

SWAT-CUP

SWAT Calibration and Uncertainty Procedures

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Content

- Issues in calibrating distributed models
- SWAT-CUP

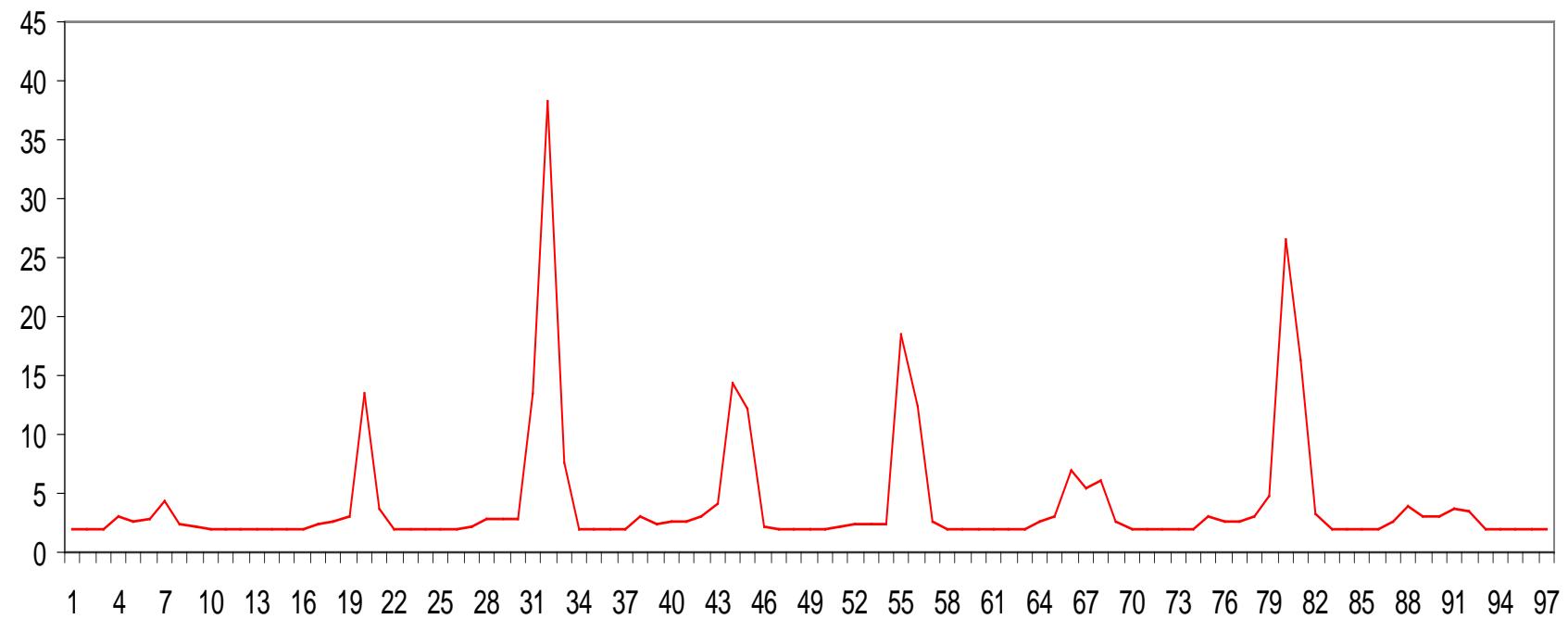
Modeling steps

- Calibration,
- Validation,
- Sensitivity analysis,
- Uncertainty analysis

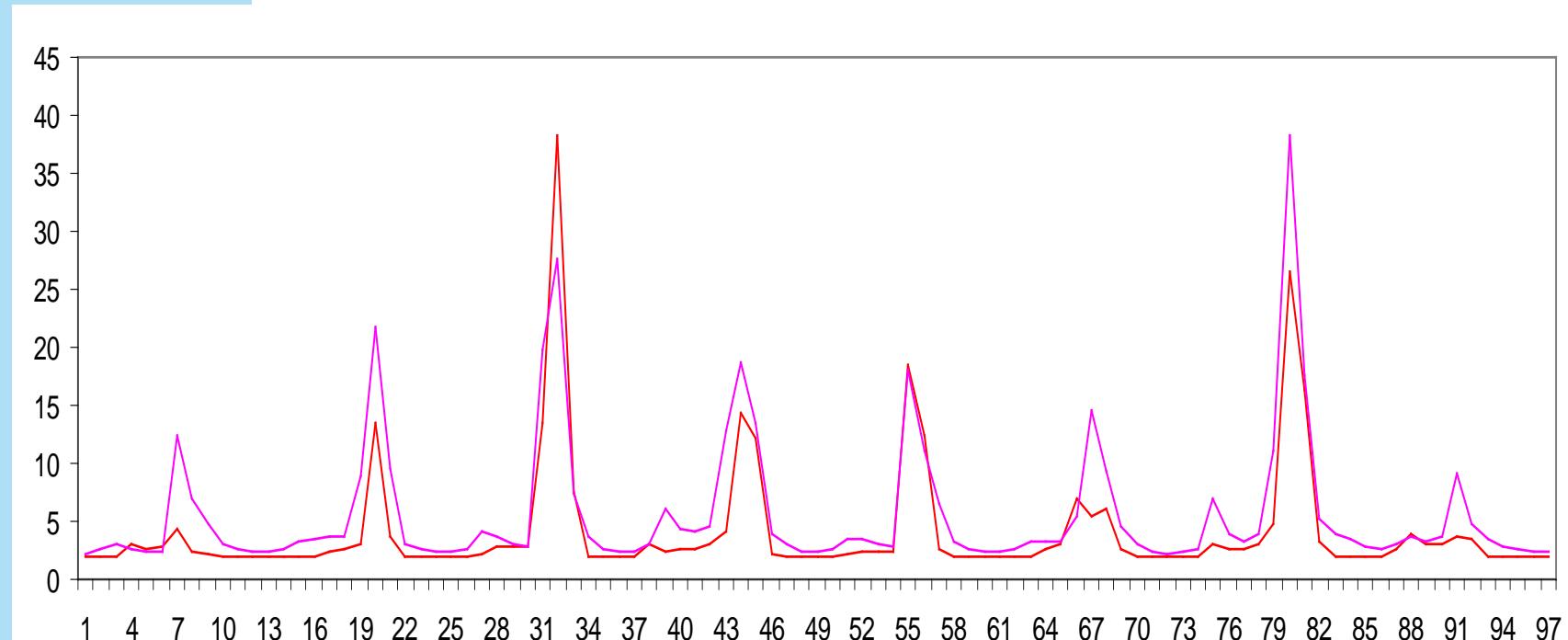
Modeling steps

- Calibration and uncertainty analysis
- Validation,
- Sensitivity analysis,

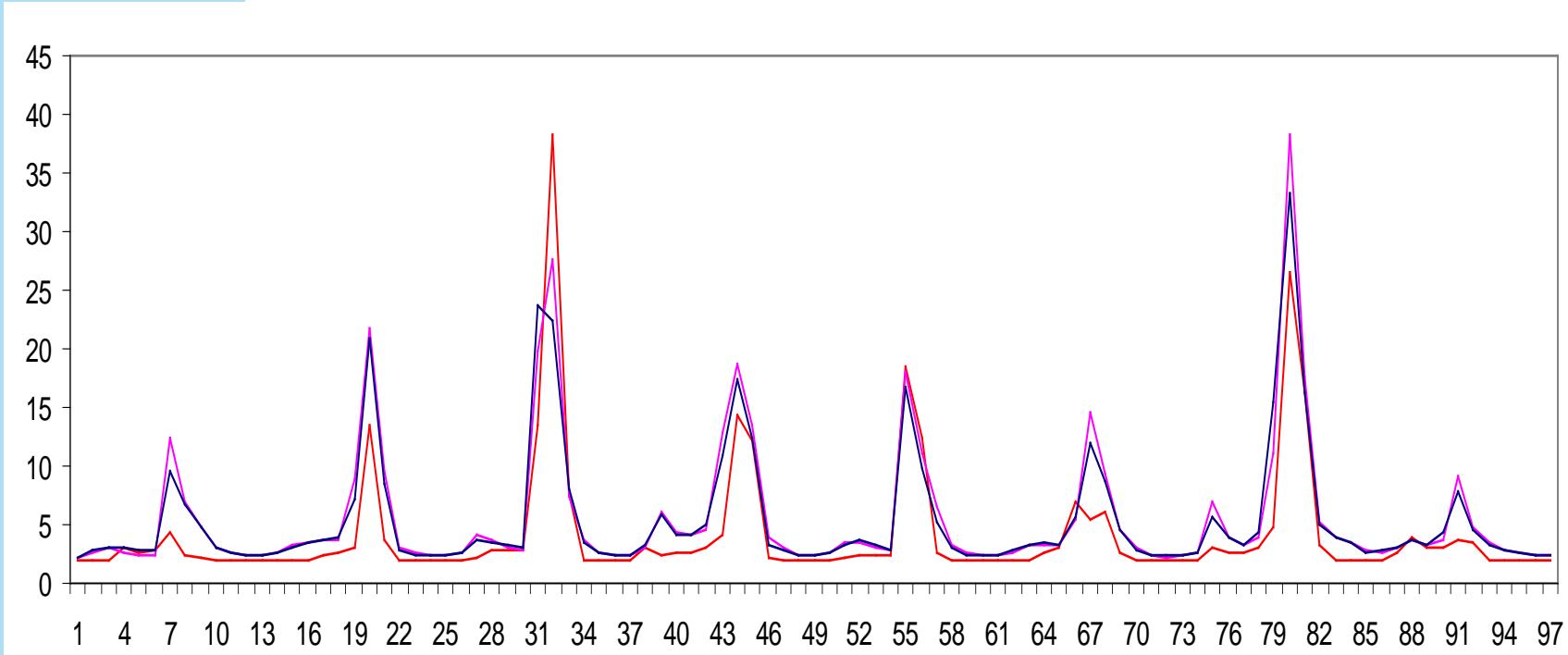
Calibration is subjective



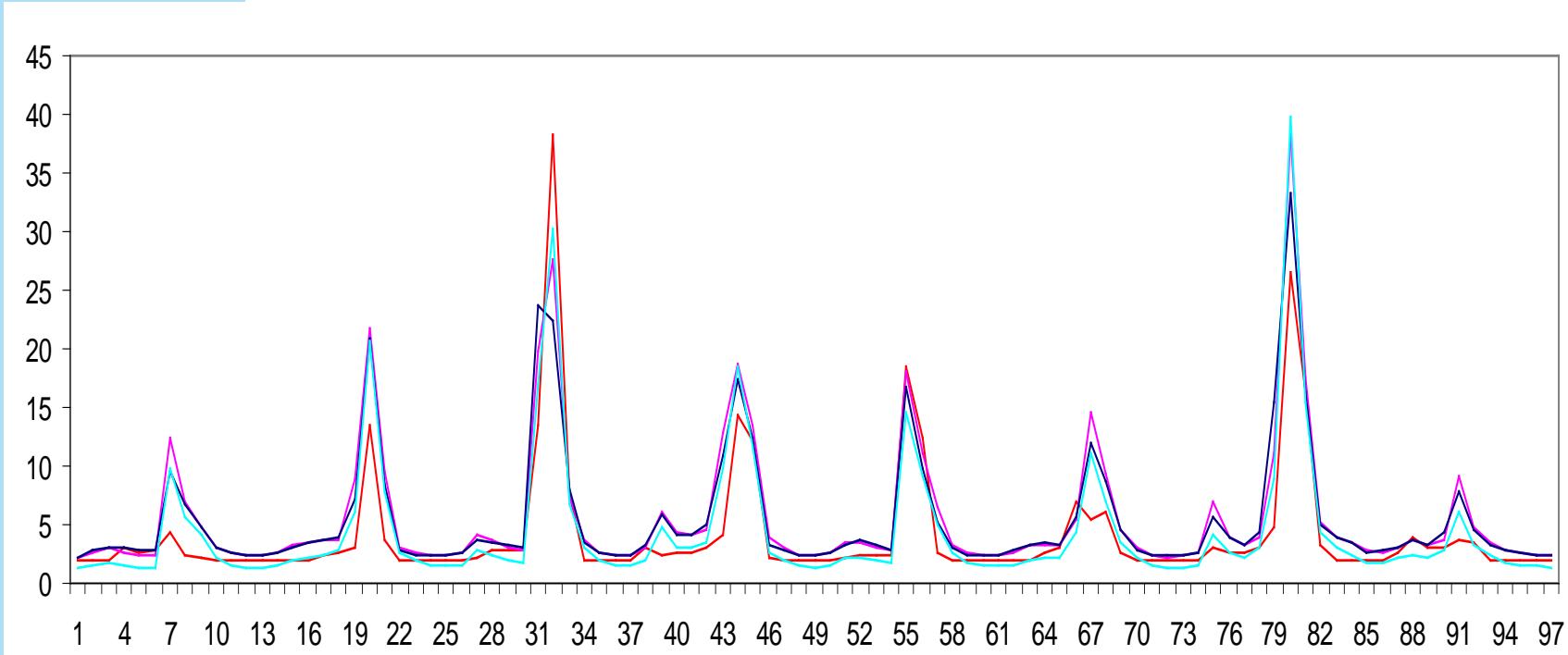
Calibration is subjective



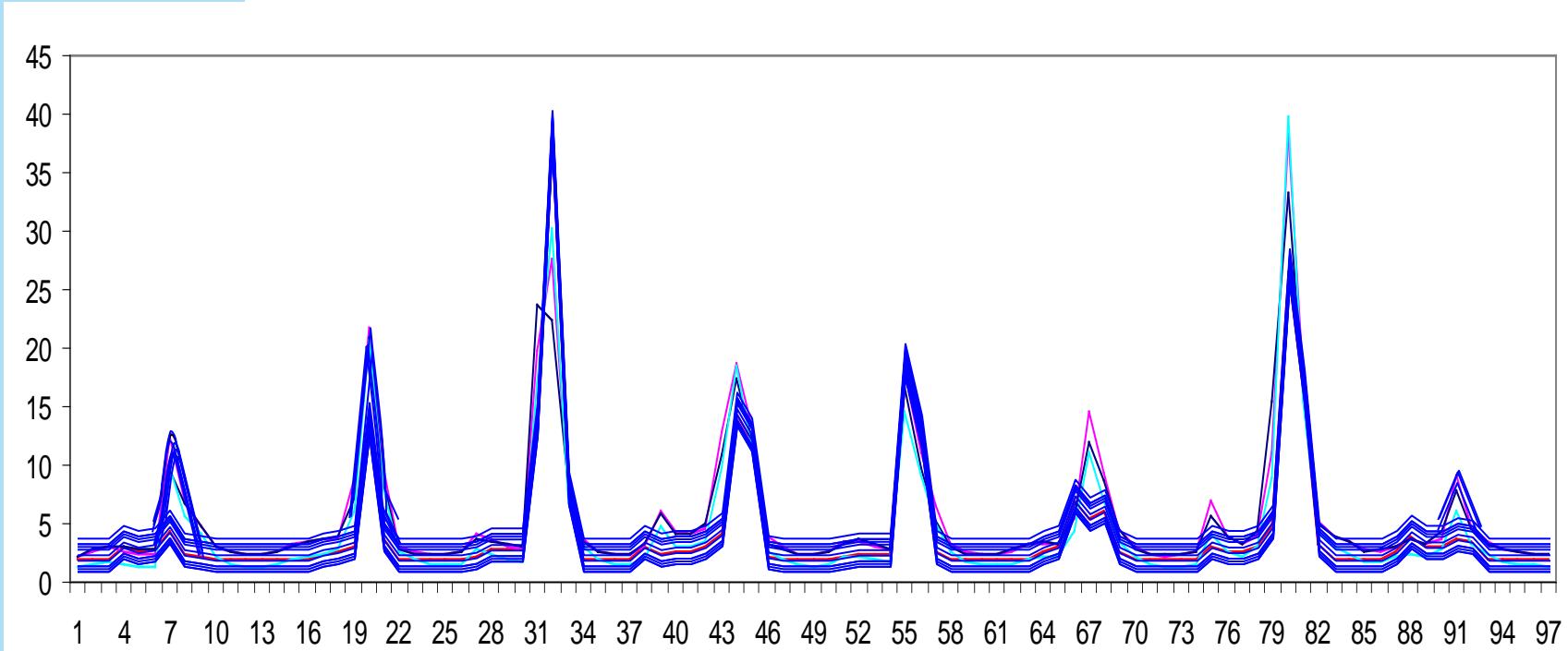
Calibration is subjective



Calibration is subjective



Calibration is subjective

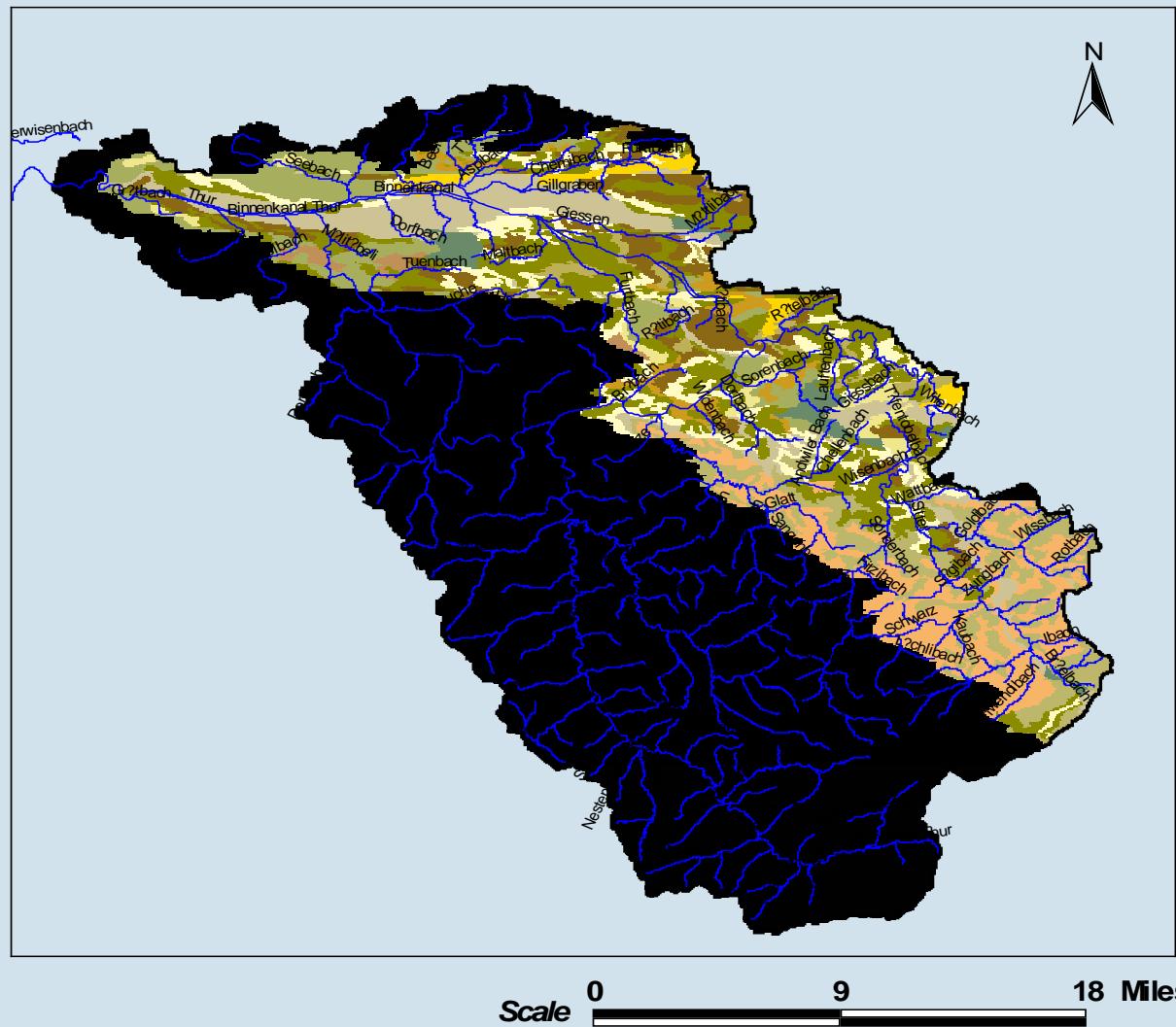
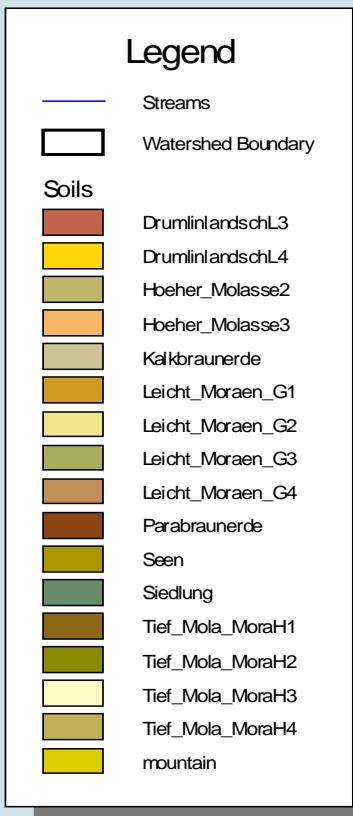


Issues in Calibration of Distributed Models

- 1- Parameterization
- 2- Objective function definition
- 3- Uniqueness problem
- 4- Parameter conditionality

1. Parameterization

Thur Basin Soil Map



1. Parameterization

Where

X

= Code to indicate the type of change to be applied to the parameter:
v – means the existing parameter value is replaced by a given value,
a – means the given value is added to the existing parameter value, and
r– means the existing parameter value is multiplied by (1+the given value);

<parname>
<ext>
<hydrogrp>
<solttext>
<landuse>
<subbsn>

Soil Parameters

Parameter identifiers	Description
r_SOL_K(1).sol	K of Layer 1 of all HRUs
r_SOL_K(1,2,4-6).sol	K of Layer 1,2,4,5, and 6 of all HRUs
r_SOL_K().sol	K of All layers and all HRUs
r_SOL_K(1).sol_D	K of layer 1 of HRUs with hydrologic group D
r_SOL_K(1).sol_FSL	K of layer 1 of HRUs with soil texture FSL
r_SOL_K(1).sol_FSL_PAST	K of layer 1 of HRUs with soil texture FSL and landuse PAST
r_SOL_K(1).sol_FSL_PAST_1-3	K of layer 1 of subbasin 1,2, and 3 with HRUs containing soil texture FSL and landuse PAST

Management Parameters

Parameter identifiers	Description
v_HEAT_UNITS{rotation no,operation no}	Management parameters that are subject to operation/rotation must have both specified

Crop Parameters

Parameter identifiers	Description
v__T_OPT{30}.CROP.DAT	Parameter T_OPT for crop number 30 in the crop.dat file
v__PLTNFR(1){3}.CROP.DAT	Nitrogen uptake parameter #1 for crop number 3 in crop.dat file

Rainfall Parameters

Parameter identifiers	Description
v_precipitation(1){1977300}.pcp	(1) means column number 1 in the pcp file {1977300} specifies year and day
v_precipitation(1-3){1977300}.pcp	(1-3) means column 1, 2, and3 {1977300} specifies year and day
v_precipitation(){1977300,1977301}.pcp	() means all columns (all stations) {1977300,1977301} means 1977 days 300 and 301
v_precipitation(){1977001-1977361,1978001-1978365,1979003}.pcp	() means all columns from day 1 to day 361 of 1977, and from day 1 to day 365 of 1978, and day 3 of 1979

2. Objective function definition

Different objective functions produce different calibration results

S-MSR

$$g(\mathbf{B}) = w_1 \sum_{i=1}^{n_1} (Q_o - Q_s)_i^2 + w_2 \sum_{i=1}^{n_2} (S_o - S_s)_i^2 + \dots$$

M-MSR

$$g(\mathbf{B}) = \sum_{i=1}^{n_1} (Q_o - Q_s)_i^2 * \sum_{i=1}^{n_2} (S_o - S_s)_i^2 * \dots$$

NS

$$g(\mathbf{B}) = \left[1 - \frac{\frac{1}{n_1} \sum_{i=1}^{n_1} (O_i - P_i)^2}{\sum_{i=1}^{n_1} (O_i - \bar{O})^2} \right]$$

2. Objective function definition

R²

$$g(\mathbf{B}) = \left[\frac{\sum_{i=1}^n (O_i - \bar{O})(P_i - \bar{P})}{\sqrt{\sum_{i=1}^n (O_i - \bar{O})^2} \sqrt{\sum_{i=1}^n (P_i - \bar{P})^2}} \right]^2$$

Chi²

$$\chi^2 = \frac{\sum_i (Q_m - Q_s)_i^2}{\sigma_Q^2}$$

bR²

$$g(\mathbf{B}) = \begin{cases} |b| \cdot R^2 & \text{for } b \leq 1 \\ |b|^{-1} \cdot R^2 & \text{for } b > 1 \end{cases}$$

2. Objective function definition

The SSQR method aims at the fitting of the frequency distributions of the observed and the simulated series. After independent ranking of the measured and the simulated values, new pairs are formed and the SSQR is calculated as

SSQR

$$SSQR = \sum_{j=1,n} [Q_{j,measured} - Q_{j,simulated}]^2$$

2. Objective function definition

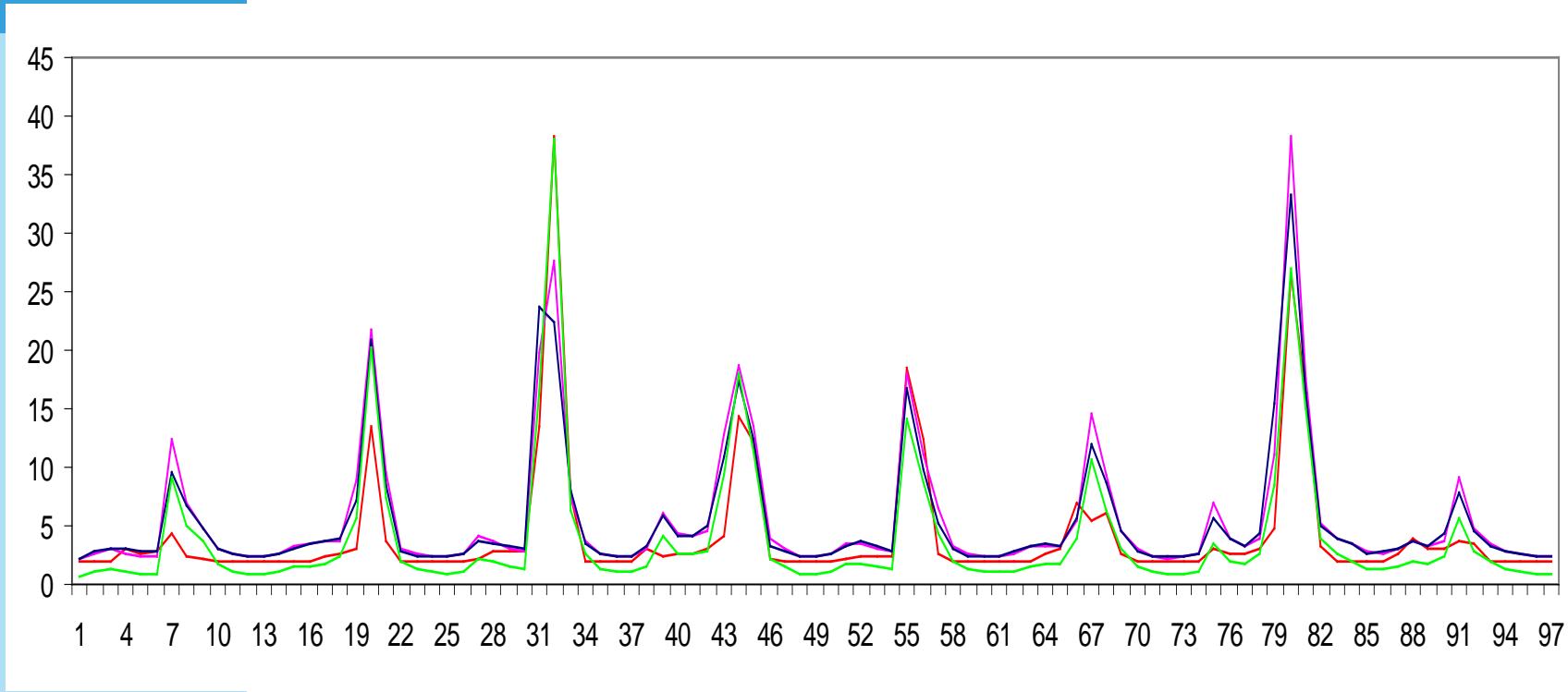
Likelihood function in a Bayesian inference using Box–Cox transformation and continuous time auto regressive function:

$$f_{\mathbf{y}^M|\boldsymbol{\theta}}(\mathbf{y}|\boldsymbol{\theta}) = \frac{1}{\sqrt{2\pi}} \frac{1}{\sigma} \exp\left(-\frac{1}{2} \frac{[g(y_{t_0}) - g(y_{t_0}^M(\boldsymbol{\theta}))]^2}{\sigma^2}\right) \cdot \left| \frac{dg}{dy} \right|_{y=y_{t_0}}$$

$$\cdot \prod_{i=1}^n \left[\frac{1}{\sqrt{2\pi}} \frac{1}{\sigma \sqrt{1 - \exp\left(-2 \frac{t_i - t_{i-1}}{\tau}\right)}} \exp\left(-\frac{1}{2} \frac{\left[g(y_{t_i}) - g(y_{t_i}^M(\boldsymbol{\theta}))\right] \exp\left(-\frac{t_i - t_{i-1}}{\tau}\right)}{\sigma^2 \left(1 - \exp\left(-2 \frac{t_i - t_{i-1}}{\tau}\right)\right)}\right)^2 \right] \cdot \left| \frac{dg}{dy} \right|_{y=y_{t_i}} \right]$$

*Yang et al., 2007, WRR,
JHydrol*

2. Objective function definition



RMSE	R2	NS	bR2
29.90	0.79	0.67	0.54
29.70	0.75	0.67	0.42
23.50	0.84	0.83	0.45
21.10	0.90	0.80	0.62
23.30	0.84	0.80	0.75

3. Uniqueness problem

Direct (deterministic) Modelling:



Inverse Modelling:



3. Uniqueness problem



So, different parameter sets can give you equally good calibration results

CN2	ALPHA_BF	REVAPMN	GW_REVAP	RCHRG_DP	SOL_AWC	SOL_K	SOL_BD
-0.20	0.25	83.4	0.05	0.09	-0.19	0.57	-0.13
0.11	0.59	66.0	0.05	0.19	-0.25	0.45	-0.19
0.33	0.35	86.1	0.07	0.19	-0.04	0.30	0.08
0.29	0.50	32.8	0.07	0.29	-0.16	0.29	-0.07

4. Parameter Conditionality

(B)

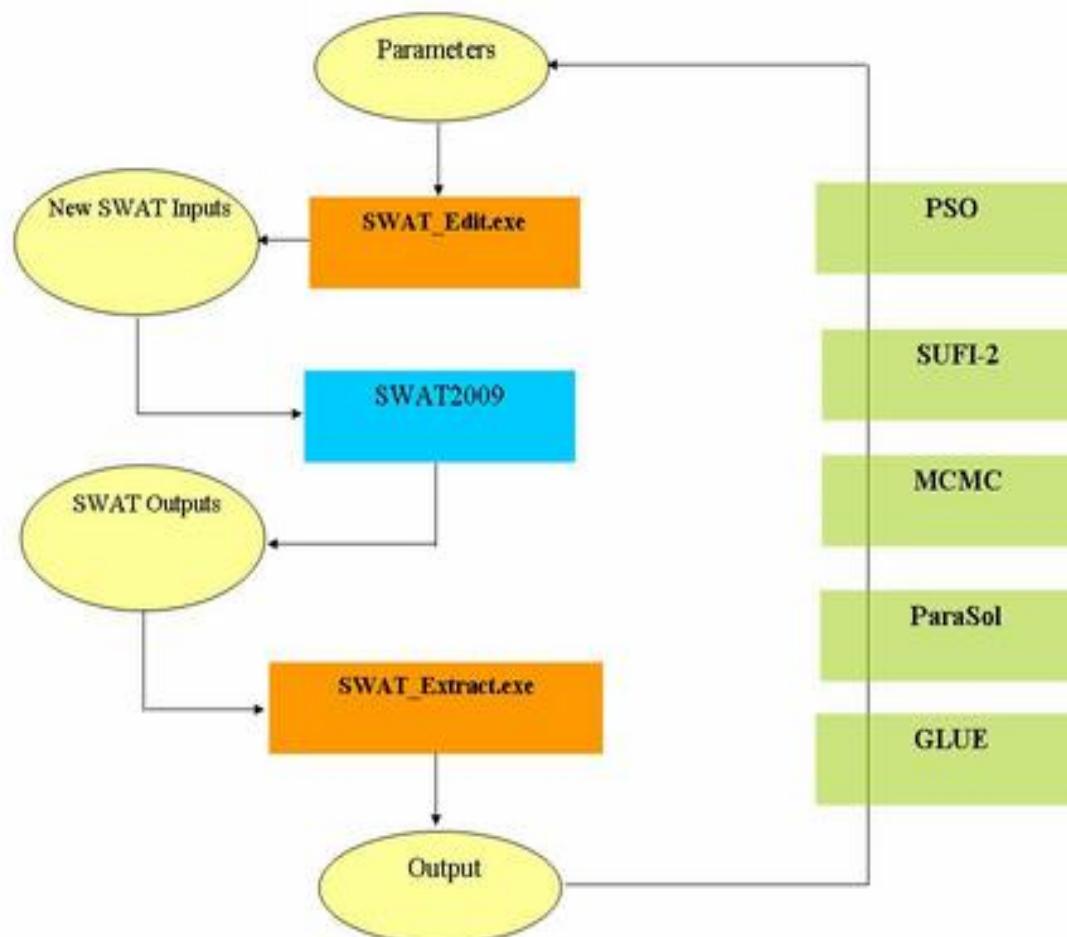
- watershed parameterization
- type of the objective function
- weights in the objective function
- conceptual model (model structure)
- experimental procedure (to collect the calibrating data)
- input (driving or forcing) data
- number and type of variables (in the objective function)
- location of outlets
-

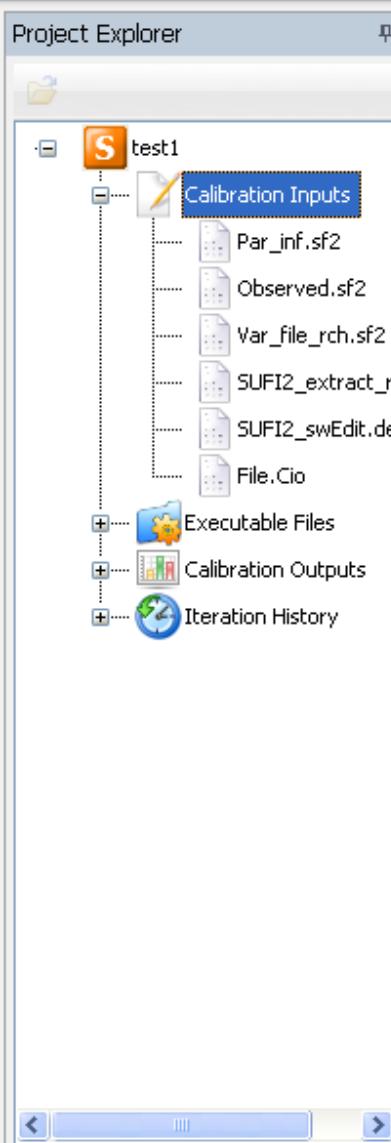
SWAT-CUP

SWAT-CUP

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 - MODAWEC
 - GEPIC

SWAT-CUP is a computer program for calibration of SWAT models. SWAT-CUP is a public domain program, and as such may be used and copied freely. The program links GLUE, ParaSol, SUFI2, MCMC, and PSO procedures to SWAT. It enables sensitivity analysis, calibration, validation, and uncertainty analysis of a SWAT model. The overall program structure is as shown in the Figure below.







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 - SUFI2_swEdit.de
 - File.Cio
 - Executable Files
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 - Iteration History

Par_inf.sf2

**Par_inf.sf2**

Sufi2 parameters information

Test_example_2009

```
Number_of_Parameters= 14
Number_of_LH_sims= 20

r__CN2.mgt_____PAST      -0.3      0.3
r__CN2.mgt_____1,4        -0.2      0.2
r__ALPHA_BF.gw              0.0       0.1
v__GW_DELAY.gw             10.0     45.0
v__CH_N2.rte                0.0       0.1
v__CH_K2.rte                5.0      40.0
v__ALPHA_BNK.rte            0.0       1.0
r__SOL_AWC(1).sol_____1,2   0.02      0.4
r__SOL_AWC(1).sol_____3,4   0.02      0.4
r__SOL_K(1).sol_____1,2    -0.5      0.8
r__SOL_K(1).sol_____3,4    -0.5      0.8
r__SOL_BD(1).sol_____1,2   -0.1      0.1
r__SOL_BD(1).sol_____3,4   -0.1      0.1
v__SFTMP.bsn                 -2.0     2.0
```

v_GW_DELAY.gw	45	29.813421	40.136478
v_ALPHA_BF.gw	45	0.320068	0.579920
v_GW_REVAP.gw	45	0.0	0.163754
v_RCHRG_DP.gw	45	0.038500	0.233160
r_SOL_K().sol	45	-0.300590	0.512008
v_ESCO.hru	45	0.391444	0.749038
v_SLSUBBSN.hru	45	18.260817	40.833183
v_CH_K2.rte	45	0.0	6.095049
r_HRU_SLP.hru	45	0.263282	0.633366

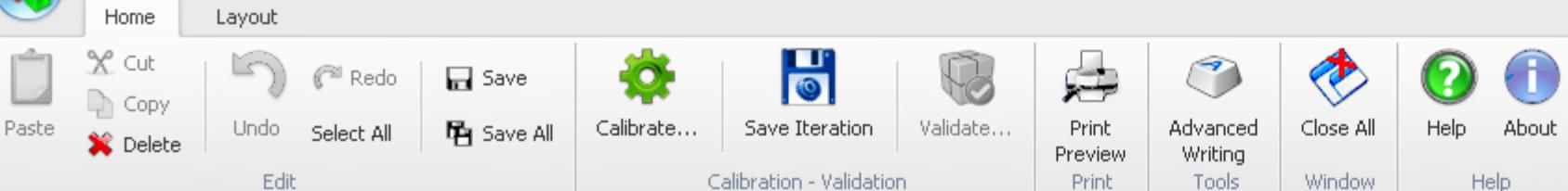
r_CN2.mgt	61	0.556328	1.020978
v_REVAPMN.gw	61	5.263700	10.631983
v_GW_REVAP.gw	61	0.083167	0.249507
v_RCHRG_DP.gw	61	0.264409	0.532161
r_SOL_K().sol	61	-0.927616	0.049724
r_SOL_BD().sol	61	0.356627	1.013543
v_ESCO.hru	61	0.02	0.235157
v_SLSUBBSN.hru	61	0.0	19.965151
v_OV_N.hru	61	0.287933	0.670415
r_CH_N2.rte	61	-0.066399	0.582939
v_ALPHA_BNK.rte	61	0.0	0.221242

r_CN2.mgt	5-11,13,14,16,18,22,23,27-30,33-35,39-41,44,47,48,50-57,59,60,63		0.348061	0.5437
r_CN2.mgt	12,15,24	-0.002354	0.682160	
r_CN2.mgt	1,2,3,4	-0.081239	0.245297	
r_CN2.mgt	17,22,31,32,36	0.435100	0.610310	
r_CN2.mgt	27,42,49,46,43	0.127156	0.425522	
r_CN2.mgt	52	-0.324336	0.006194	

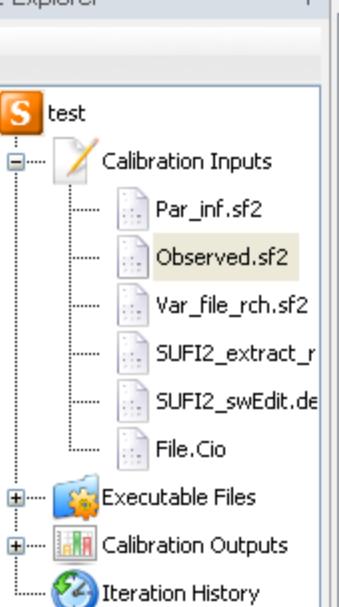
v_GW_REVAP.gw	1,2,3,4	0.129748	0.389252
v_GW_REVAP.gw	17,22,31,32,36	0.059568	0.217864
v_GW_REVAP.gw	52	0.0	0.087147

r_SOL_AWC().sol	5-16,18-25,26-30,33-35,37-41,44,47,48,50-57,59,60,63		0.070241	0.280667
r_SOL_AWC().sol	1,2,3,4	-0.118537	0.181741	
r_SOL_AWC().sol	27,42,49,46,43	0.100708	0.336324	
r_SOL_AWC().sol	52	-0.007669	0.250197	

v_ALPHA_BNK.rte	5-16,18-25,26-30,33-35,37-41,44,47,48,50-57,59,60,63		0.321167	0.628545
v_SMTMP.bsn	2.482387	5.280932		



Project Explorer



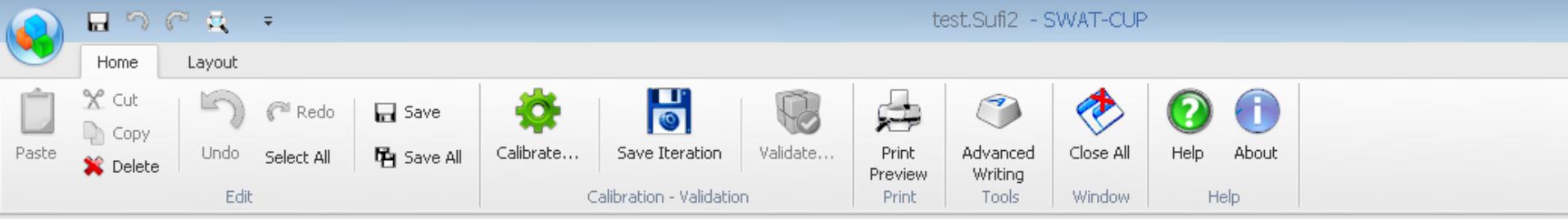
Par_inf.sf2 Observed.sf2



no_obs_vars= 5
Obj_Fn_Type(1=mult,2=sum,3=r2,4=chi2,5=NS,6=br2,7=Ssqr)= 5
behavioral_threshold=.45

q_1
var_weight= 1
var_Threshold= -1
wt_below_threshold= 1
wt_above_threshold= 1
pcnt_Error= 10
NO_Data= 21

	q_1_1977.4	0.5913
4	q_1_1977.5	0.8188
5	q_1_1977.6	0.3899
6	q_1_1977.7	0.2955
7	q_1_1977.8	0.1019
8	q_1_1977.9	0.2147
9	q_1_1977.10	1.906
10	q_1_1977.11	0.4995
11	q_1_1977.12	0.3348
12	q_1_1978.1	0.5686
13	q_1_1978.2	0.7132
14	q_1_1978.3	0.4877
15	q_1_1978.4	0.5748
16	q_1_1978.5	2.199
17	q_1_1978.6	0.5848
18	q_1_1978.7	0.1127
19	q_1_1978.8	0.0012
20	q_1_1978.9	0.8347



Project Explorer

Par_inf.sf2 Observed(sf2) SUFI2_extract_rch.def

SUFII2_extract_rch.def

```
swat_output_file=      output.rch

no_vars_to_get=      3
var_column_no[no_vars_to_get]=      7    11    18

reaches_for_each_variable[no_vars_to_get]
no_reaches_to_get=      2
reach_no=            1    2

no_reaches_to_get=      2
reach_no=            1    3

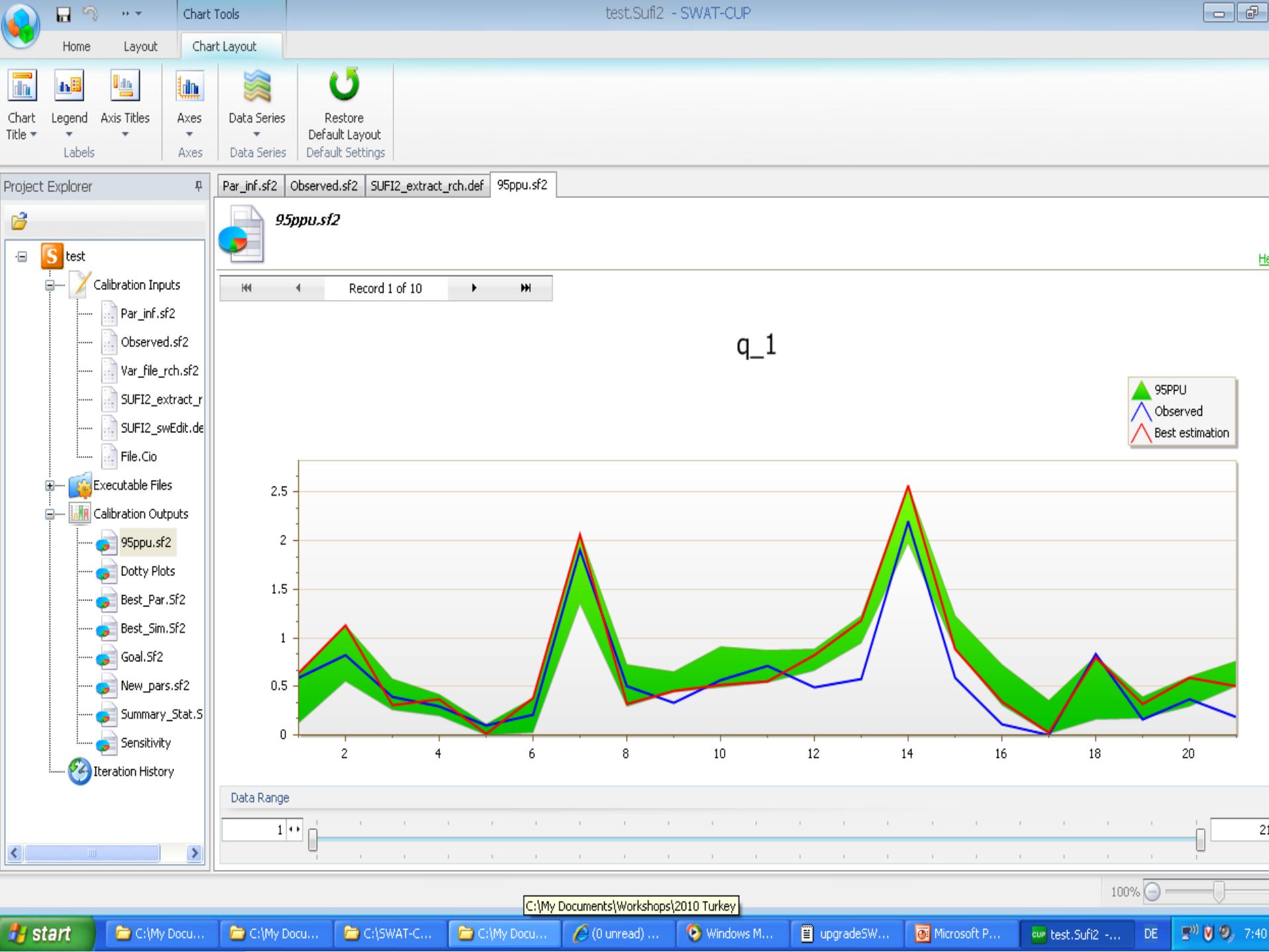
no_reaches_to_get=      1
reach_no=            4

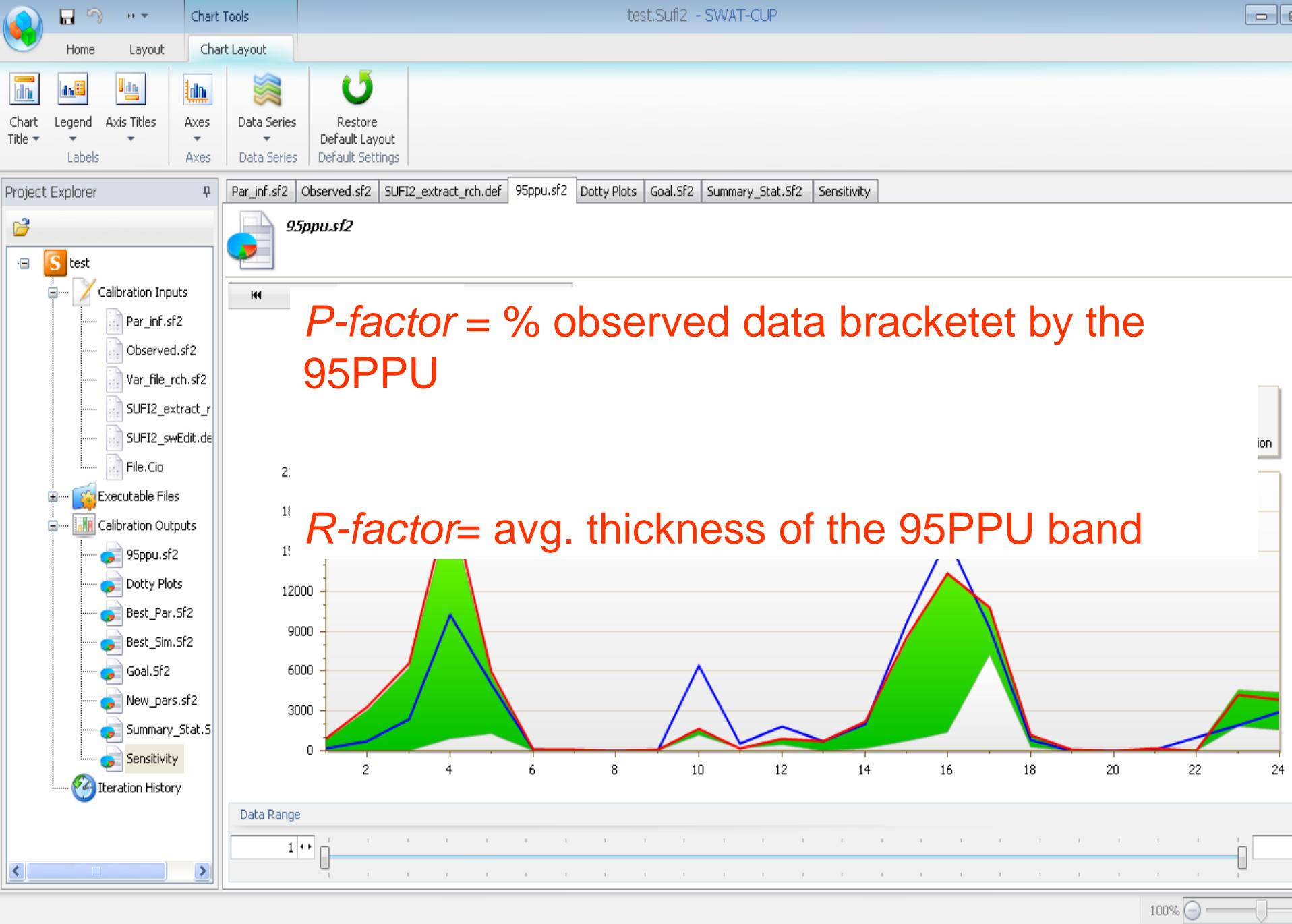
total_reaches_in_project=      4

beg_year=              1977
end_year=              1978

time_step(1d,2m,3y)=  2

/***** Remark
column_no= 7    discharge (m3/s)
column_no= 11   sed out (tn)
```







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Calibration - Validation

Project Explorer Par_inf.sf2 Observed.sf2 SUFI2_extract_rch.def 95ppu.sf2 Dotty Plots

Dotty Plots

Calibration Inputs

- Par_inf.sf2
- Observed.sf2
- Var_file_rch.sf2
- SUFI2_extract_r...
- SUFI2_swEdit.de...
- File.Cio

Executable Files

Calibration Outputs

- 95ppu.sf2
- Dotty Plots
- Best_Par.SF2
- Best_Sim.SF2
- Goal.SF2
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- Summary_Stat.S...
- Sensitivity

Iteration History

100% Zoom Factor: 100%

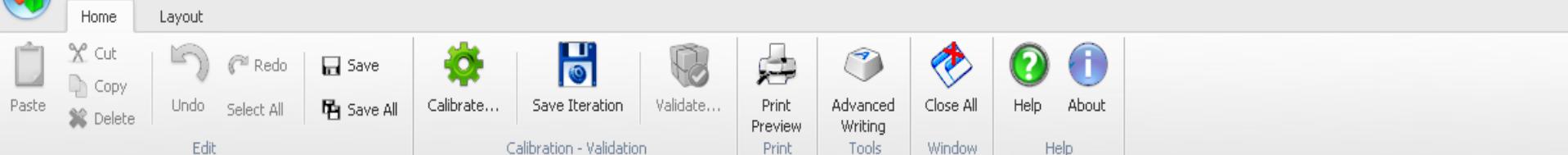
Current Page No: none Total Page No: 0

r_CN2.mgt_PAST

r_CN2.mgt_1,4

r_ALPHA_BF.gw

v_GW_DELAY.gw



Project Explorer

Par_inf.sf2	Observed(sf2)	SUFI2_extract_rch.def	95ppu.sf2	Dotty Plots	Goal.SF2
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Goal.SF2

Sim_No.	r_CN2.mgt	PAST	r_CN2.mgt	1,4	r_ALPHA_BF.gw	v_GW_DELAY.gw	v_CH_N2.rte	v_CH_K2.rte	
1	0.255000	-0.030000	0.087500	12.625000	0.007500	9.375000	0.175000	0.333500	0.048500
2	0.045000	0.190000	0.002500	30.125000	0.022500	26.875000	0.825000	0.181500	0.105500
3	-0.285000	-0.150000	0.097500	17.875000	0.027500	12.875000	0.725000	0.371500	0.029500
4	-0.225000	-0.090000	0.057500	31.875000	0.052500	16.375000	0.225000	0.200500	0.219500
5	0.285000	0.150000	0.022500	35.375000	0.072500	14.625000	0.875000	0.314500	0.086500
6	0.225000	-0.070000	0.067500	10.875000	0.097500	21.625000	0.425000	0.219500	0.181500
7	-0.075000	0.010000	0.007500	42.375000	0.087500	35.625000	0.675000	0.029500	0.333500
8	0.075000	-0.130000	0.072500	21.375000	0.092500	28.625000	0.275000	0.105500	0.162500
9	0.105000	0.130000	0.062500	23.125000	0.047500	30.375000	0.475000	0.295500	0.295500
10	-0.105000	0.090000	0.052500	33.625000	0.002500	23.375000	0.575000	0.086500	0.238500
11	-0.015000	-0.170000	0.077500	14.375000	0.032500	32.125000	0.125000	0.067500	0.390500
12	-0.165000	-0.050000	0.032500	24.875000	0.067500	7.625000	0.325000	0.352500	0.314500
13	0.165000	-0.110000	0.092500	44.125000	0.057500	25.125000	0.375000	0.162500	0.200500
14	-0.135000	0.110000	0.037500	19.625000	0.042500	19.875000	0.025000	0.238500	0.352500
15	-0.195000	0.030000	0.017500	40.625000	0.082500	5.875000	0.775000	0.143500	0.276500
16	-0.255000	-0.190000	0.082500	37.125000	0.037500	33.875000	0.625000	0.124500	0.257500
17	0.195000	0.170000	0.047500	38.875000	0.017500	37.375000	0.075000	0.257500	0.371500
18	-0.045000	-0.010000	0.027500	16.125000	0.012500	39.125000	0.925000	0.390500	0.067500
19	0.135000	0.070000	0.042500	26.625000	0.062500	18.125000	0.525000	0.276500	0.143500
20	0.015000	0.050000	0.012500	28.375000	0.077500	11.125000	0.975000	0.048500	0.124500



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**Summary_Stat.Sf2****S** test

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- SUFI2_swEdit.de
- File.Cio

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- Dotty Plots
- Best_Par.Sf2
- Best_Sim.Sf2
- Goal.Sf2
- New_pars.sf2
- Summary_Stat.S
- Sensitivity

Iteration History

Goal_type= Nash_Sutcliffe (type 5) Best_sim_no= 5 Best_goal = 7.658981e-001

Variable	p_factor	r-factor	R2	NS	br2	MSE
q_1	0.62	0.70	0.90	0.80	0.8397	0.0561
q_2	0.58	0.63	0.94	0.86	0.9317	0.0977
S_1	0.50	0.31	0.74	0.70	0.4481	764768
s_3	0.63	0.65	0.75	0.65	0.7433	611138
N_4	0.52	9.31	0.82	0.82	0.6819	256179

-- Results for behavioral parameters

Variable	p_factor	r-factor	R2	NS	br2	MSE
q_1	0.52	0.35	0.90	0.80	0.8397	0.0561
q_2	0.29	0.22	0.94	0.86	0.9317	0.0977
S_1	0.29	0.19	0.74	0.70	0.4481	764768
s_3	0.29	0.23	0.75	0.65	0.7433	611138
N_4	0.48	0.73	0.82	0.82	0.6819	256179



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 - Goal.SF2
 - New_pars.sf2
 - Summary_Stat.SF2
 - Sensitivity
 - Iteration History

Par_inf.sf2 Observed.sf2 SUFI2_extract_rch.def 95ppu.sf2 Dotty Plots Goal.SF2 Summary_Stat.SF2 Sensitivity

Sensitivity

Parameter Name	t-Stat	P-Value
r_ALPHA_BF.gw	-1.570698190	0.177052024
v_CH_K2.rte	-0.884914156	0.416722277
v_GW_DELAY.gw	-0.685187837	0.523692215
v_CH_N2.rte	-0.410948069	0.698130054
r_SOL_AWC(1).sol_____...	-0.279574449	0.791000307
r_SOL_K(1).sol_____...	-0.160762679	0.878573818
v_SFTMP.bsn	-0.160692450	0.878626319
v_ALPHA_BNK.rte	-0.145360643	0.890104276
r_CN2.mgt_____1,4	-0.007925449	0.993982968
r_SOL_AWC(1).sol_____...	0.119566045	0.909482520
r_SOL_BD(1).sol_____...	0.446672588	0.673793633
r_SOL_BD(1).sol_____...	0.792913927	0.463773734
r_SOL_K(1).sol_____...	1.076260875	0.330977237
r_CN2.mgt_____PAST	2.717782435	0.041885535

Sensitivity Analysis

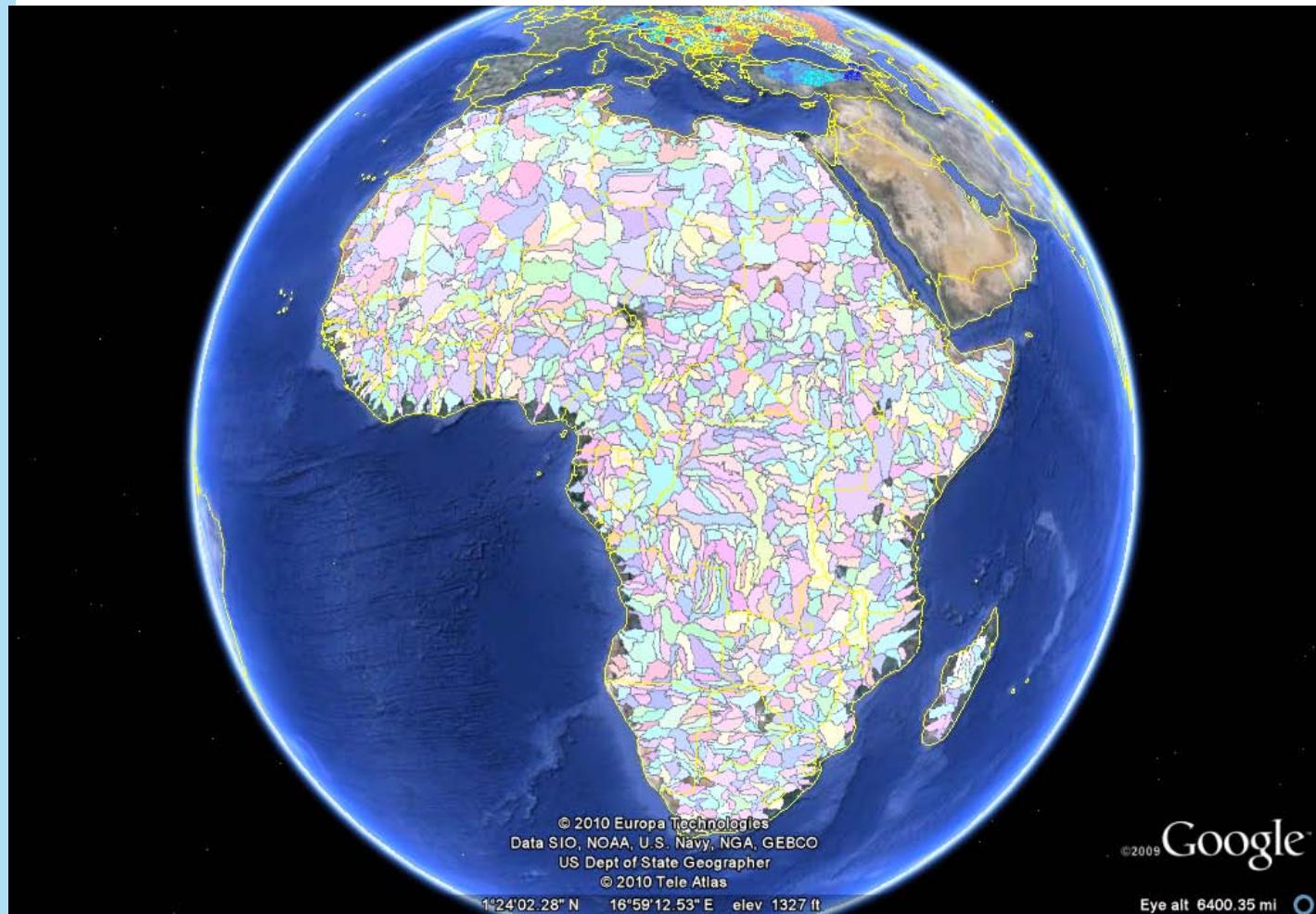
1. Global sensitivity analysis

$$g_n = \alpha + \sum_{j=1}^m \beta_j b_j$$

2. Local sensitivity analysis

One-at-a-time sensitivity analysis

Visualization of the calibrated outputs



Future addition to SWAT-CUP

Parallelization of calibration runs

1	0.600000	0.066667	38.033333	0.029333
2	-0.066667	0.024000	36.566666	0.056000
3	0.133333	0.018667	39.500000	0.013333
4	0.333333	0.008000	43.166668	0.045333
5	0.533333	0.029333	34.366665	0.066667
6	0.400000	0.050667	35.833332	0.024000
7	0.066667	0.077333	42.433334	0.061333
8	0.266667	0.002667	37.299999	0.077333
9	0.800000	0.072000	41.700001	0.050667
10	-0.000000	0.013333	43.900002	0.034667
11	0.200000	0.034667	44.633335	0.008000
12	0.466667	0.045333	35.099998	0.040000
13	0.666667	0.056000	40.966667	0.072000
14	0.866667	0.061333	38.766666	0.002667
15	0.733333	0.040000	40.233334	0.018667

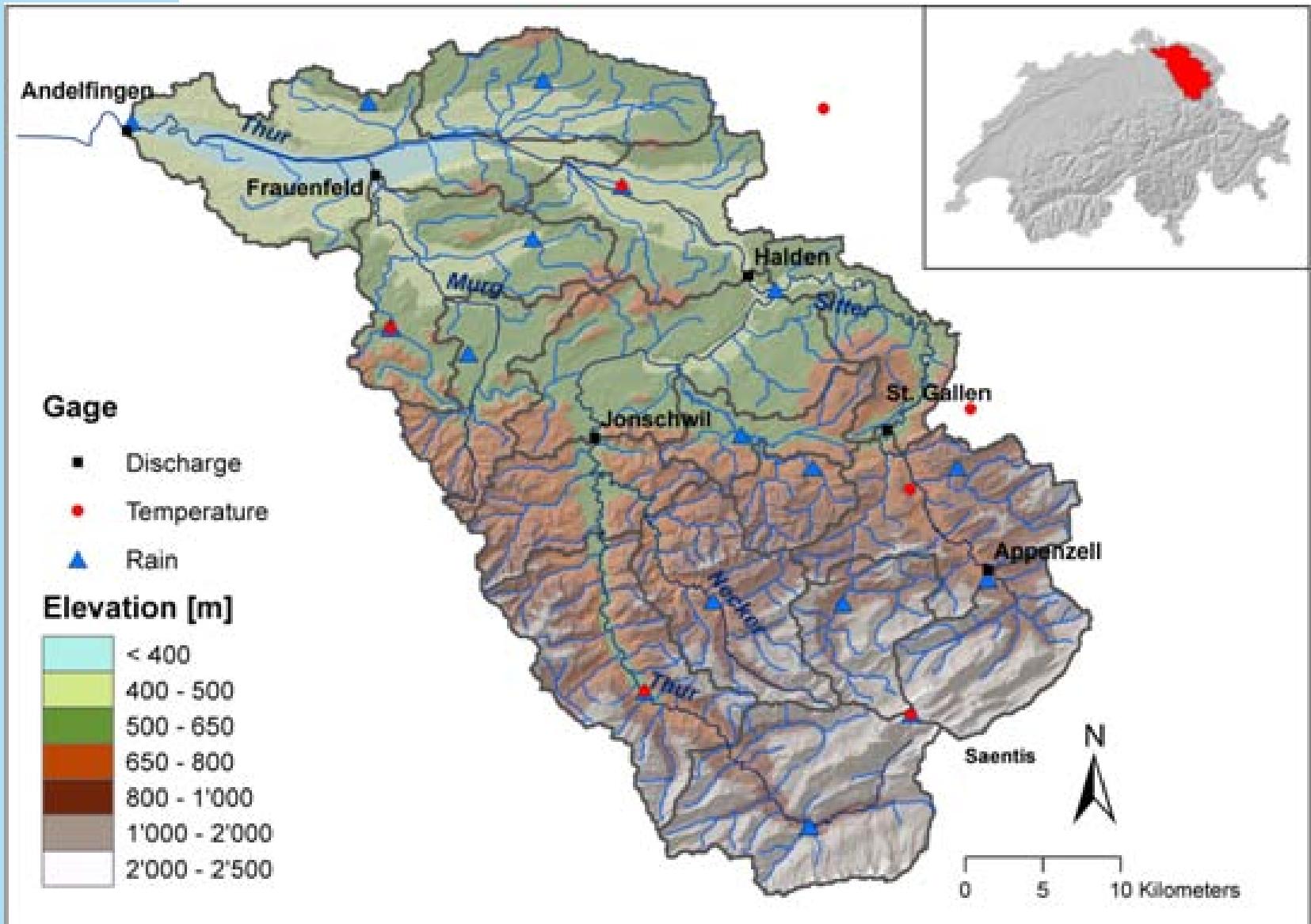
→ CPU1,1
→ CPU1,2
→ CPU2,1
→ CPU2,2

COLLECT OUTPUT

Post Processing

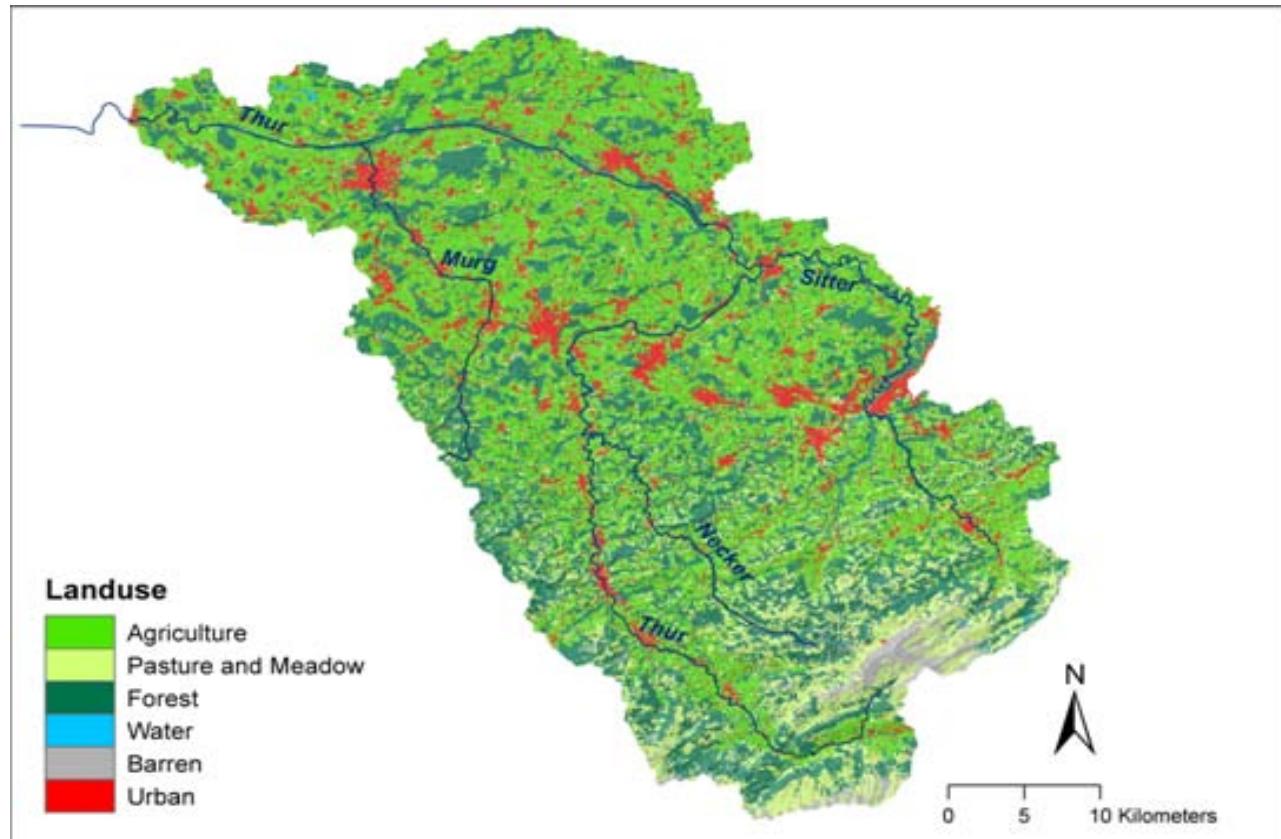
Thank you for your attention!

Thur Watershed Application



Objective Function

$$g = w_1 \sum_{i=1}^n (Q_m - Q_s)_i^2 + w_2 \sum_{i=1}^n (S_m - S_s)_i^2 + w_3 \sum_{i=1}^n (N_m - N_s)_i^2 + w_4 \sum_{i=1}^n (P_m - P_s)_i^2$$



Constrained Objective Function

$$g = w_1 \sum_{i=1}^n (Q_m - Q_s)_i^2 + w_2 \sum_{i=1}^n (S_m - S_s)_i^2 + w_3 \sum_{i=1}^n (N_m - N_s)_i^2 + w_4 \sum_{i=1}^n (P_m - P_s)_i^2$$

$$2.2 < N_{\text{forest}} < 16$$

$$19 < N_{\text{agricultural}} < 47$$

$$15 < N_{\text{pasture}} < 25$$

.....

Conditionality of Calibrated Models

A calibrated model is always conditioned on the situation that it was calibrated for and care must be taken to apply it to outside this boundary

