

# Considering Measurement Uncertainty in H/WQ Model Evaluation

Daren Harmel – USDA-ARS, Temple, TX

Patti Haan-Smith – Texas A&M Univ., College Station, TX



# Measurement Uncertainty in H/WQ Modeling

**“Should it not be required that every... (field and modeling study) ...attempt to evaluate the uncertainty in the results?”**

- Beven. 2006. On undermining the science? *Hydrol. Process.* 20:3141-3146.

**“The use of uncertainty estimation... (should be)...routine in hydrological and hydraulic science.”**

- Pappenberger and Beven. 2006. Ignorance is bliss: Or 7 reasons not to use uncertainty analysis. *Water Resources Res.* 42(5):xx-xx.

- Haan (1995) suggested that uncertainty analysis in H/WQ modeling represents intellectual integrity
- Reckhow (1994) emphasized the importance of communicating uncertainty to stakeholders and decision-makers to improve policy and management decisions

# Measurement Uncertainty in H/WQ Modeling

- An important source of uncertainty in H/WQ modeling is measurement uncertainty.
- However, when “measurement uncertainty” is included in uncertainty analysis
  - focuses almost exclusively on model inputs or parameter estimation (e.g. hydraulic conductivity, CN, fertilizer application)
  - does ***not*** address uncertainty in measured data, against which model outputs are compared (e.g. flow, water quality)
- **This research focuses on uncertainty in measured data used to calibrate, validate, or evaluate H/WQ models.**

# Measurement Uncertainty in H/WQ Modeling

- Why is the uncertainty in measured H/WQ data typically not considered in model calibration, validation, and application???
- Until recently...
- Scientists had not established an adequate understanding of uncertainty in measured H/WQ data
- No complete uncertainty (error propagation) analysis had been conducted on measured H/WQ data
- No goodness-of-fit methods had been developed to explicitly consider measurement uncertainty





# Objectives

- **Objective #1 – Briefly describe a method for estimating the “quality” of calibration, validation, and evaluation data**
  - Fundamental scientific estimates
  - Methodology for project-specific uncertainty analysis
  - Focused on uncertainty in measured streamflow and water quality data (TSS, N, P) for small watersheds
- **Objective #2 – Describe modified versions of several “goodness-of-fit” indicators that consider measurement uncertainty in H/WQ model evaluation**
  - $E_{NS}$ ,  $d$ , RMSE, MAE

# Objective 1 – Quality of Measured Data

- Root mean square error propagation method (Topping, 1972)
  - includes all steps required to measure flow and water quality data
  - widely-accepted error propagation method
    - previously used for discharge, pesticides
  - combines all potential errors to produce realistic estimates of overall error (cumulative probable uncertainty)
  - assumes potential errors are bi-directional and non-additive

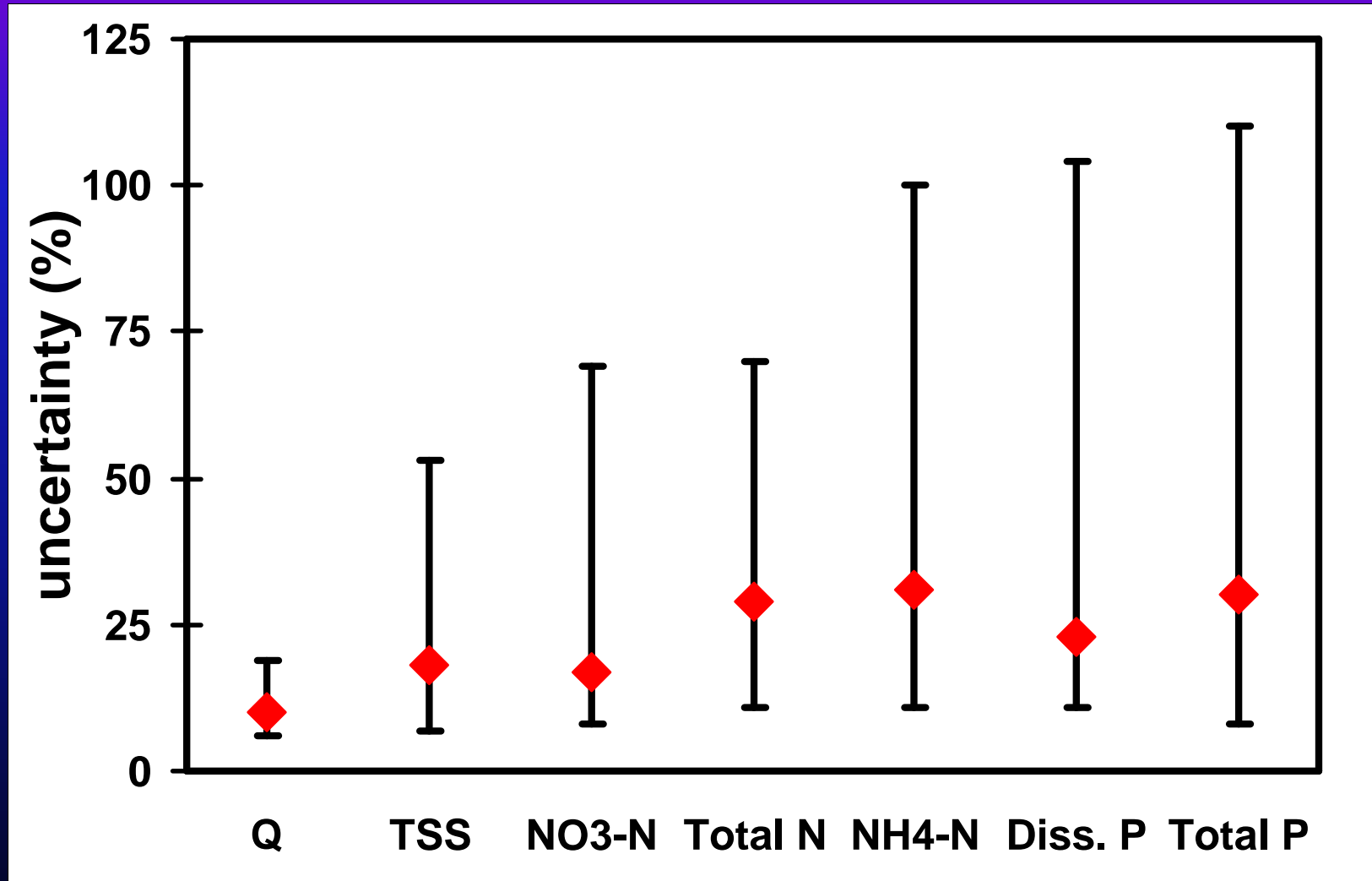
$$E_P = \sqrt{\sum_{i=1}^n (E_1^2 + E_2^2 + E_3^2 + \dots + E_n^2)}$$

# Objective 1 – Quality of Measured Data

- Created several arbitrary “data quality” scenarios
  - best case, worst case, typical – based on QA/QC, available resources, and monitoring conditions
- Categorized uncertainty sources into procedural categories
  - Q measurement, sample collection, sample preservation and storage, laboratory analysis
- Calculated cumulative uncertainty in resulting data



# Objective 1 – Quality of Measured Data





# Objective 1 – Quality of Measured Data

	Q (%)	TSS (%)	NO <sub>3</sub> -N (%)	Total P (%)
<b>Worst case scenario</b>	<b>42</b>	<b>117</b>	<b>421</b>	<b>249</b>
Typical scenario max.	19	53	69	110
Typical scenario avg.	10	18	17	30
Typical scenario min.	6	7	8	8
<b>Best case scenario</b>	<b>3</b>	<b>3</b>	<b>4</b>	<b>3</b>

**Worst  
Case**

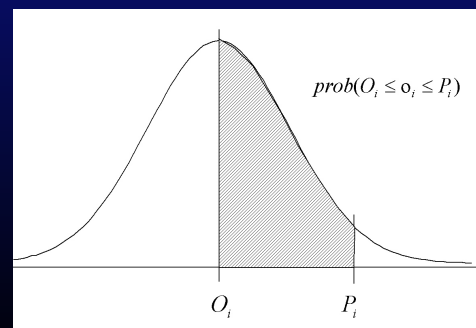
**Previous  
Data**

## Objective 2 – Modified Goodness-of-Fit Indicators

- Measurement uncertainty should be considered when evaluating H/WQ models
- Specifically, H/WQ models should:
  - not be expected to simulate/reproduce uncertain data values
  - produce output within the uncertainty range of measured data
- The error term ( $e_i = O_i - P_i$ ) appears in several popular model goodness-of-fit indicators
  - e.g.  $E_{NS}$ ,  $d$ , RMSE, MAE
- This error term should be modified to reflect measurement uncertainty

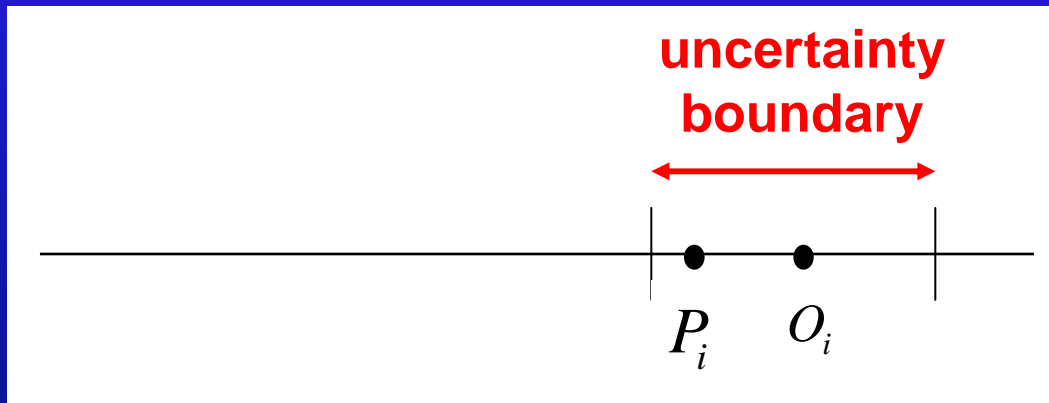
# Objective 2 – Modified Goodness-of-Fit Indicators

- Developed two error term modifications, based on available measurement uncertainty information.
  - **Modification 1** is most appropriate if:
    - only uncertainty boundary is known (+/- %)
    - probability distribution cannot be reasonably assumed
  - **Modification 2** is most appropriate if:
    - distribution of uncertainty is known or reasonably assumed

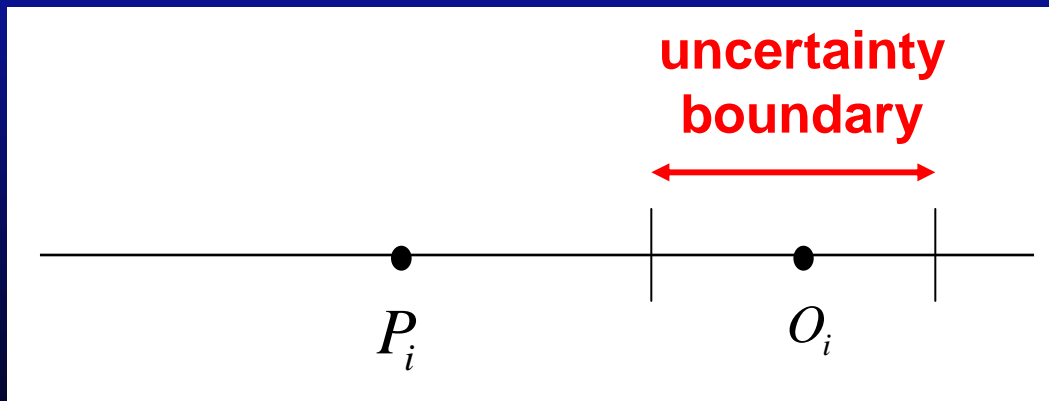


# Objective 2 – Modified Goodness-of-Fit Indicators

## Modification 1- if only uncertainty boundary is known



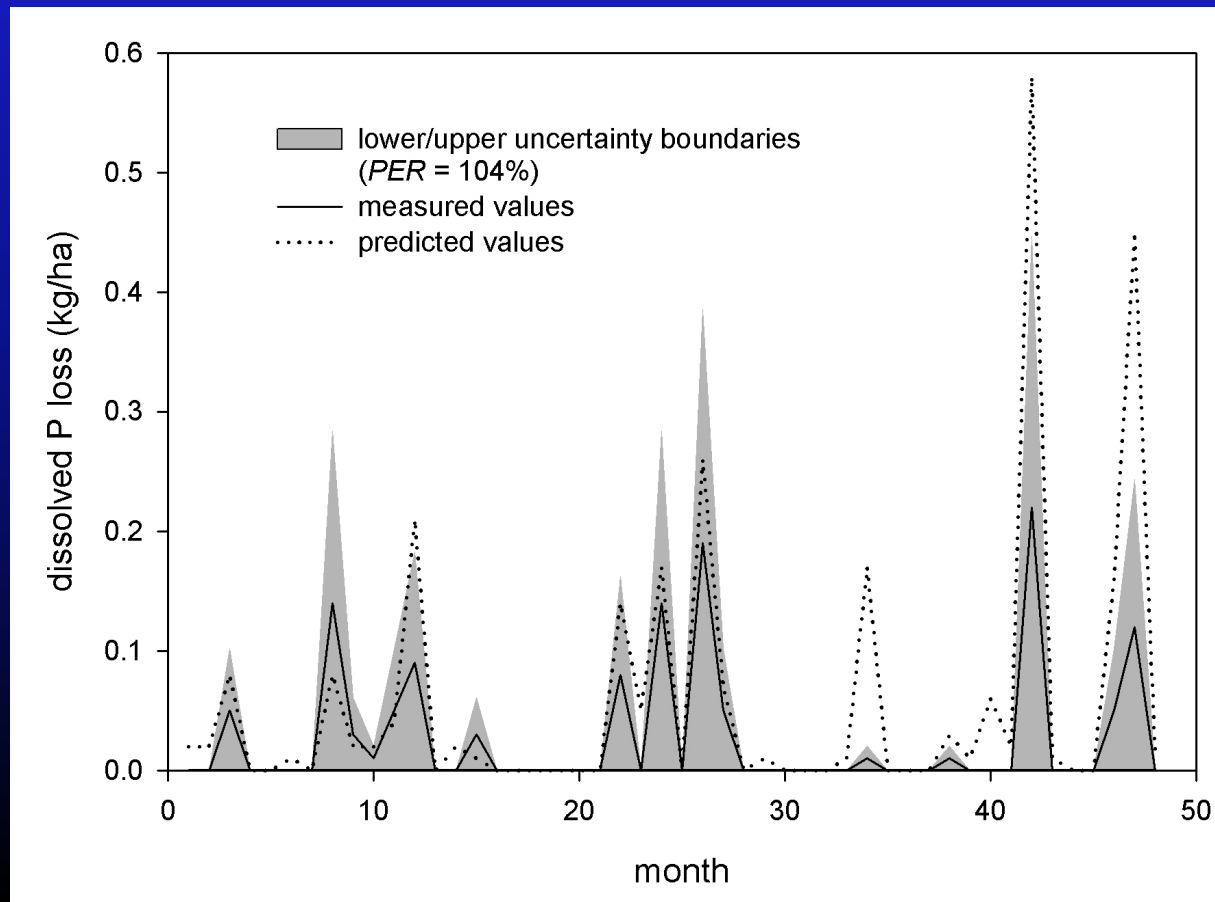
$$e_i = 0$$



$$e_i = \text{boundary} - P_i$$

# Objective 2 – Modified Goodness-of-Fit Indicators

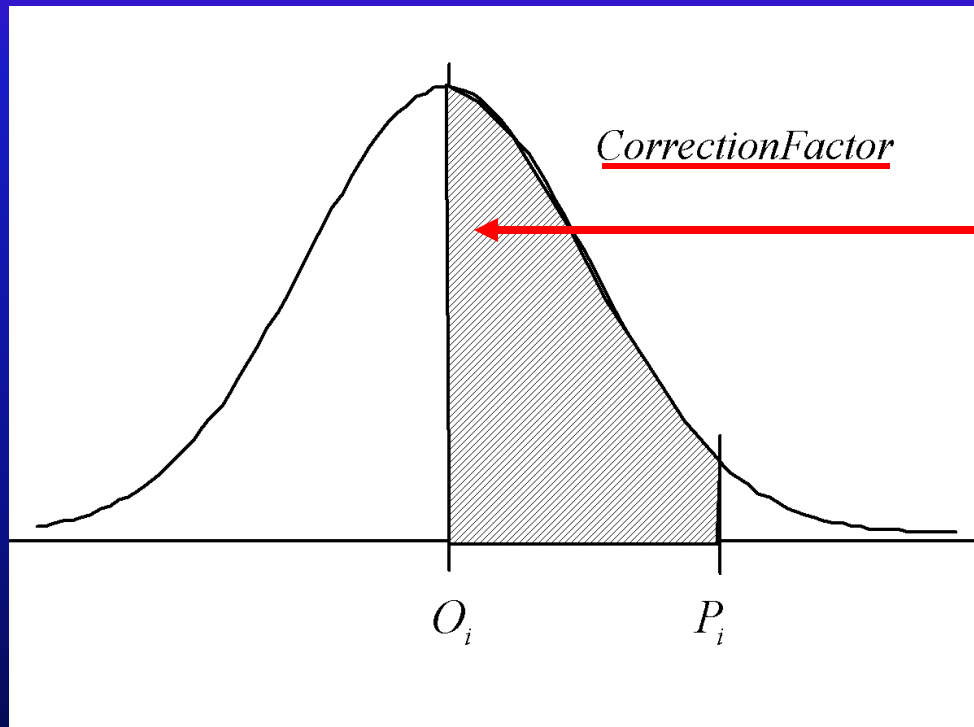
- **Modification 1** - provides conservative goodness-of-fit estimate
  - Goodness-of-fit improves substantially because minimize  $e_i$
  - Facilitates visual assessment





# Objective 2 – Modified Goodness-of-Fit Indicators

## Modification 2 - if distribution of uncertainty is known

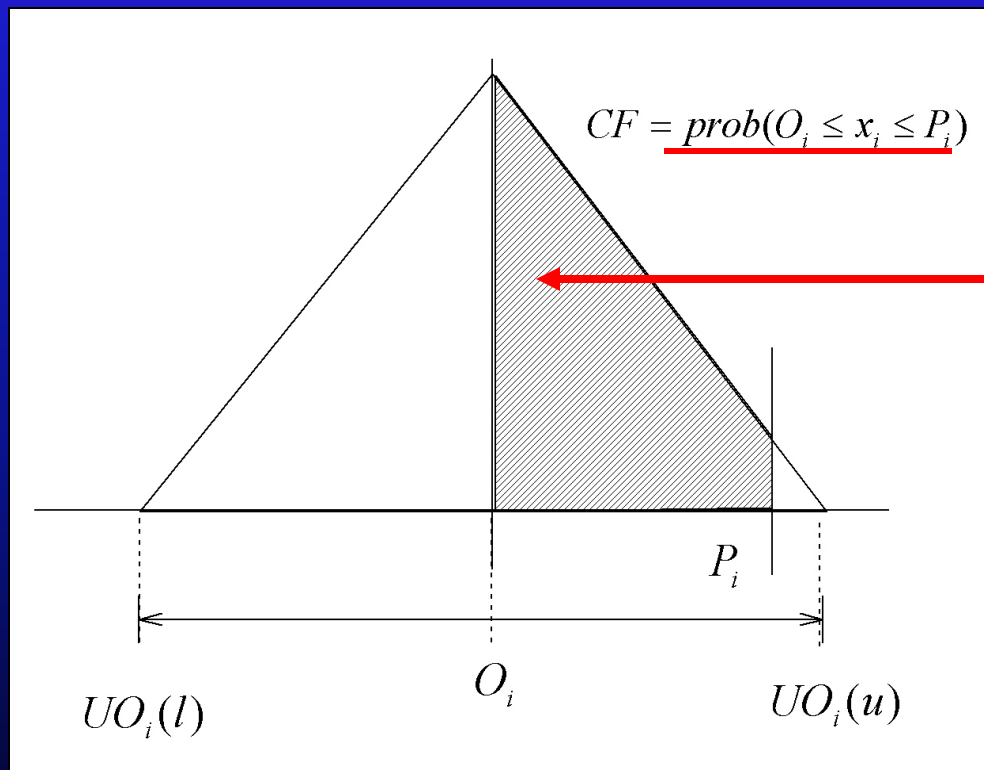


$$e_i = \frac{CF_i}{0.5} \times (O_i - P_i)$$

In Modification 2, the probability distributions represent possible measured values for each point ( $O_i$ ) not for the entire population of measured data.

# Objective 2 – Modified Goodness-of-Fit Indicators

## Modification 2 - if distribution of uncertainty is known



$$e_i = \frac{CF_i}{0.5} \times (O_i - P_i)$$

# Objective 2 – Modified Goodness-of-Fit Indicators

- Modification 2 – provides more realistic estimate of  $e_i$  when distributional information of measurement uncertainty known or reasonably assumed
  - Goodness-of-fit increased only slightly for measured data with little uncertainty.
  - Modest improvement when data with substantial uncertainty were compared with both poor and good model predictions.
  - **Important result** - poor performance shouldn't appear satisfactory because of measurement uncertainty, especially for large model structure errors

# Recent Model-Related Uncertainty Pubs.

Harmel, et al. 2006. Cumulative uncertainty in measured streamflow and water quality data for small watersheds. *Trans. ASABE* 49(3): 689-701.

Shirmohammadi, et al. 2006. Uncertainty in TMDL models. *Trans. ASABE* 49(4):1033-1049.

Harmel and Smith. 2007. Consideration of Measurement Uncertainty in the Evaluation of Goodness-of-Fit in Hydrologic and Water Quality Modeling. *J. Hydrology* 337:326-336.

Moriasi, et al. 2007. Model evaluation guidelines for systematic quantification of accuracy in watershed simulations. *Trans. ASABE* 50(3):xxx-xxx.

# Conclusion and Acknowledgments

- **Conclusions related to H/WQ modeling...**
  - no longer acceptable to not consider uncertainty in H/WQ modeling
  - advantageous for modelers to quantify the “quality” calibration, validation, and evaluation data
- **Insight and groundbreaking work by many contributed to the foundation for this research.**
  - **Richard Cooper, Ken Reckhow, Keith Beven, Florian Pappenberger, Dmitri Kavetski, Ann van Griensven (and her colleagues), Bruce Beck, Tom Haan, Dan Storm, Raymond Slade.**



# Upcoming Research on H/WQ Data Uncertainty

- Refine the uncertainty estimation method to facilitate estimation in measured H/WQ data
  - Procedure, field/data form, simple spreadsheet
- Push for increased emphasis on sample collection in QA
- Emphasize benefits of uncertainty estimates accompanying measured H/WQ data sets
- **Apply modified goodness-of-fit indicators in H/WQ modeling and other fields**
- **Incorporate uncertainty estimates and modified goodness-of-fit indicators in SWAT,EPIC/APEX interface**



**Any Questions??**

**Daren Harmel, PhD  
USDA-ARS  
808 E. Blackland Rd.  
Temple, TX**

**(254) 770-6521**

**[dharmel@spa.ars.usda.gov](mailto:dharmel@spa.ars.usda.gov)**

**<http://www.ars.usda.gov/spa/dharmel>**