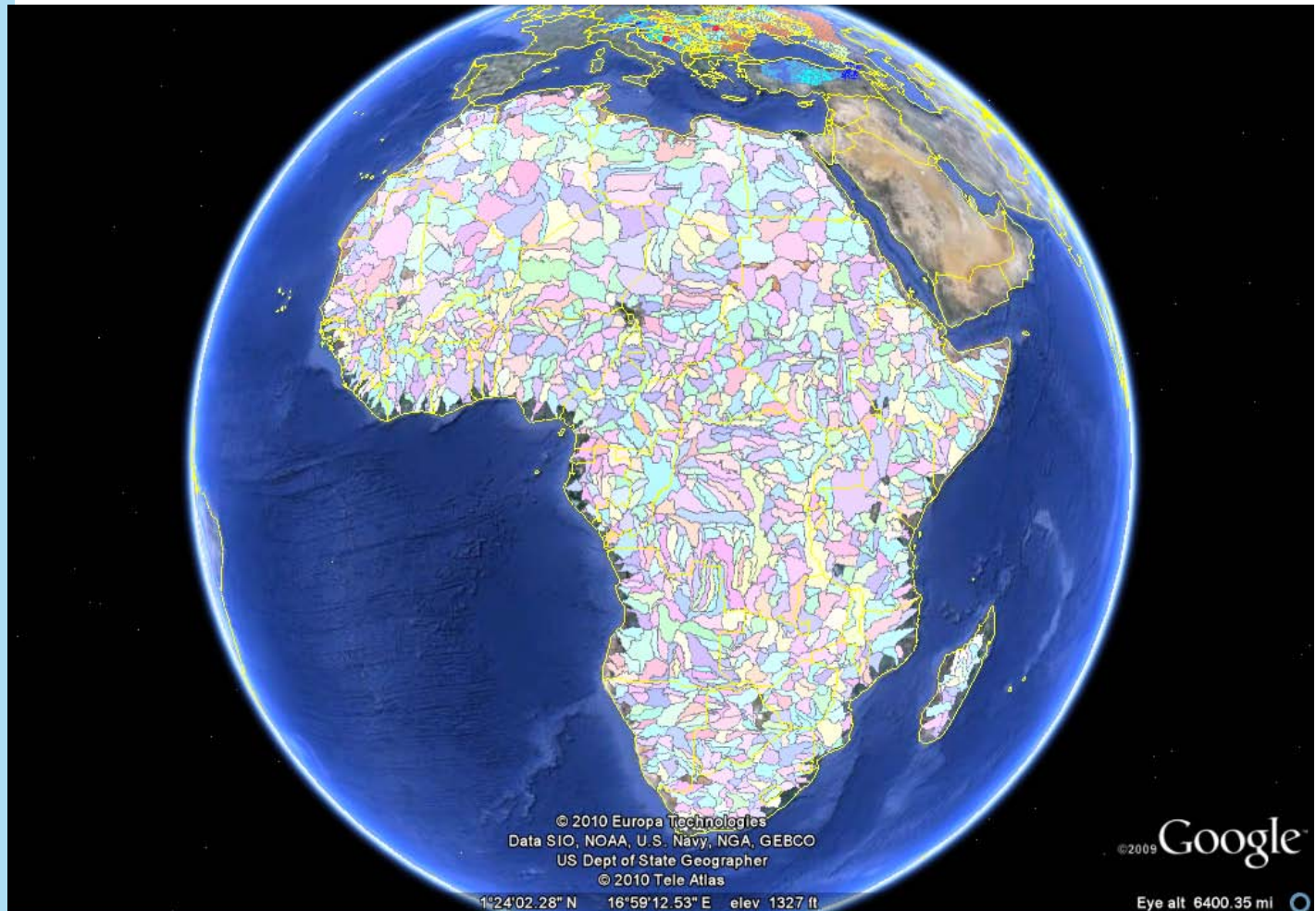
$$g_n = \alpha + \sum_{j=1}^m \beta_j b_j$$

2. Local sensitivity analysis

One-at-a-time sensitivity analysis

Future addition to SWAT-CUP

Visualization of the calibrated outputs



Future addition to SWAT-CUP

Parallelization of calibration runs

1	0.600000	0.066667	38.033333	0.029333
2	-0.066667	0.024000	36.566666	0.056000
3	0.133333	0.018667	39.500000	0.013333
4	0.333333	0.008000	43.166668	0.045333
5	0.533333	0.029333	34.366665	0.066667
6	0.400000	0.050667	35.833332	0.024000
7	0.066667	0.077333	42.433334	0.061333
8	0.266667	0.002667	37.299999	0.077333
9	0.800000	0.072000	41.700001	0.050667
10	-0.000000	0.013333	43.900002	0.034667
11	0.200000	0.034667	44.633335	0.008000
12	0.466667	0.045333	35.099998	0.040000
13	0.666667	0.056000	40.966667	0.072000
14	0.866667	0.061333	38.766666	0.002667
15	0.733333	0.040000	40.233334	0.018667

→ CPU1,1

→ CPU1,2

→ CPU2,1

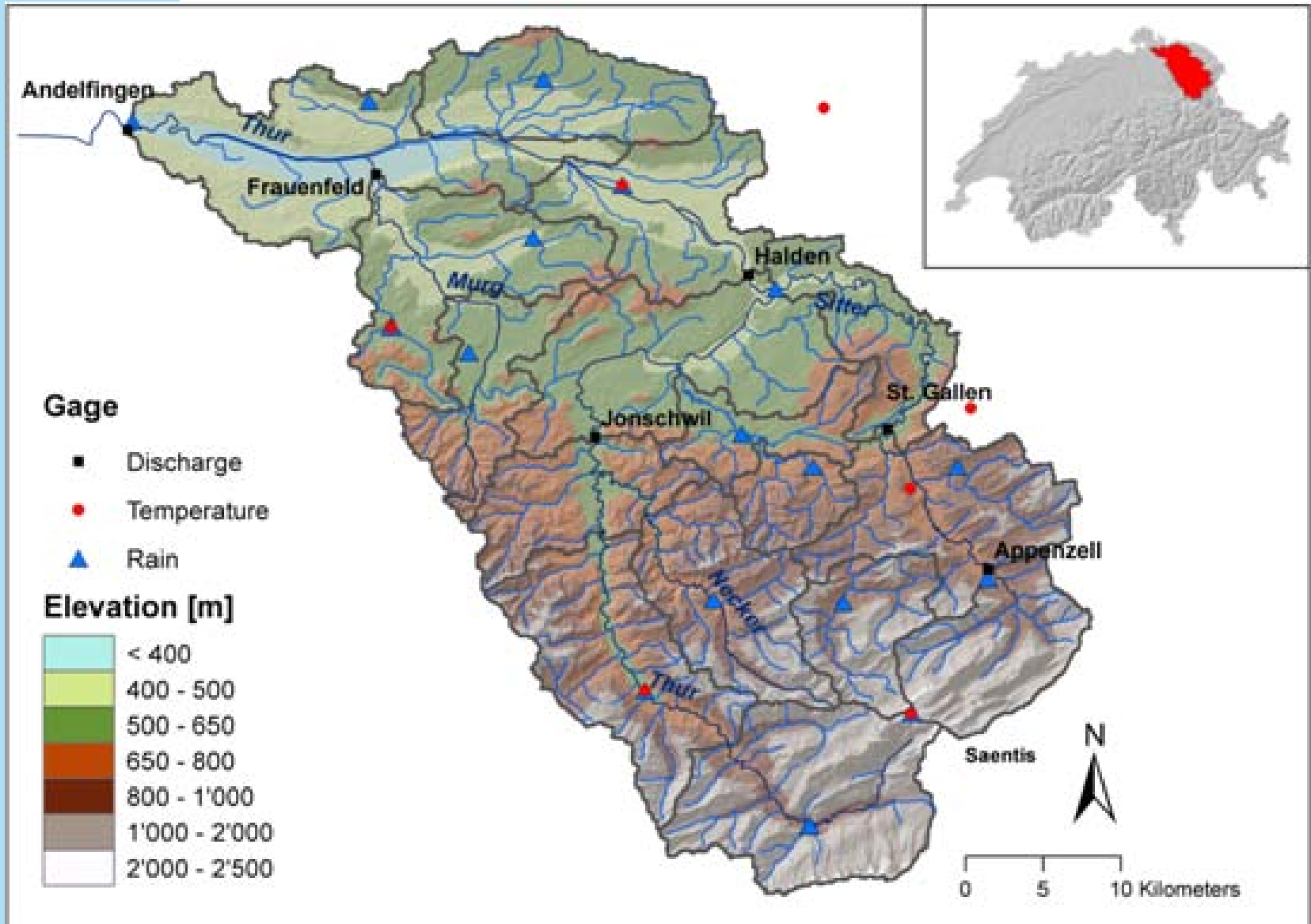
→ CPU2,2

COLLECT OUTPUT

Post
Processing

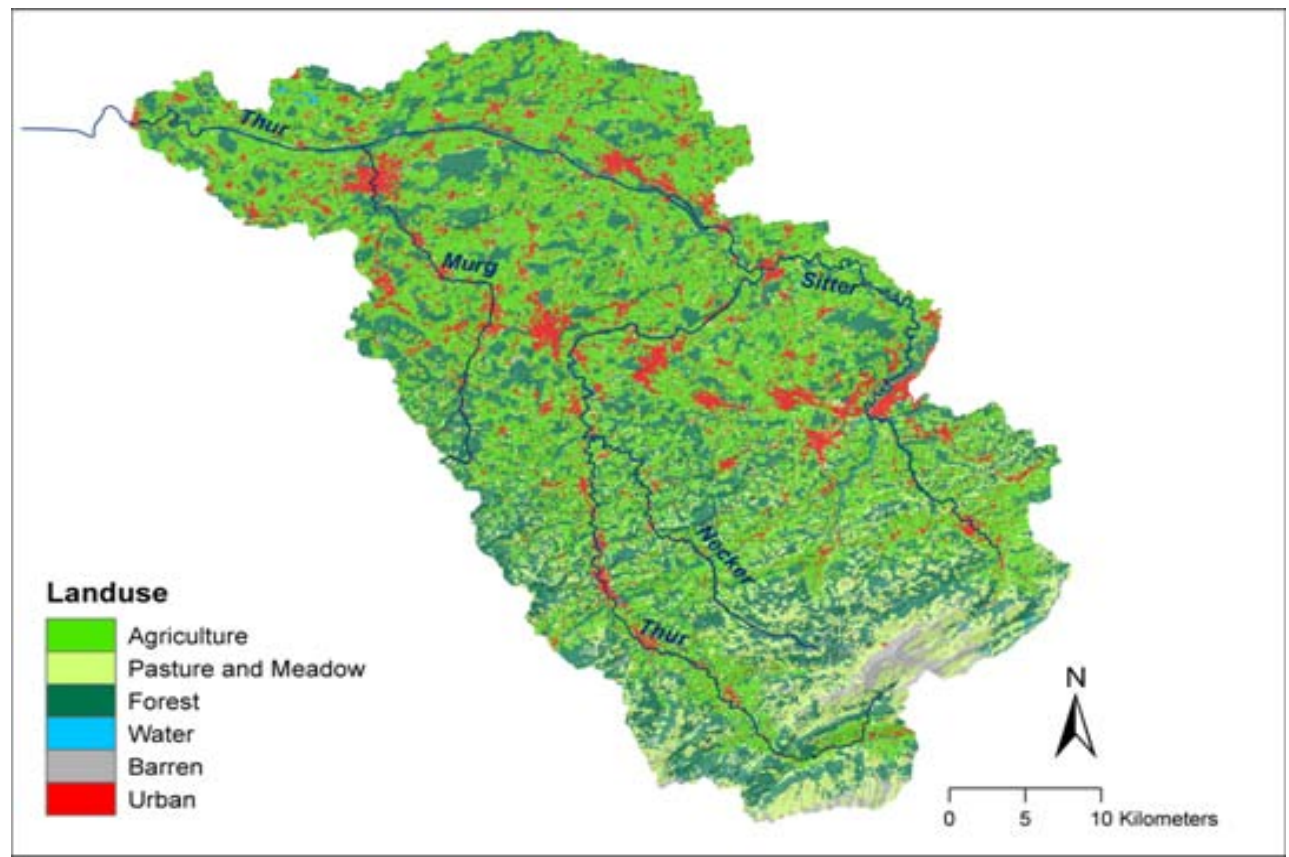
Thank you for your attention!

Thur Watershed Application



Objective Function

$$g = w_1 \sum_{i=1}^n (Q_m - Q_s)_i^2 + w_2 \sum_{i=1}^n (S_m - S_s)_i^2 + w_3 \sum_{i=1}^n (N_m - N_s)_i^2 + w_4 \sum_{i=1}^n (P_m - P_s)_i^2$$



Constrained Objective Function

$$g = w_1 \sum_{i=1}^n (Q_m - Q_s)_i^2 + w_2 \sum_{i=1}^n (S_m - S_s)_i^2 + w_3 \sum_{i=1}^n (N_m - N_s)_i^2 + w_4 \sum_{i=1}^n (P_m - P_s)_i^2$$

$$2.2 < N_{\text{forest}} < 16$$

$$19 < N_{\text{agricultural}} < 47$$

$$15 < N_{\text{pasture}} < 25$$

.....

Conditionality of Calibrated Models

A calibrated model is always conditioned on the situation that it was calibrated for and care must be taken to apply it to outside this boundary

